

# Studying wave dynamics in turbulent flows via space and time resolved spectra

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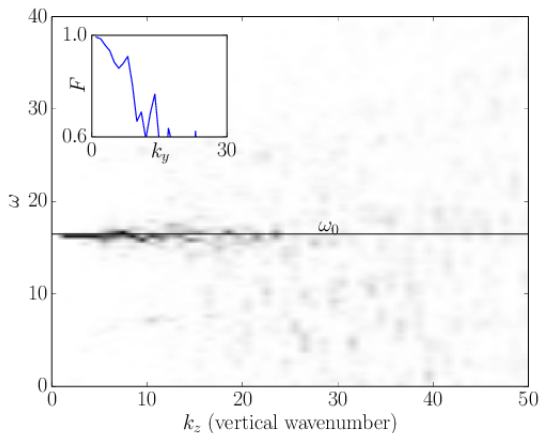
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- ▶ Characterization of the effect of waves, and measurements of the amount of energy in wave modes has been done mostly **indirectly**.
- ▶ By calculating space and time resolved spectra from DNS we study **directly** the effect wave motions in turbulent flows.

## Rotating flow (Navier Stokes in rotating frame)

$$E(k, \omega)$$

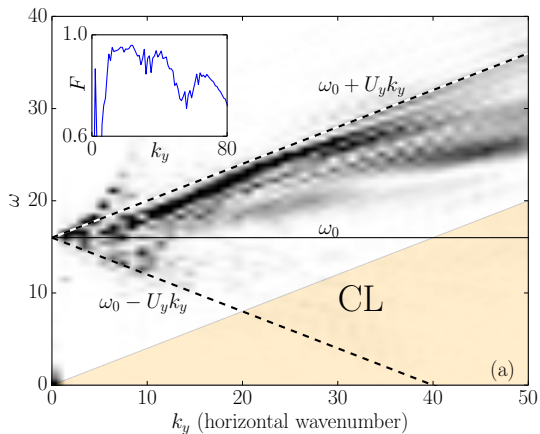
Only In the larger scales energy accumulates along modes satisfying the dispersion relation of inertial waves!



*Clark di Leoni, Cobelli, Mininni, Dmitruk & Matthaeus, PoF (2014)*

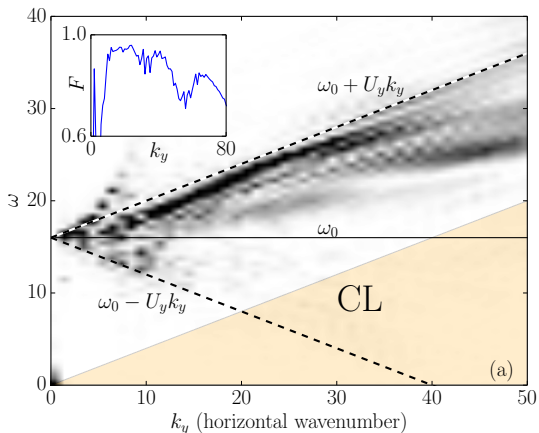
# Stratified flow (Boussinesq model with no rotation)

$E(k, \omega)$



## Stratified flow (Boussinesq model with no rotation)

$E(k, \omega)$



Doppler shifting and Critical Layer absorption appear! This indicates a nonlocal transfer of energy from the small to the large scales. *Clark di Leoni and Mininni, PRE (in press)*

## Superfluid turbulence (Gross-Pitaevskii equation)

Nonlinear PDE describing a Bose Einstein condensate for wavefunction  $\psi$

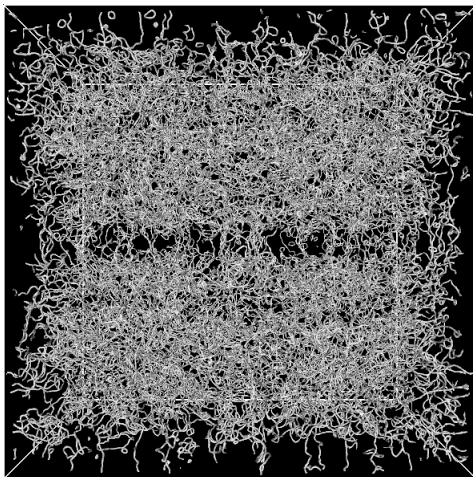
$$\psi(\mathbf{r}, t) = \sqrt{\frac{\rho(\mathbf{r}, t)}{m}} e^{i\frac{m}{\hbar}\phi(\mathbf{r}, t)}$$

Vorticity is quantized and concentrated along lines with  $\rho = 0$



# Superfluid turbulence (Gross-Pitaevskii equation)

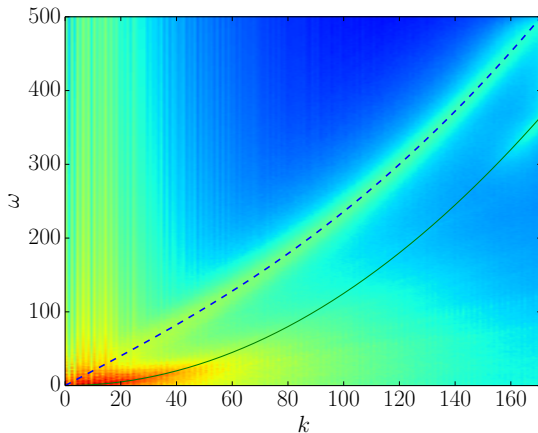
$\rho(\mathbf{r})$



# Superfluid turbulence (Gross-Pitaevskii equation)

$$\rho(k, \omega)$$

Sound and kelvin waves!



In collaboration with Marc Brachet

# Superfluid turbulence (Gross-Pitaevskii equation)

$$\rho(k, \omega)$$

