

Turbulence on the water surface and vorticity generation by waves

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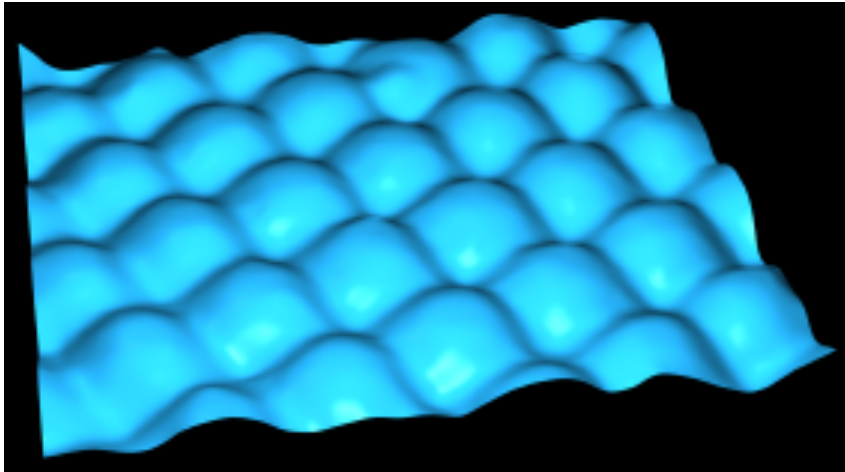
The Australian National University,
Canberra, Australia

Collaborators: H. Xia, N. Francois, H. Punzmann, G. Falkovich

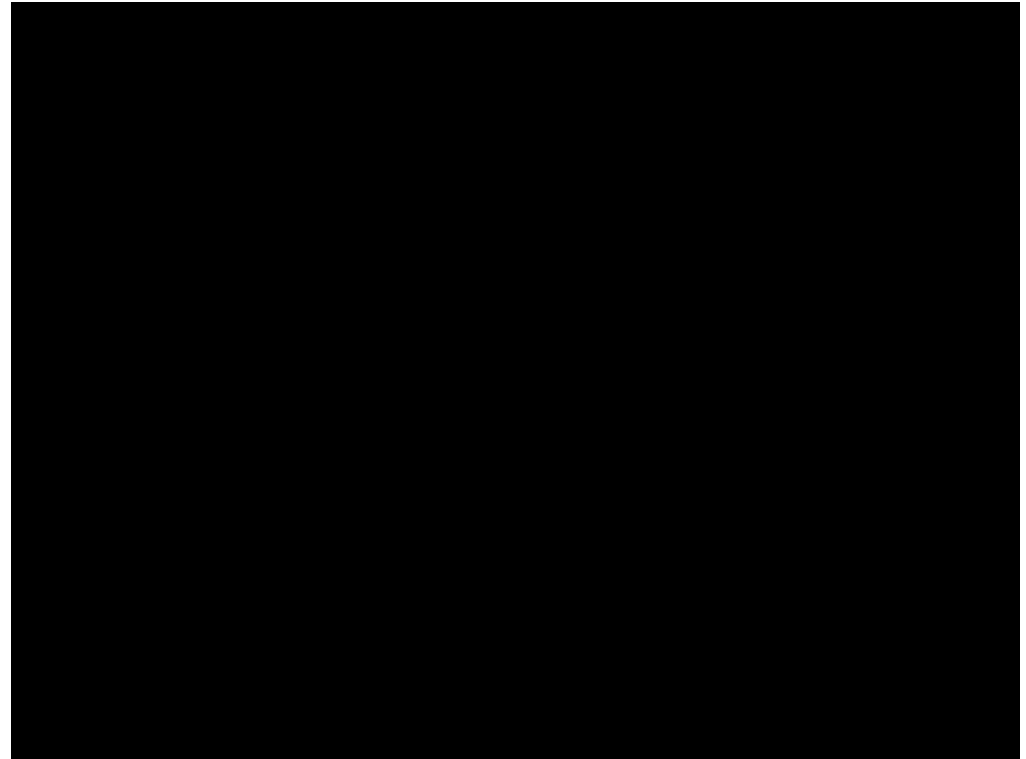
2D turbulence in Faraday waves: turbulent horizontal fluid motion

Faraday waves as a lattice of oscillons

Supercritical acceleration:
lattice of oscillons



Subcritical acceleration: individual oscillon

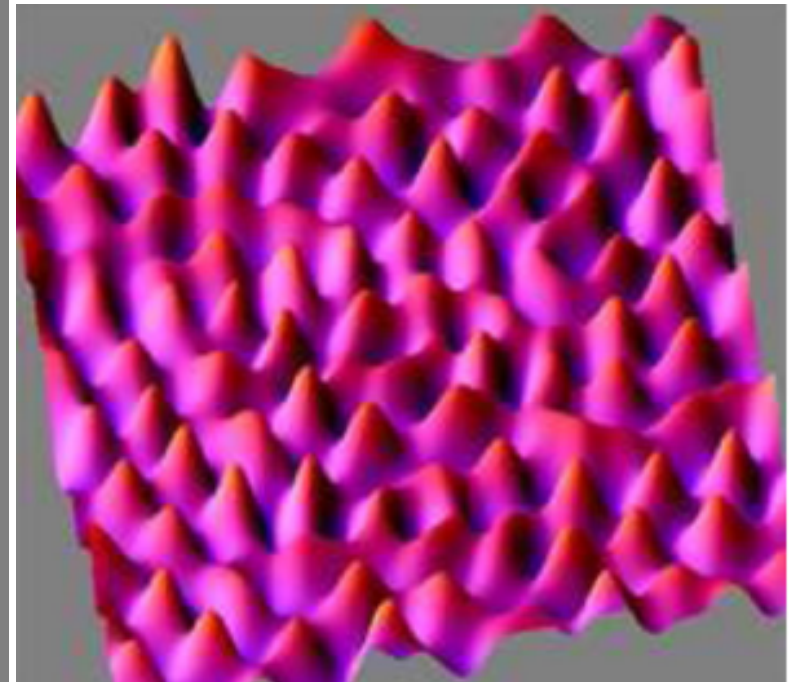
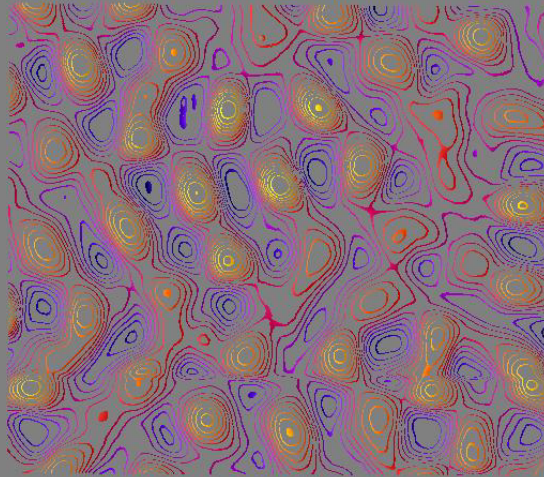


Glycerol-water solution, high viscosity (190 mPa.s), acceleration 3.1g

Shats, Xia, Punzmann, *Phys. Rev. Lett.* **108**, 034502 (2012)

In water lattices become disordered

Oscillon mobility



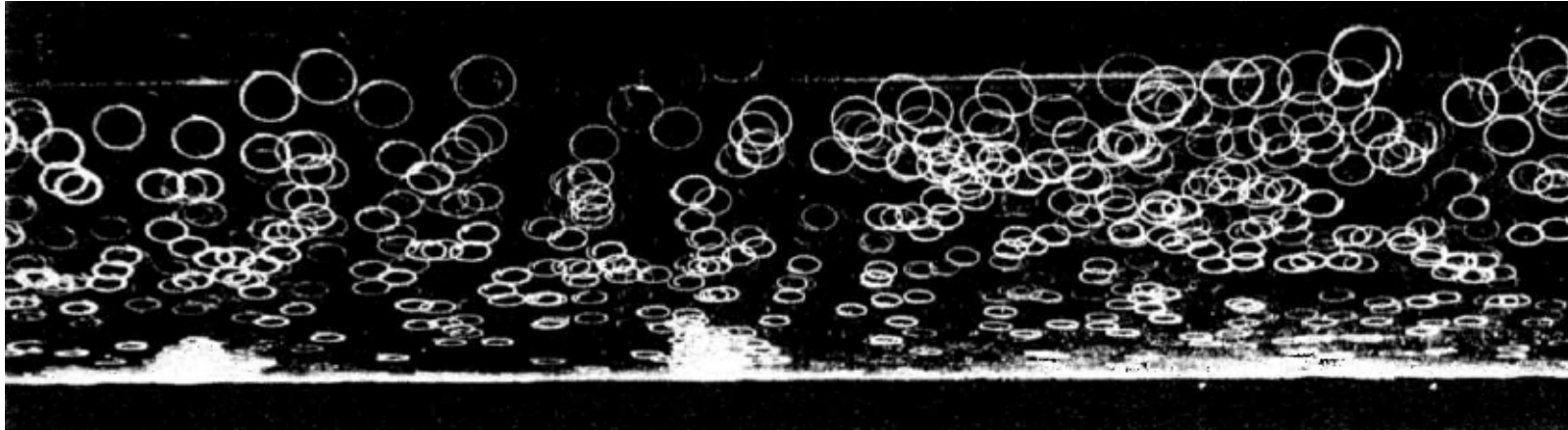
Shats M., Xia H., and Punzmann H.
Phys. Rev. Lett. 108, 034502 (2012)

Xia, Maimbourg, Punzmann, and Shats
Phys. Rev. Lett. 109, 114502 (2012)

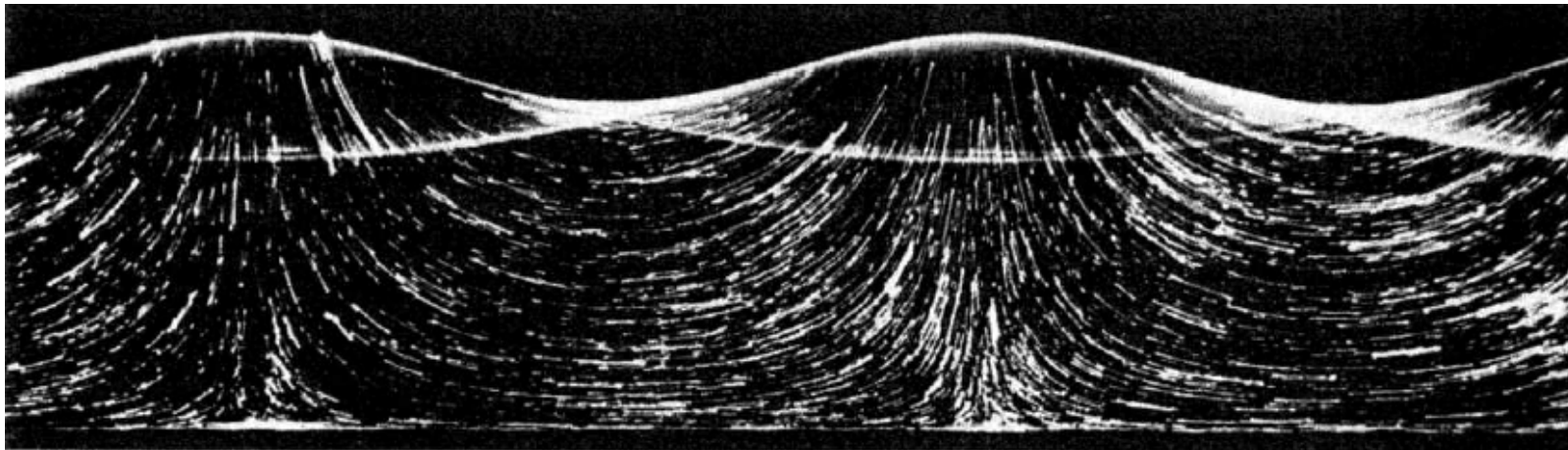
Particle trajectories in plane periodic 2D waves

Propagating wave

Long narrow wave flume

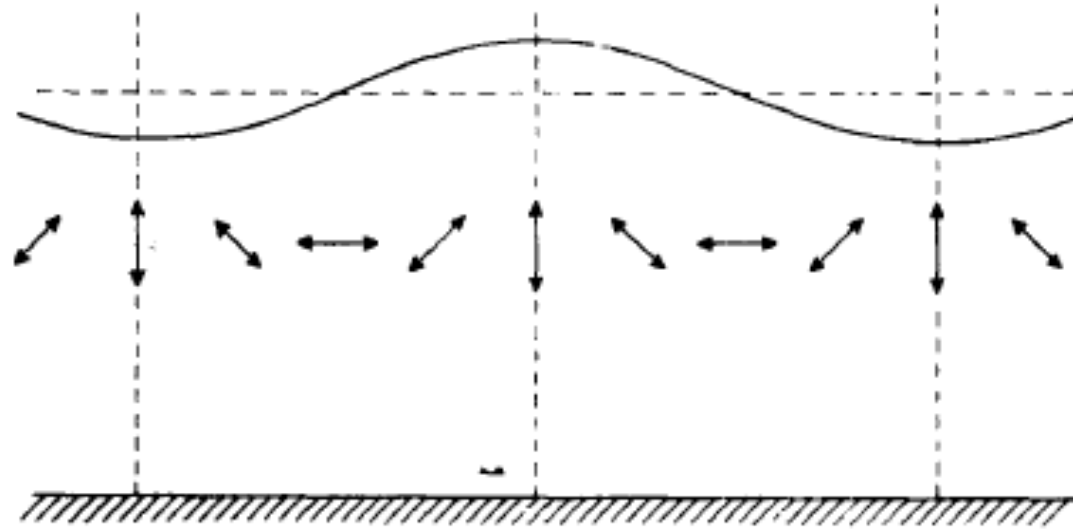
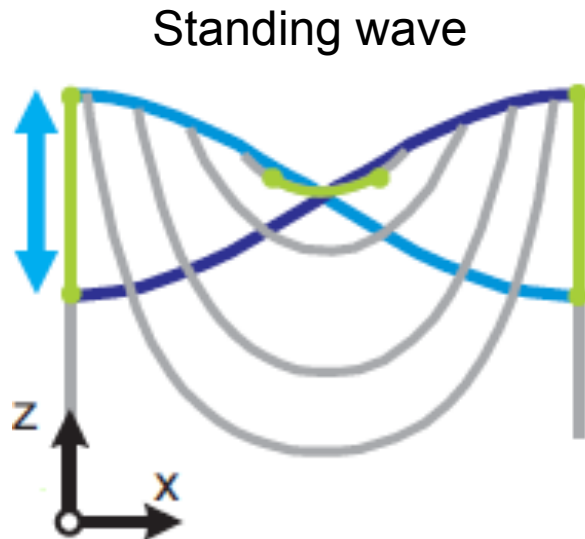


Standing wave



A.Wallet, and F. Ruellan, La Houille Blanche 5, 483-489 (1950).

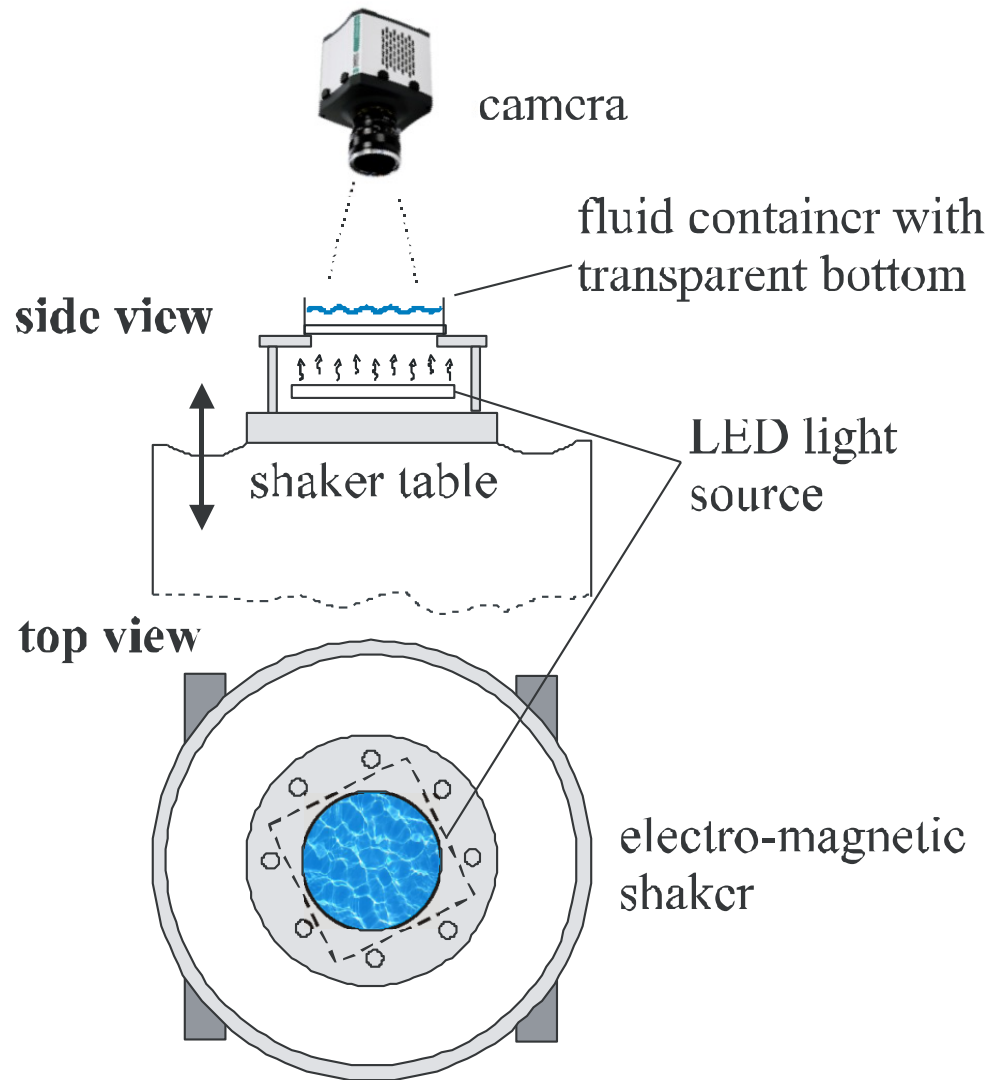
Particle trajectories in standing 2D waves



Longuet-Higgins, Stewart, Deep-Sea Research,
1964, Vol. II, pp. 529

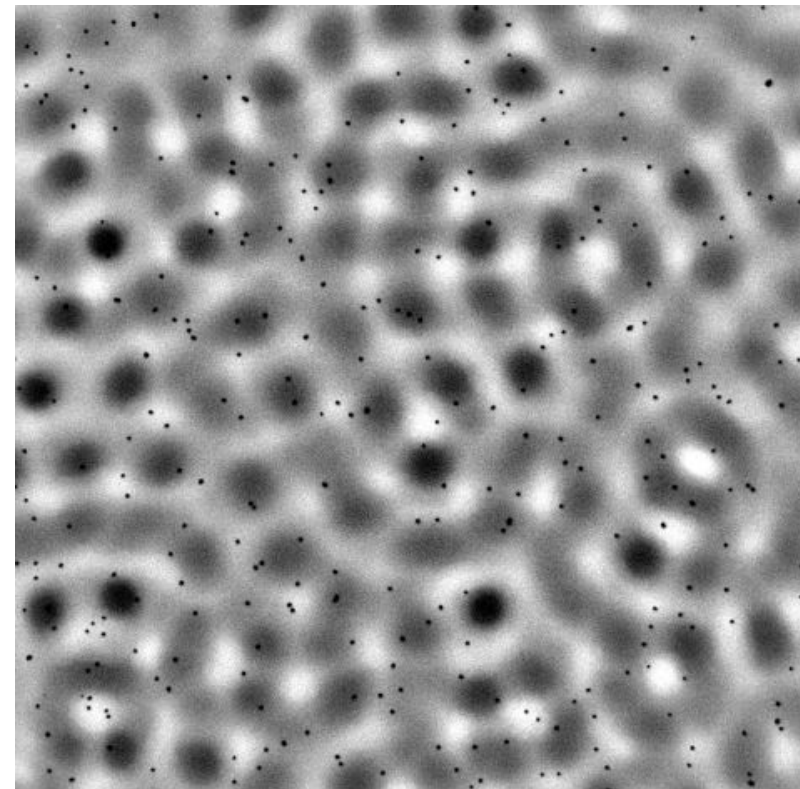
Particle trajectories correspond to vertical lines near the wave crest/trough,
while particles perform the pendulum motion near the wave nodes

Experimental setup to visualize 3D trajectories



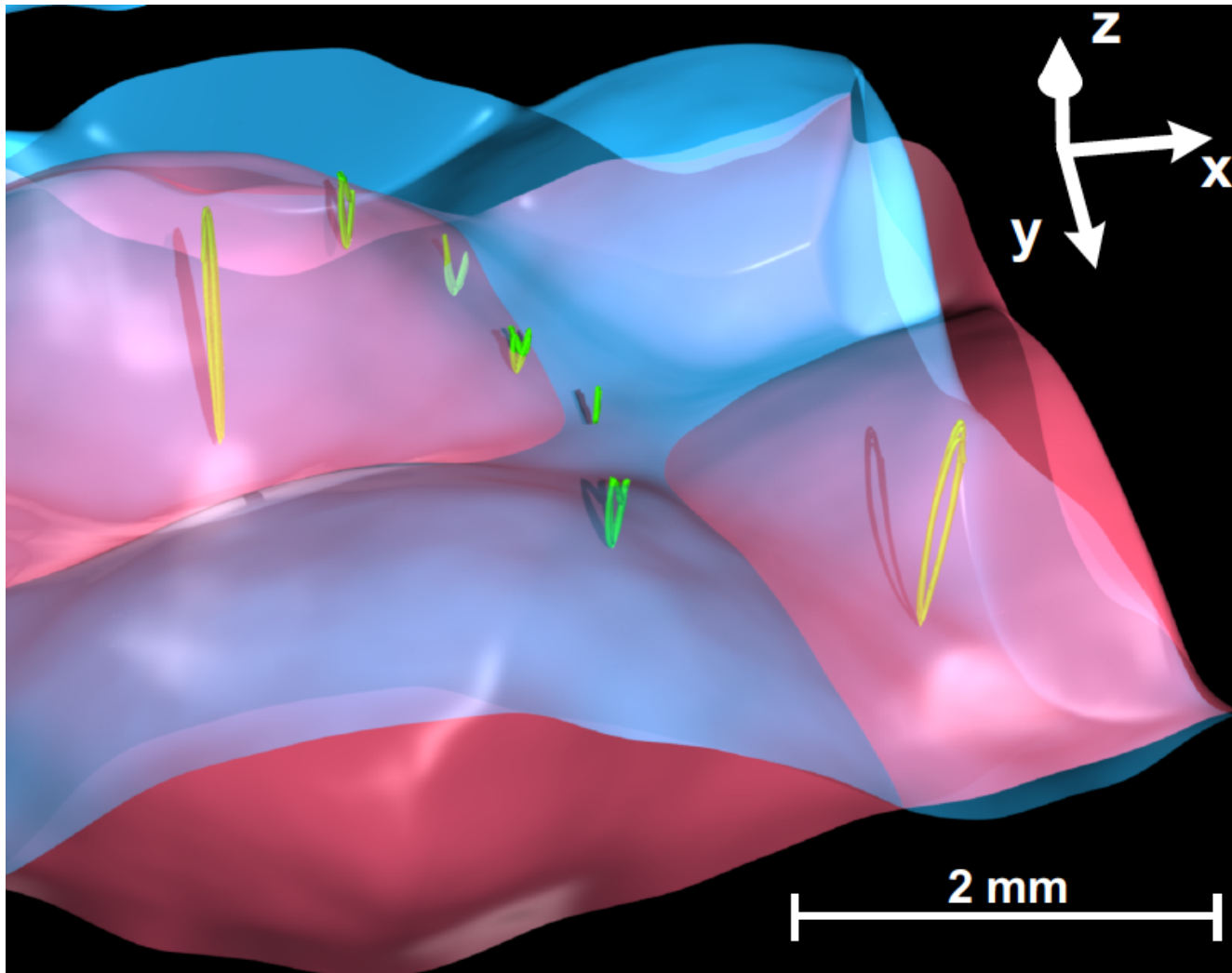
Diffusive light imaging

+ 2D PTV



Fluid particle orbits at high dissipation

solution of 73% glycerol + water



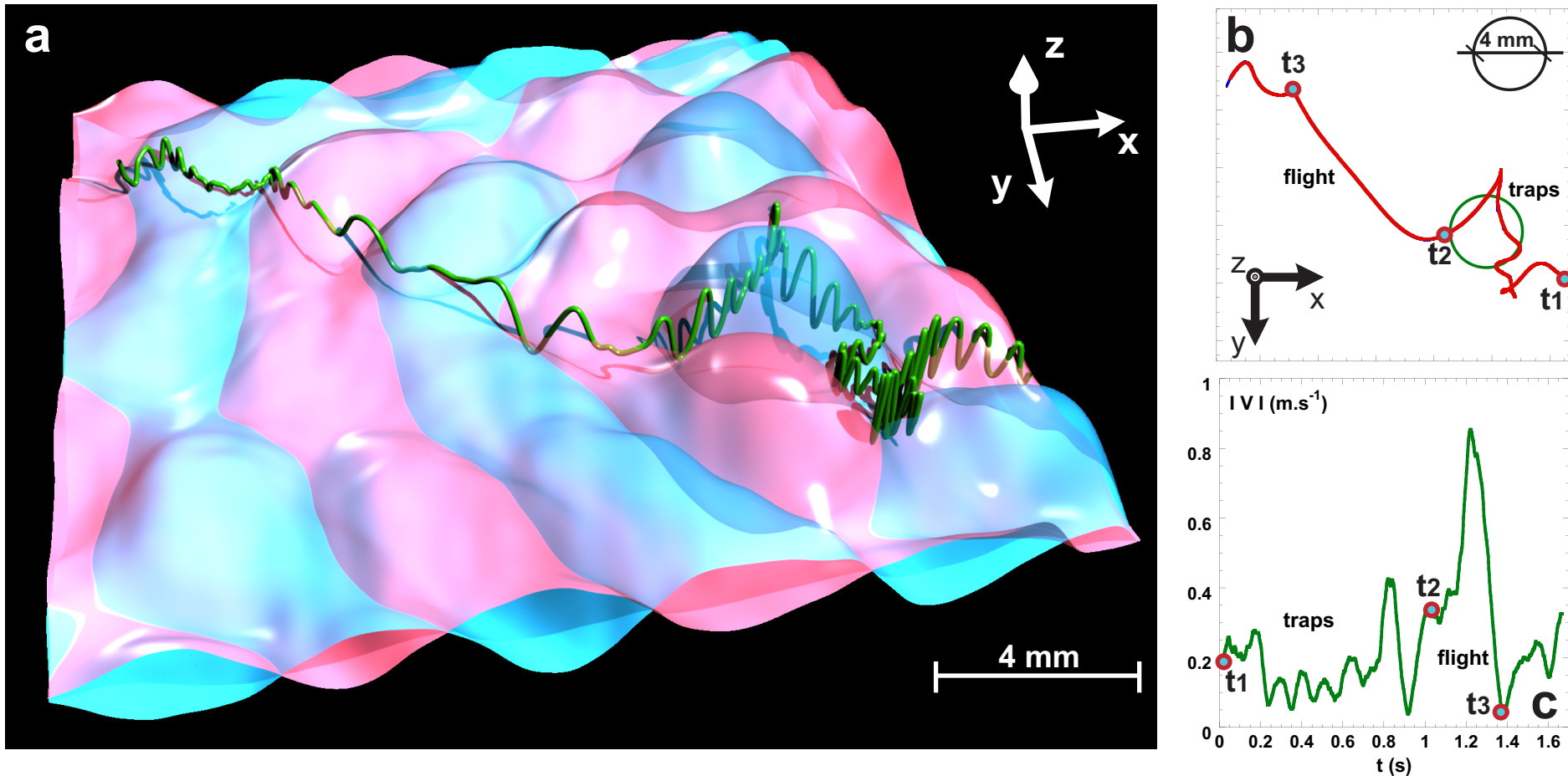
**Dissipation reduces
oscillon mobility,
ordered lattice is
formed**

Particle trajectories are followed for 8 Faraday periods in a FW crystal

Closed orbits:

- Almost vertical motion near troughs/crests;
- Pendulum motion near wave nodes

3D trajectories in Faraday waves in water



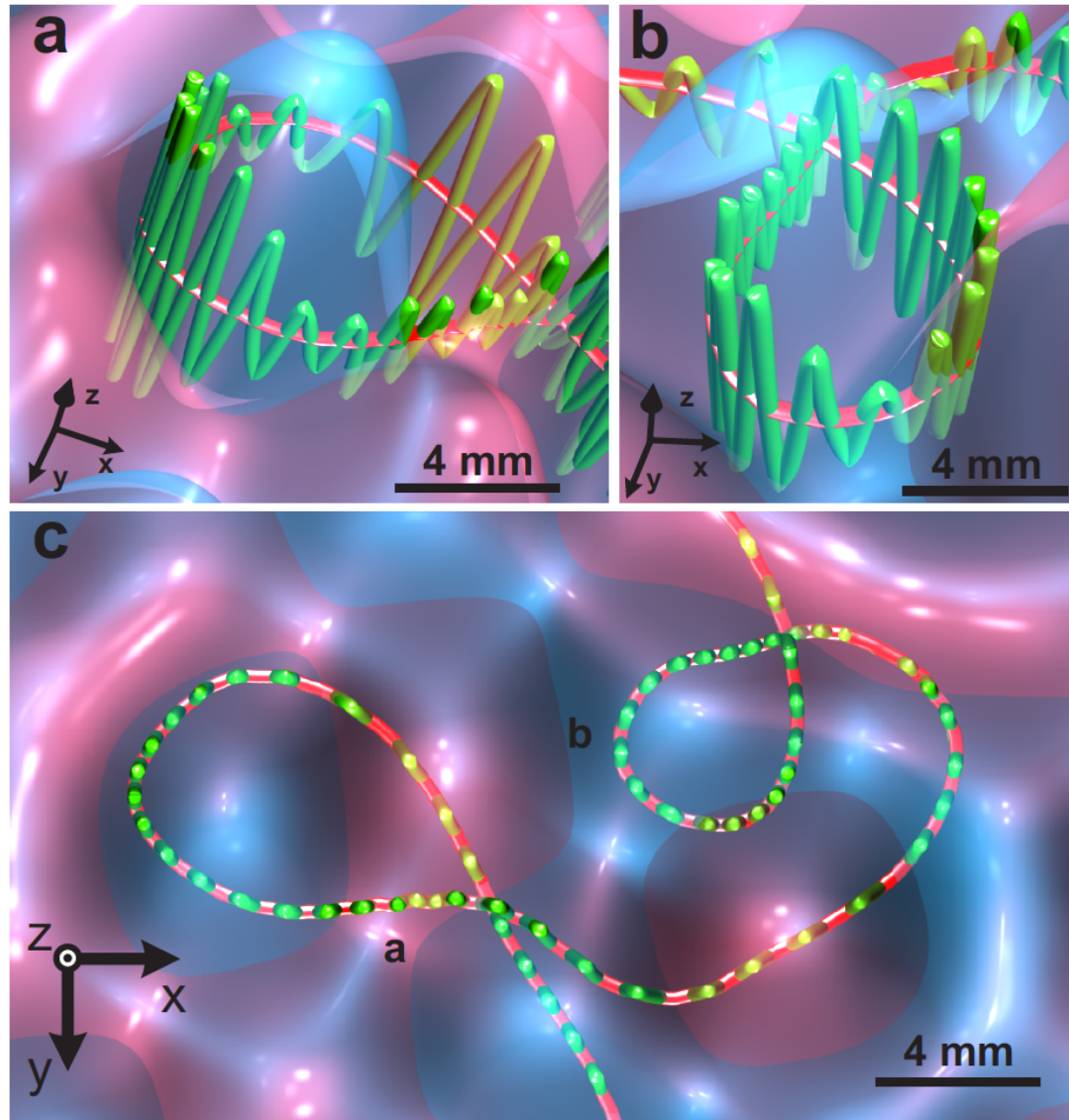
Particle trajectory followed for 1.6 s ($a = 1.6g$ $f_0 = 60\text{Hz}$)

Francois N., Xia H., Punzmann H., Ramsden S., and Shats M., *Phys. Rev. X* 4, 021021 (2014).

3D particle trajectories in 2D Faraday turbulence



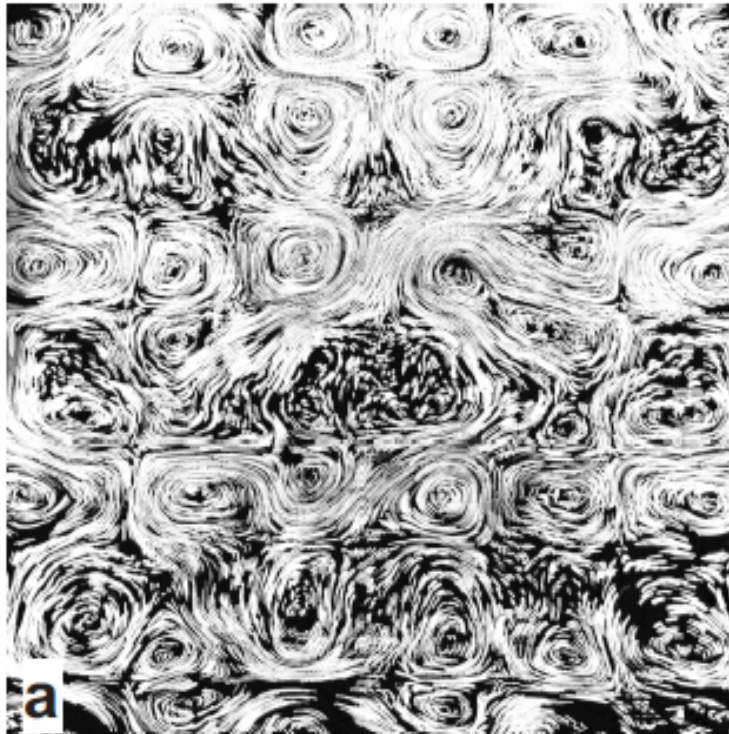
Particle trajectories are vertically polarized



Wave induced vorticity

Early stage of turbulence development

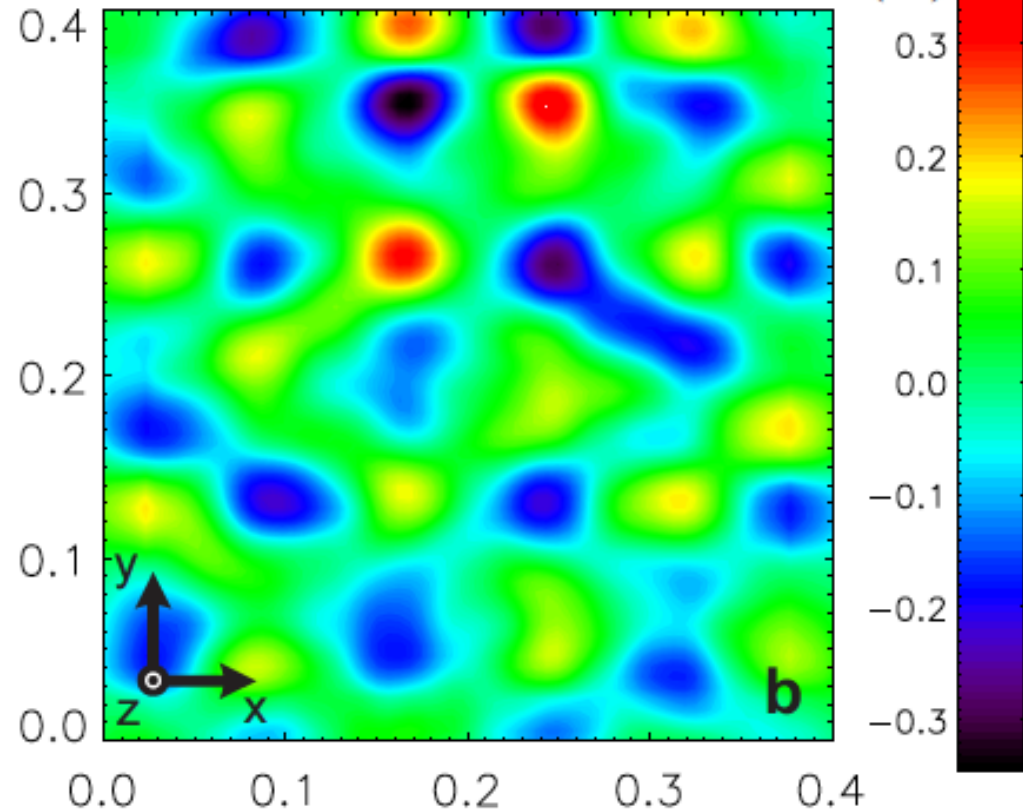
Particle trajectories



y (m)

Vorticity

Ω (s⁻¹)



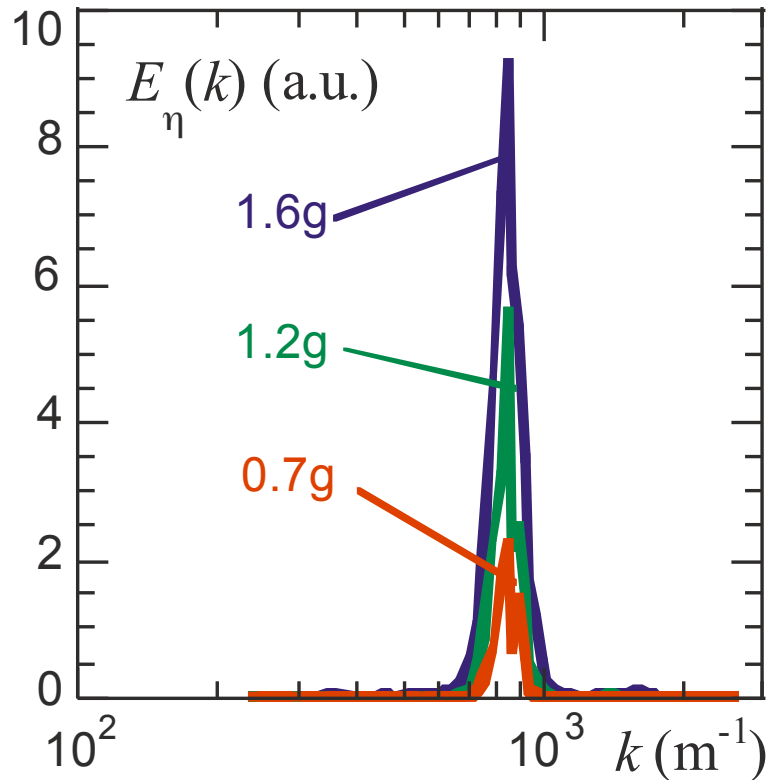
$$f_0 = 10 \text{ Hz and } a = 0.04g$$

Summary 1

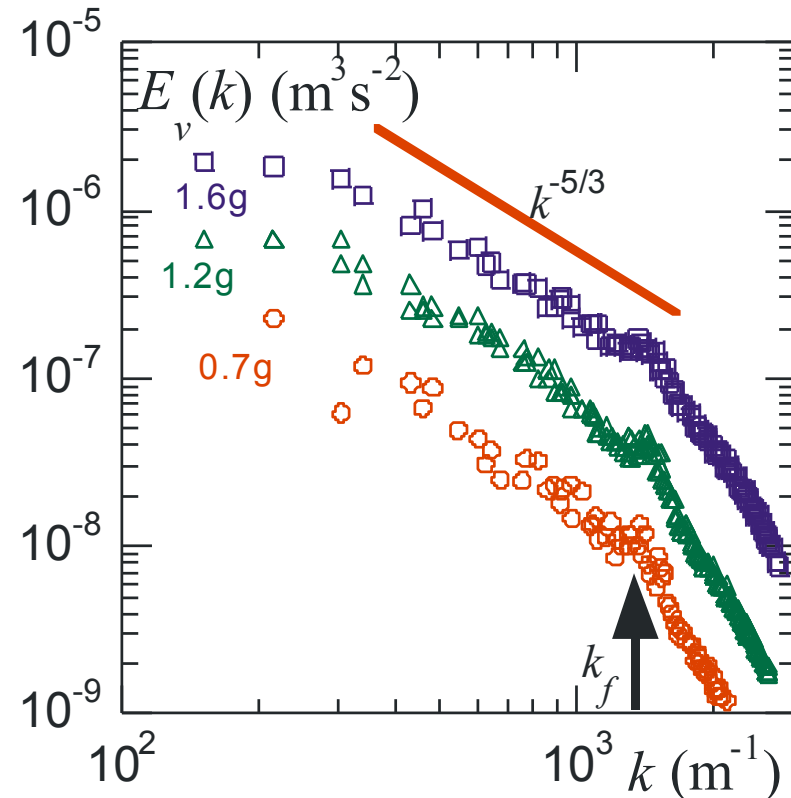
- **Faraday waves generate horizontal vortices on the water surface**
- **Those vortices interact inducing complex horizontal motion**

Wave spectra and horizontal kinetic energy spectra

Surface elevation spectra



Horizontal KE spectra



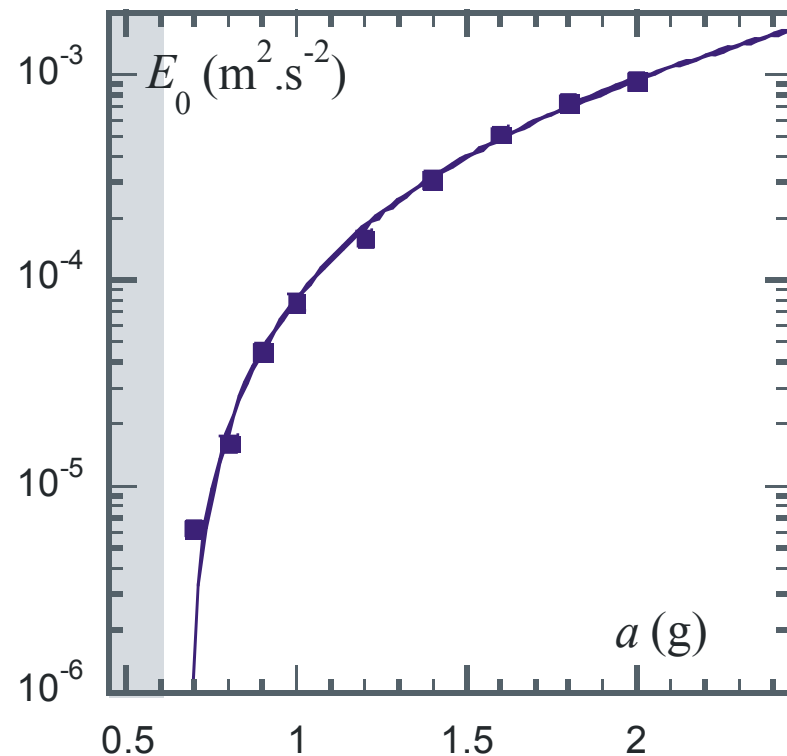
$$E(k) = C \varepsilon^{2/3} k^{-5/3}$$

A. von Kameke et al., *Phys. Rev. Lett.* **107**, 074502 (2011) – shallow water

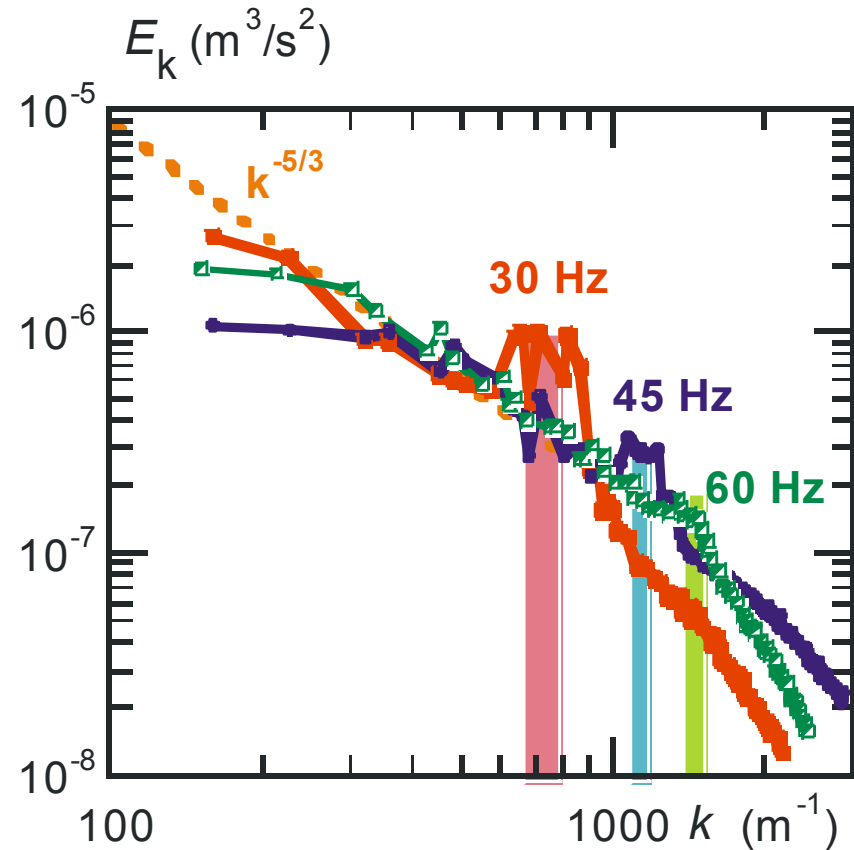
N. Francois, H. Xia, H. Punzmann, & M. Shats, *Phys. Rev. Lett.* **110**, 194501 (2013)

Turbulence control: acceleration and frequency

**Turbulence KE
vs vertical acceleration**



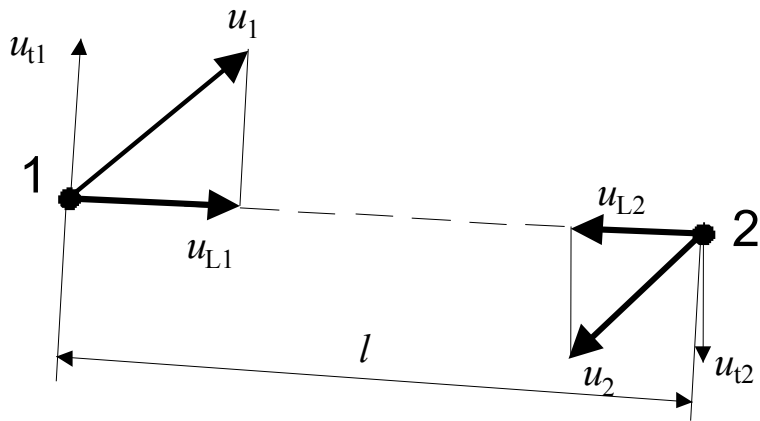
**Faraday wave frequency
controls turbulence forcing scale**



Inverse energy cascade in wave-driven turbulence

Third-order velocity structure function

$$S_{3L}(r) = \left\langle \left[u_{L1}(x+r) - u_{L2}(x) \right]^3 \right\rangle$$

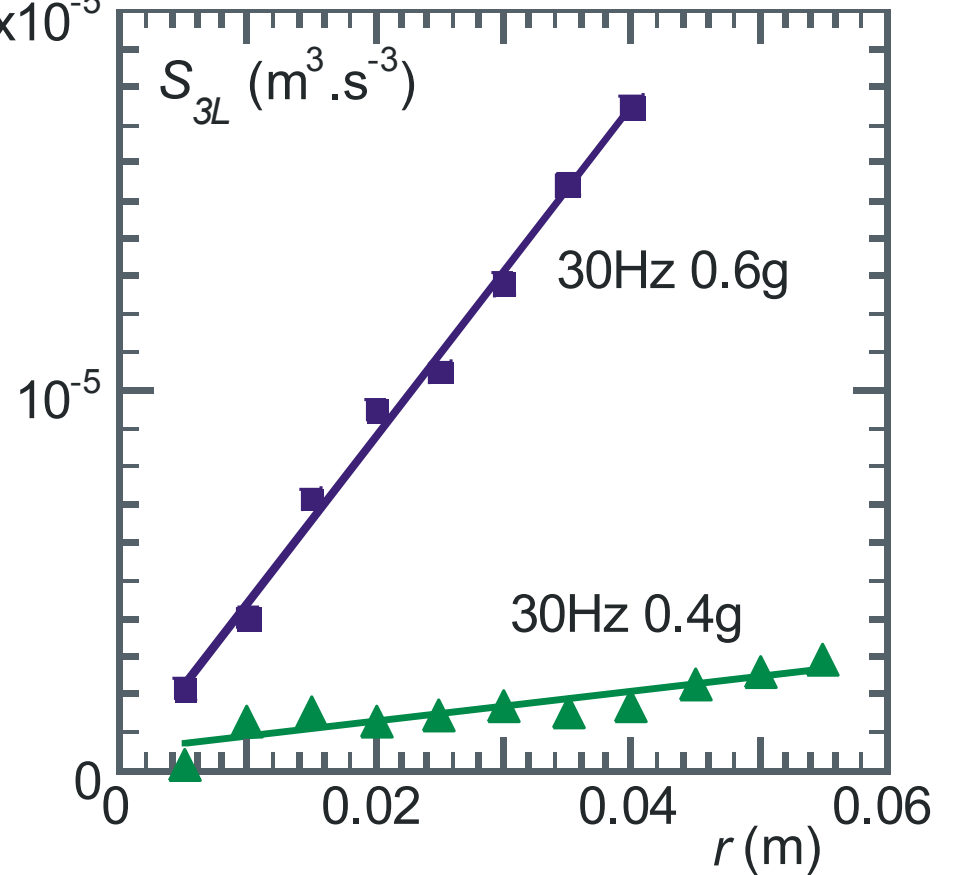


$$S_{3L}(l) = -\frac{3}{2} \epsilon r$$

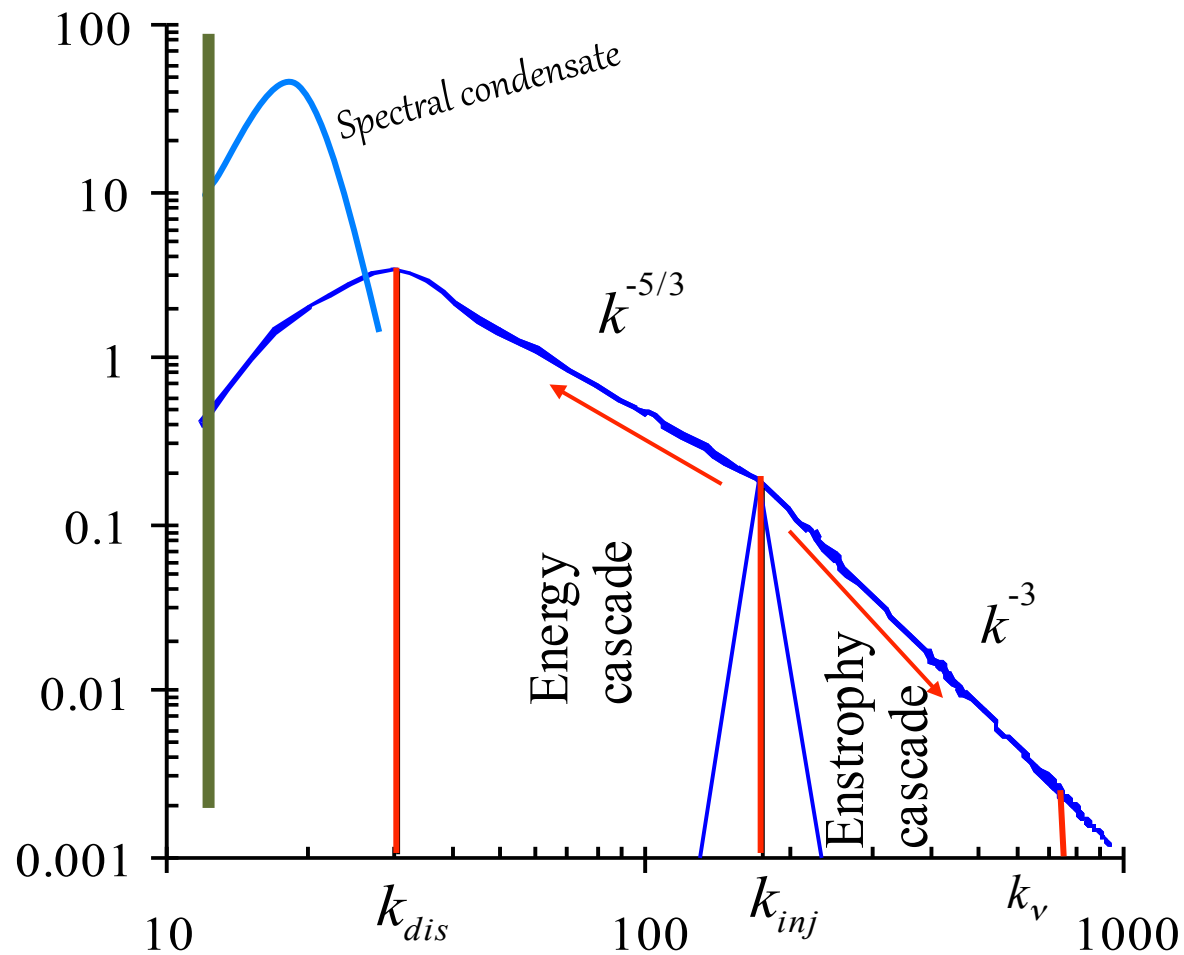
$$S_3 > 0 \quad \text{in 2D}$$

$$S_3 < 0 \quad \text{in 3D}$$

Faraday wave turbulence



Spectral condensation of 2D turbulence

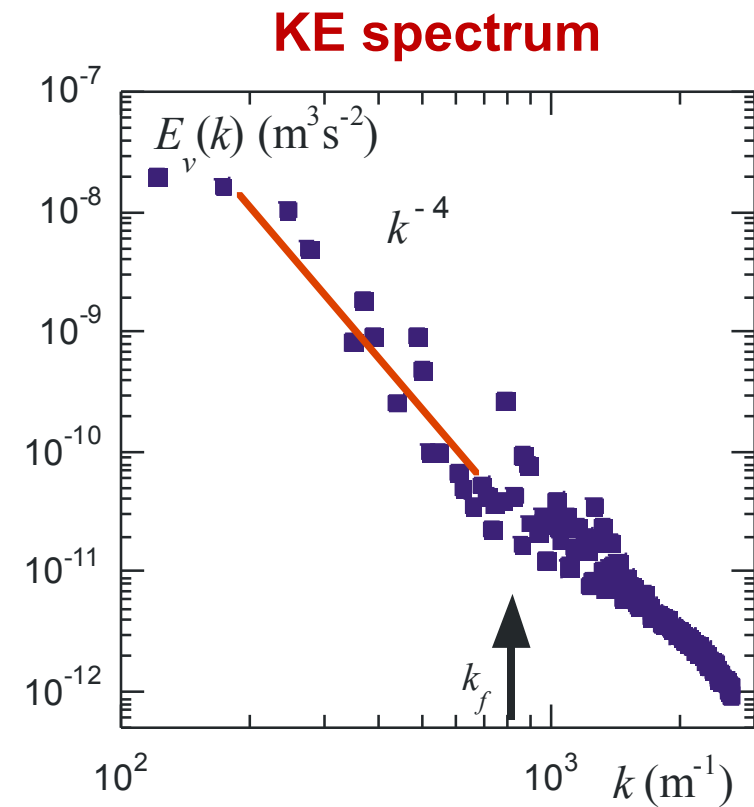
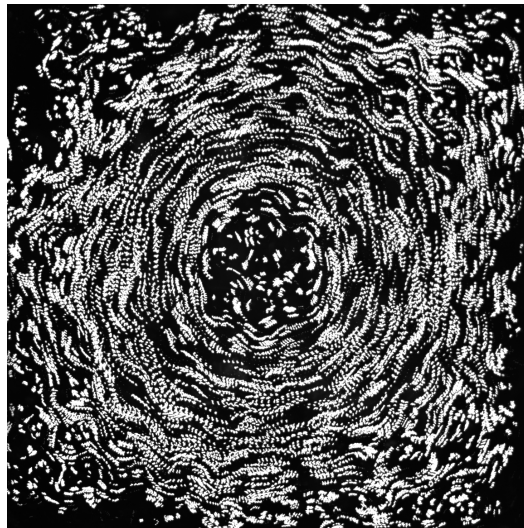


Kraichnan's inverse energy cascade (1967)

Spectral condensation in Faraday turbulence



Square container



Novel method of converting energy of the wave vertical energy into coherent horizontal motion

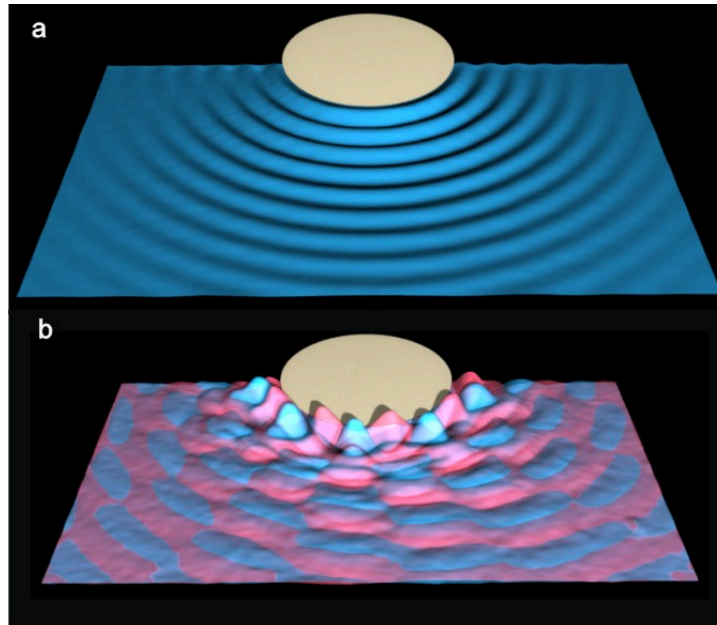
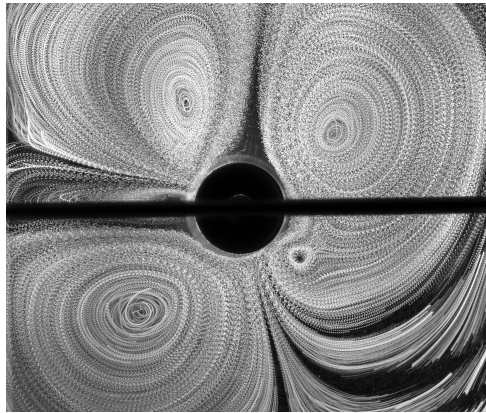
Summary 2

- **Faraday waves generate 2D turbulence on the water surface**
- **Wave-driven 2D turbulence can spectrally condense within a square boundary**

**Propagating waves also can generate horizontal vortices
on the water surface which drive surface flows**

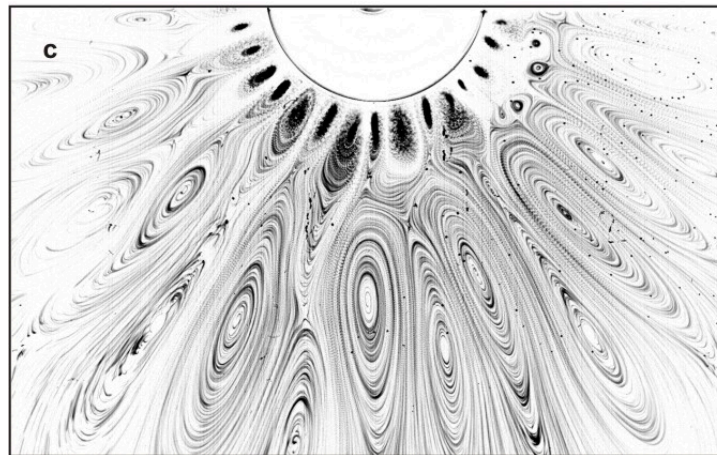
Punzmann, Francois, Xia, Falkovich & Shats, *Nature Physics* **10**, 658-663 (2014).

Waves and vortices by conical wavemaker



Below MI threshold

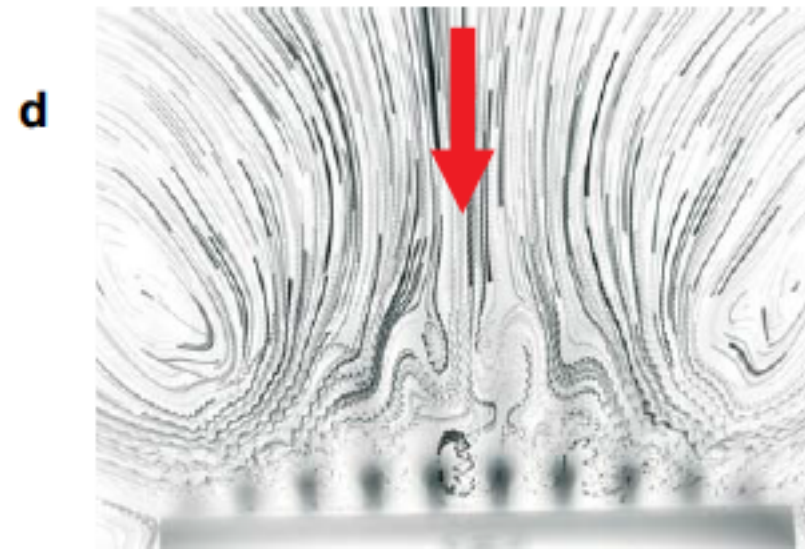
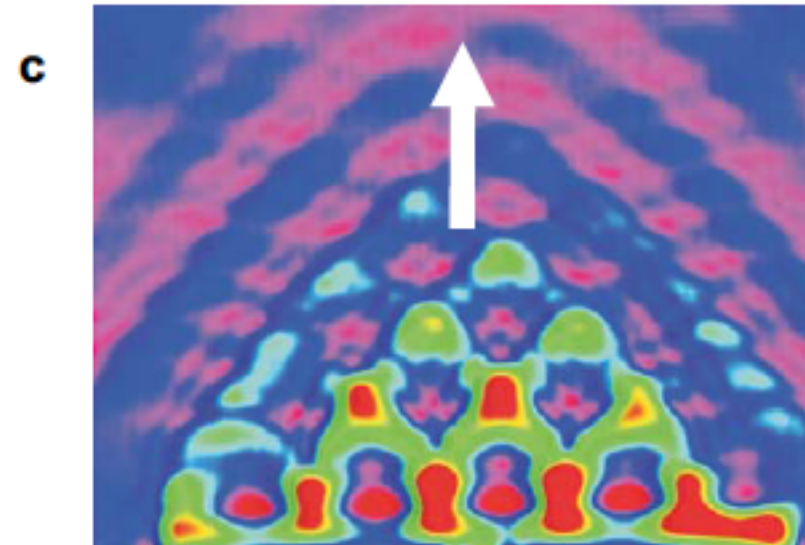
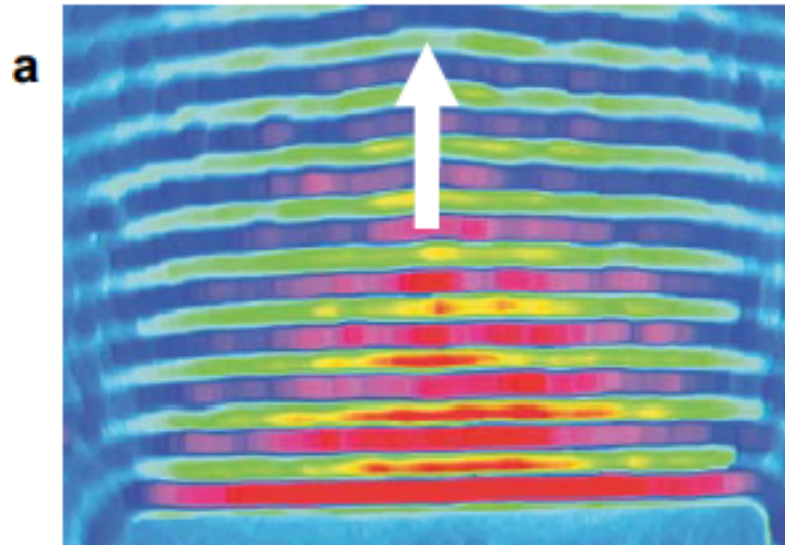
Above MI threshold



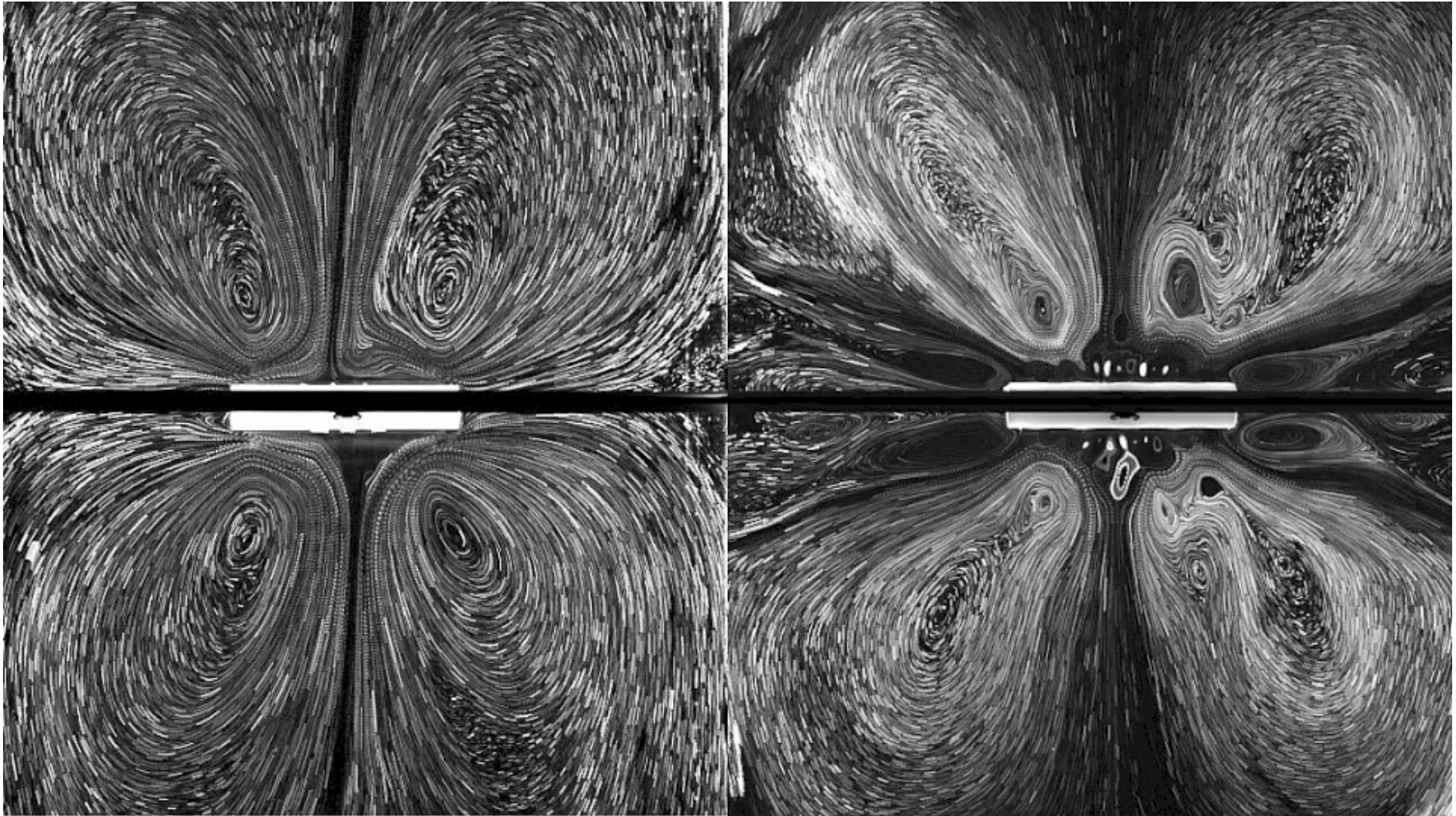
Surface flow

Water

Tractor beam by propagating waves



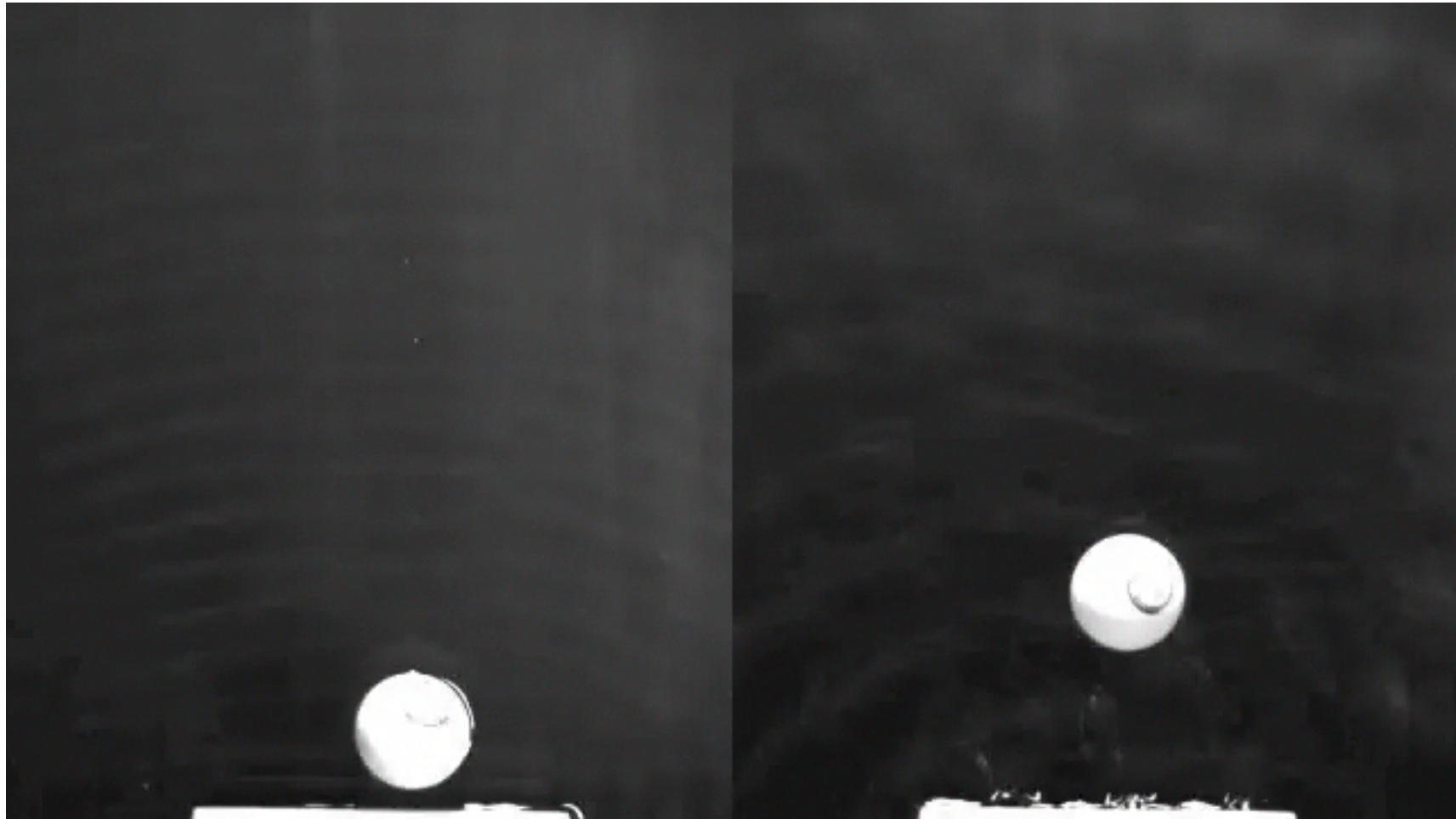
Water surface tractor beam



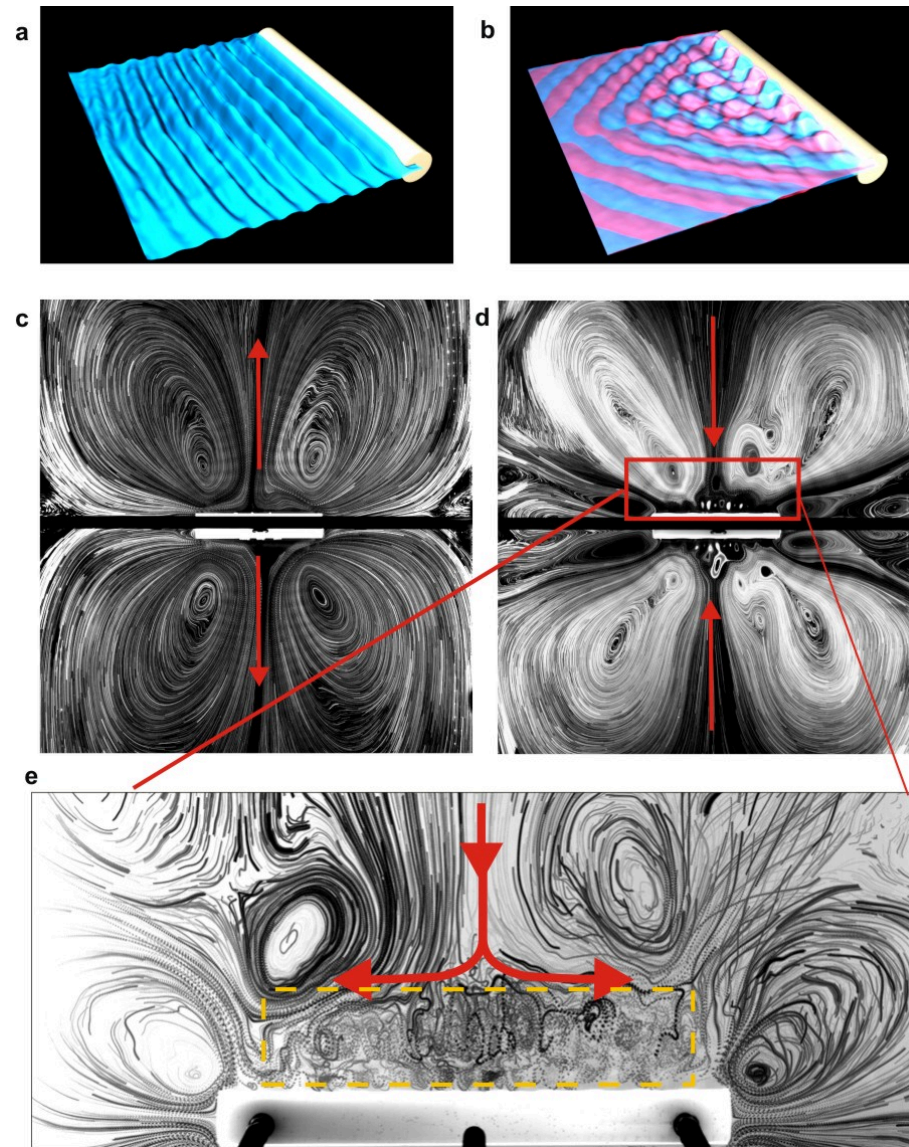
Object manipulation on the surface

Linear waves

Nonlinear waves



Stochastic pumping drives inward flow



**Stochastic
region**

Summary 3

- **Propagating waves also generate horizontal vortices on the water surface**
- **Wave-driven vortices can generate strong stochastic transport of fluid particles on the surface**