

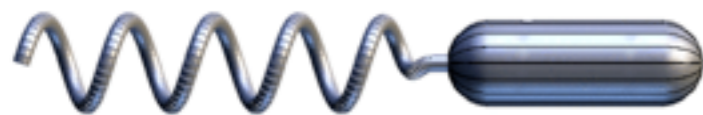


# **Swimming in complex environments: from biofilms to bacteria powered micro-devices**

**ROBERTO DI LEONARDO**

Dip. Fisica, Sapienza Università di Roma, Italy  
CNR-NANOTEC Soft and Living Matter Laboratory  
School for Advanced Studies Sapienza

## A SELF-PROPELLED MICRO-MACHINE



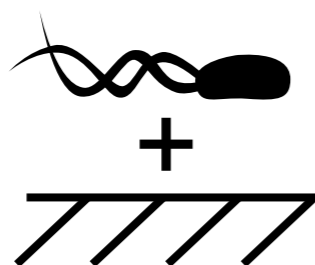
## TUESDAY

### Microhydrodynamics

#### a) SELF PROPELLING BACTERIA



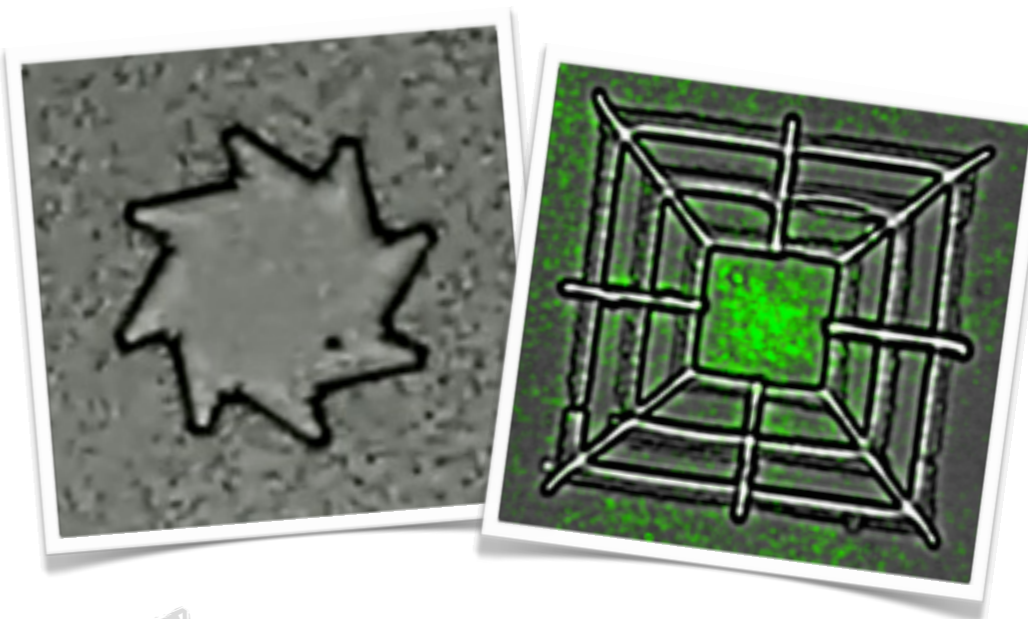
#### b) CONFINED SWIMMING



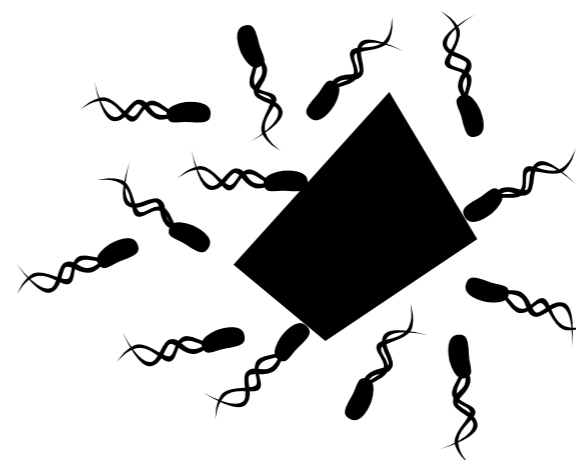
## TODAY

### Statistical Mechanics

#### d) BACTERIA POWERED MICRODEVICES



#### c) STOCHASTIC DYNAMICS IN ACTIVE BATHS



STOCHASTIC DYNAMICS IN ACTIVE BATHS I

targeted delivery of colloidal cargos

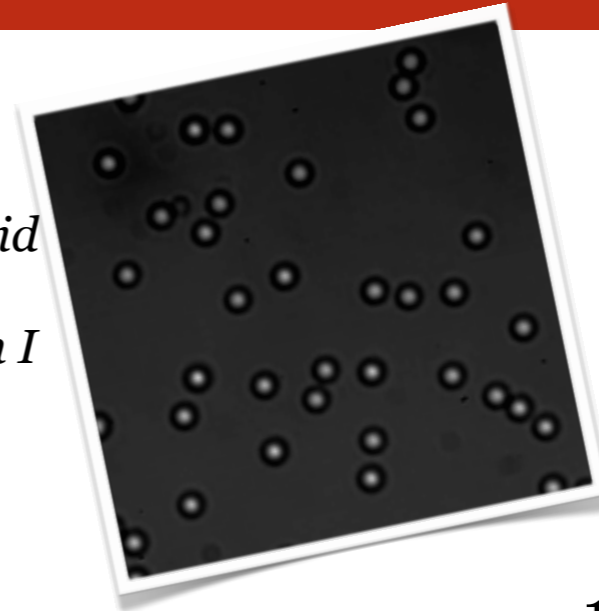
# Brownian motion: thermal motion at equilibrium



1827

*“Extremely minute particles of solid matter, when suspended in pure water ... exhibit motions for which I am unable to account.”*

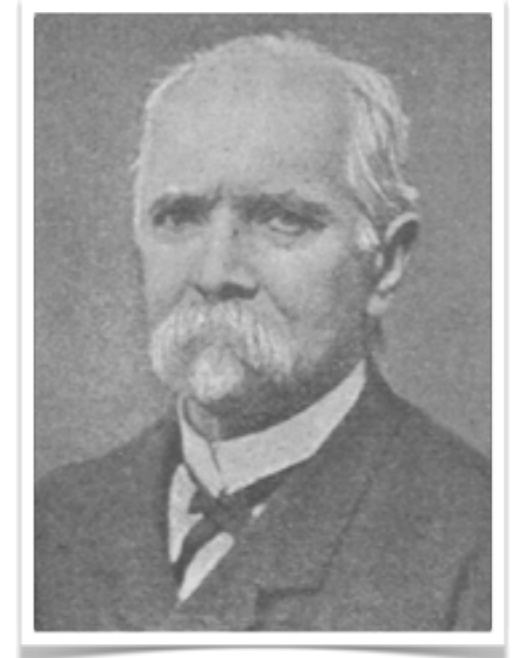
**ROBERT BROWN**



1867

*“Brownian motion [...] provides us with one of the most beautiful and direct experimental demonstrations of the fundamental principles of the mechanical theory of heat, making manifest the assiduous vibrational state that must exist both in liquids and solids”*

**GIOVANNI CANTONI**



1905

**A. EINSTEIN**

**W. SUTHERLAND**



MEAN-SQUARE  
DISPLACEMENT

$$\langle \Delta r^2(t) \rangle = 6Dt$$

DIFFUSION  
COEFFICIENT

$$D = k_B T / \gamma$$

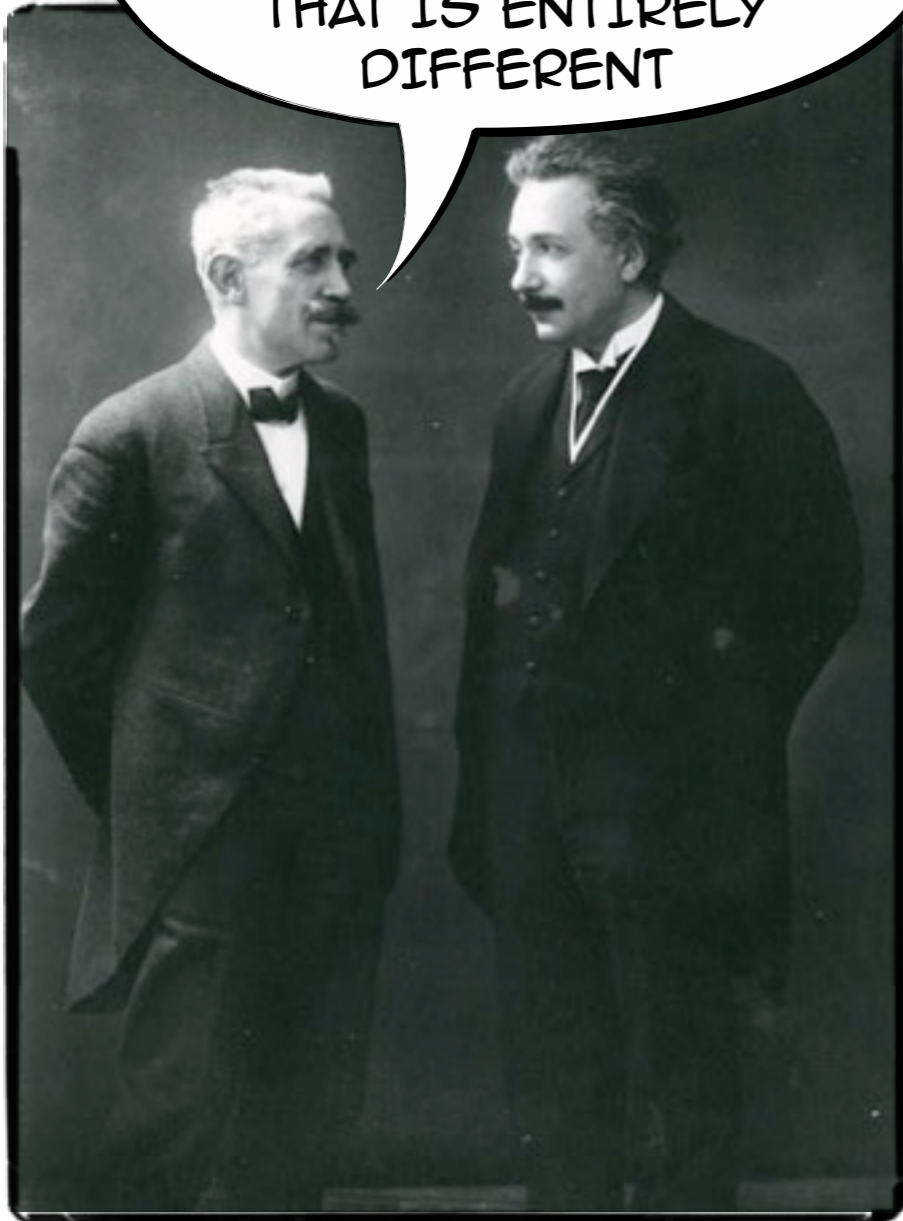
STOKES DRAG

$$\gamma = 6\pi\mu a$$

# Langevin equation

1908 **PAUL LANGEVIN:**

IT IS EASY TO GIVE A DEMONSTRATION THAT IS INFINITELY MORE SIMPLE BY MEANS OF A METHOD THAT IS ENTIRELY DIFFERENT



**LANGEVIN EQUATION**

$$m\ddot{x} \sim 0 = \underbrace{f(x)}_{\text{EXTERNAL}} - \underbrace{\gamma\dot{x}(t)}_{\text{FRICTION}} + \underbrace{\eta(t)}_{\text{RANDOM FORCE}}$$

INTERACTION WITH SOLVENT

**UNBIASED**  $\langle \eta(t) \rangle = 0$

**WHITE NOISE**  $\langle \eta(t)\eta(t') \rangle = k_B T \underbrace{2\gamma\delta(t-t')}_{\text{FLUCTUATION}}$

**FRICTION**  $\gamma\dot{x}(t) = \int_0^t \underbrace{2\gamma\delta(t-t')}_{\text{DISSIPATION}} \dot{x}(t') dt'$

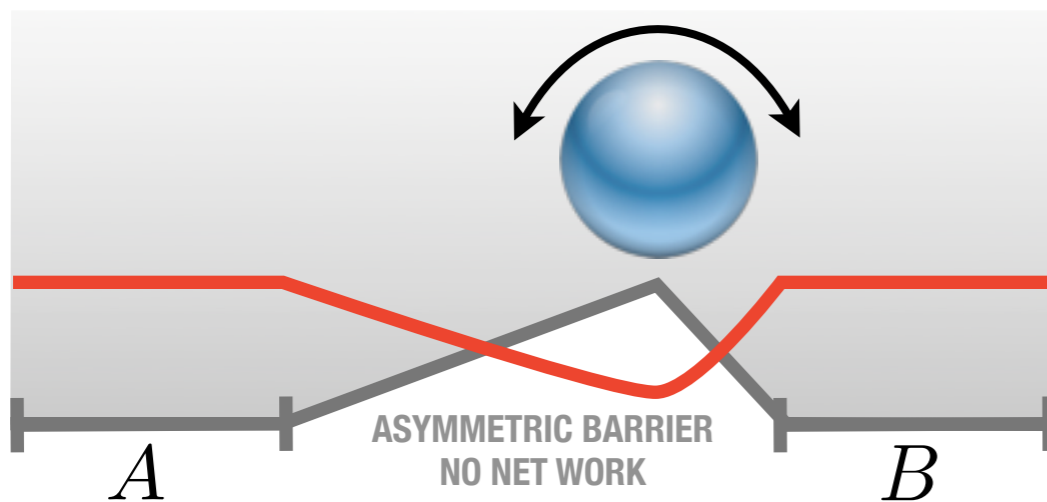
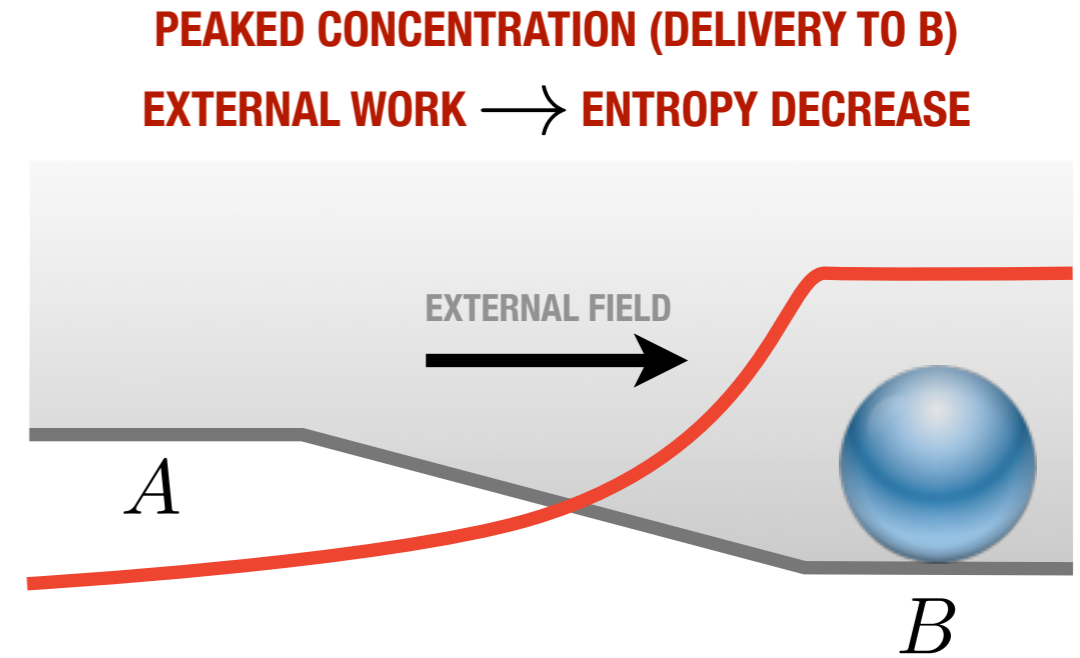
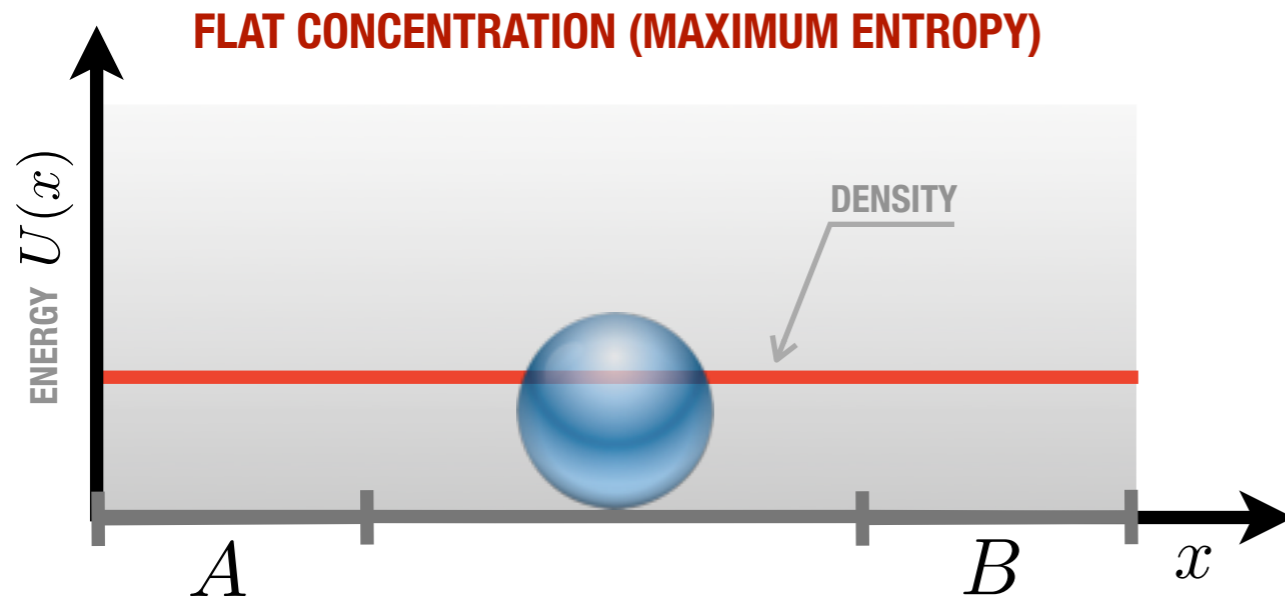
⇓

$$\frac{\rho_B}{\rho_A} = \exp \left[ \int_A^B \frac{f(x)}{k_B T} dx \right]$$

≡

**BOLTZMANN DISTRIBUTION**  $\exp \left[ -\frac{U_B - U_A}{k_B T} \right]$

# Colloidal delivery at equilibrium

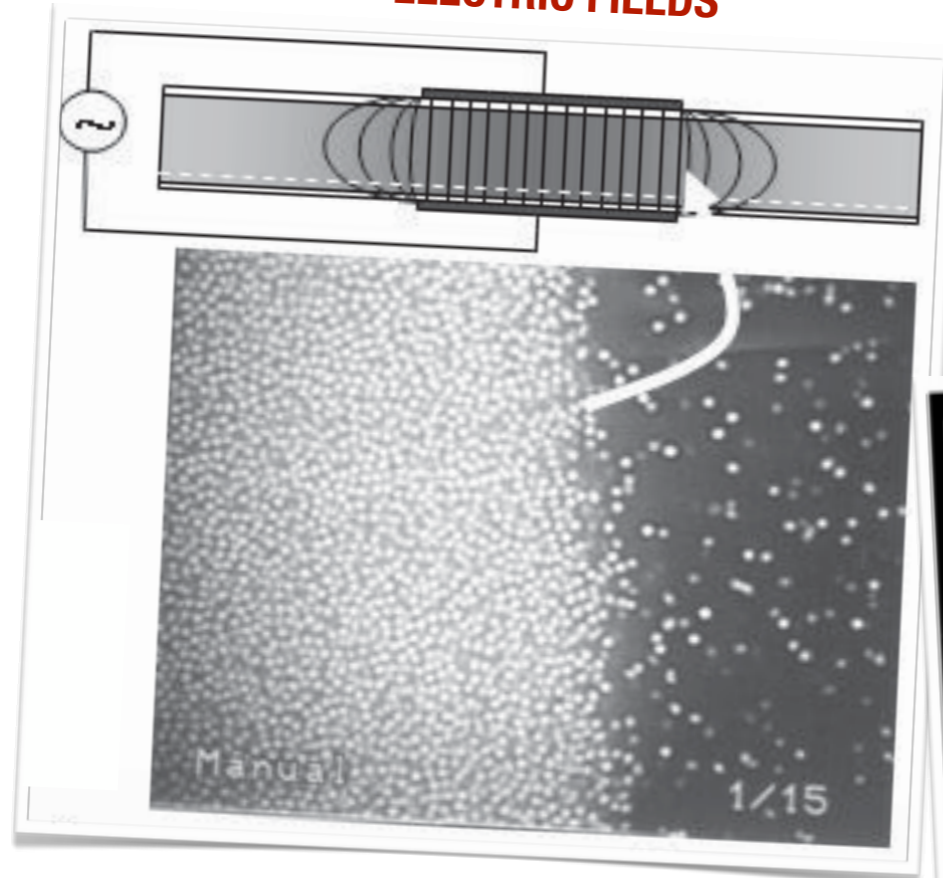


$$\frac{\rho_B}{\rho_A} = \exp \left[ \int_A^B \frac{f(x)}{k_B T} dx \right]$$

**BOLTZMANN DISTRIBUTION**  $\exp \left[ -\frac{U_B - U_A}{k_B T} \right]$

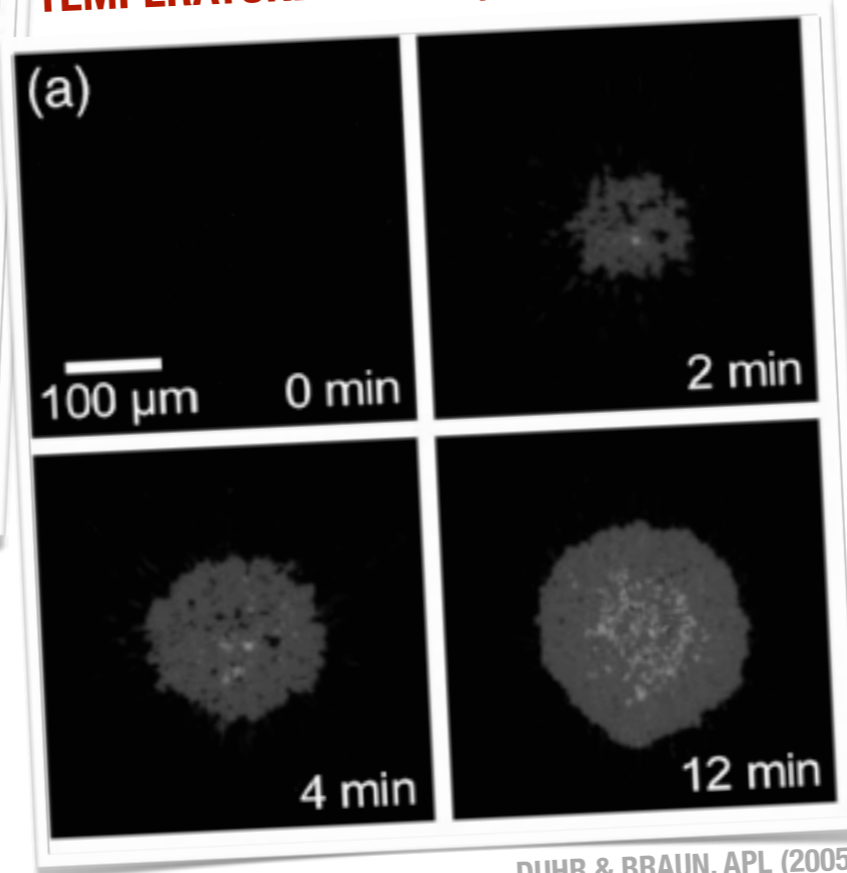
# Transport with external fields

## ELECTRIC FIELDS



SULLIVAN et al. PRL (2006)

## TEMPERATURE FIELDS (LASER HEATING)



DUHR & BRAUN, APL (2005)

MAGNETIC, FLOW ...

# Optical micromanipulation: Holographic Tweezers

GRIER, NATURE (2003)

PADGETT & DI LEONARDO, Lab Chip (2011)

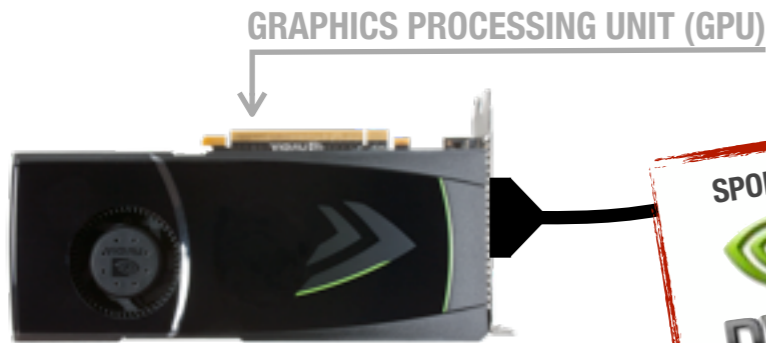
SPATIAL LIGHT MODULATOR

MICROSCOPE OBJECTIVE



## LIQUID CRYSTALS SLM

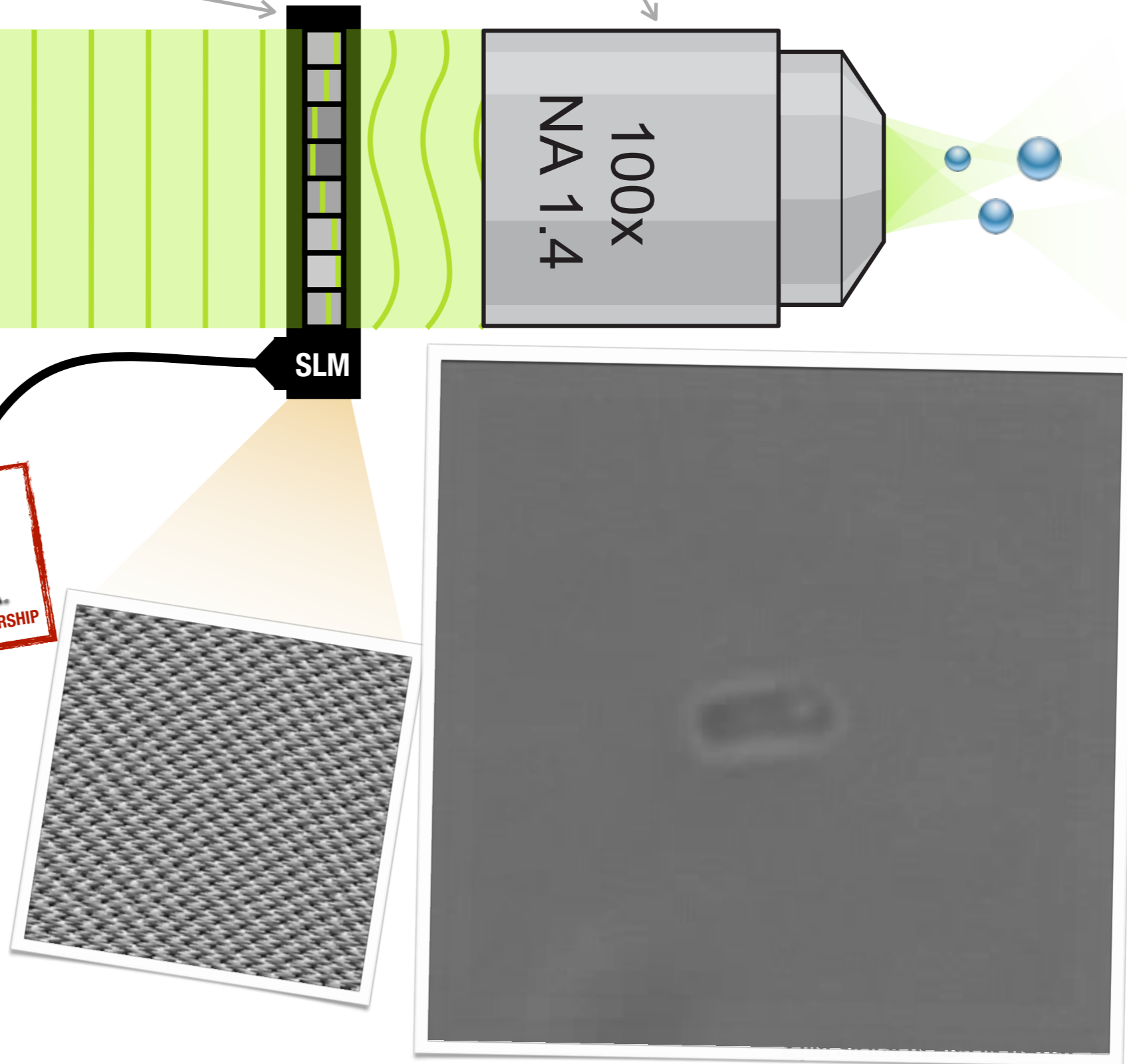
8 bit,  $0-2\pi$  phase modulation  
1 Megapixel resolution



GRAPHICS PROCESSING UNIT (GPU)

## DIGITAL PARALLEL HOLOGRAPHY

Highly optimized holograms in real time  
DI LEONARDO et al., Opt. Express (2006)  
BIANCHI & DI LEONARDO Comp. Phys. Comm. (2010)

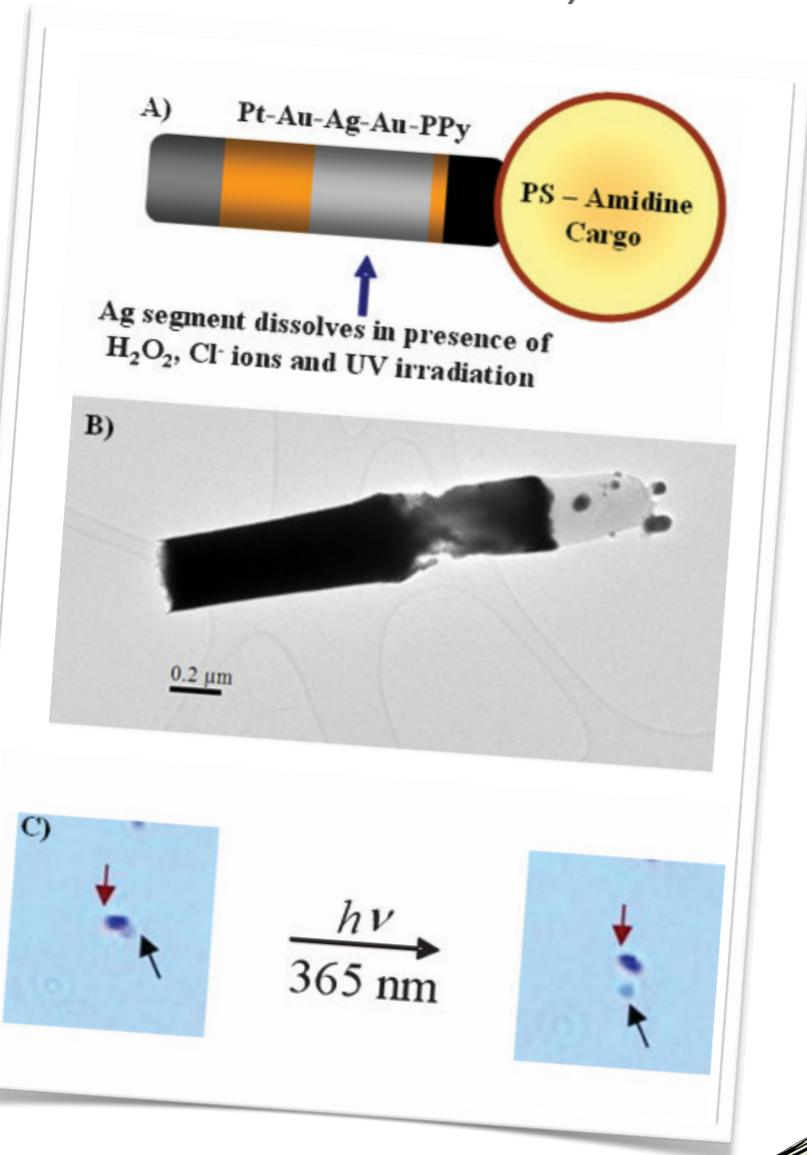




# Using active particles as micro-oxen

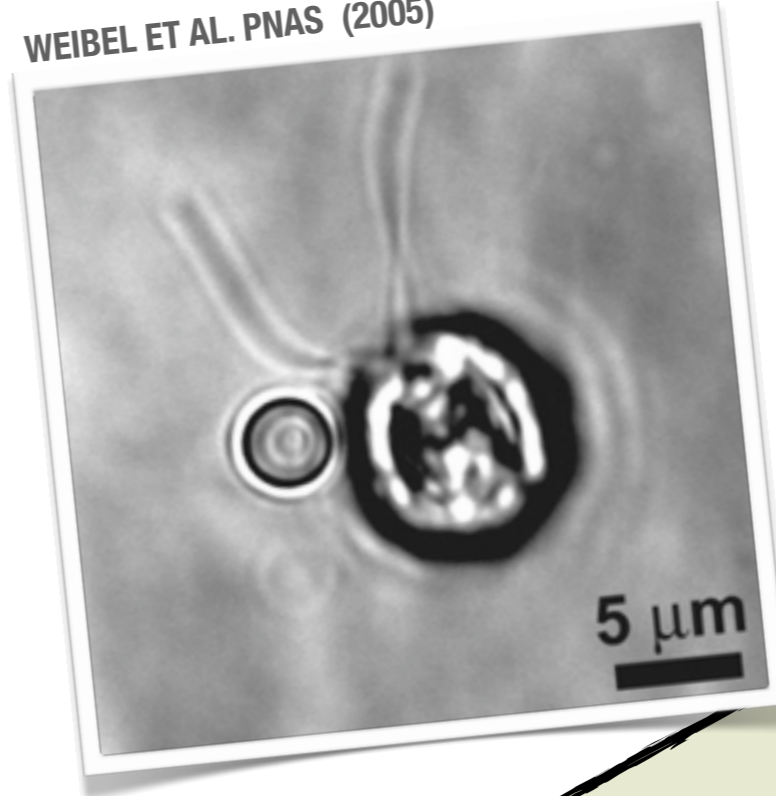
## SYNTHETIC SWIMMERS CATALYTIC Pt-Au NANOMOTOR

SUNDARARAJAN et al. SMALL (2010)



## SWIMMING CELLS *C. reinhardtii*

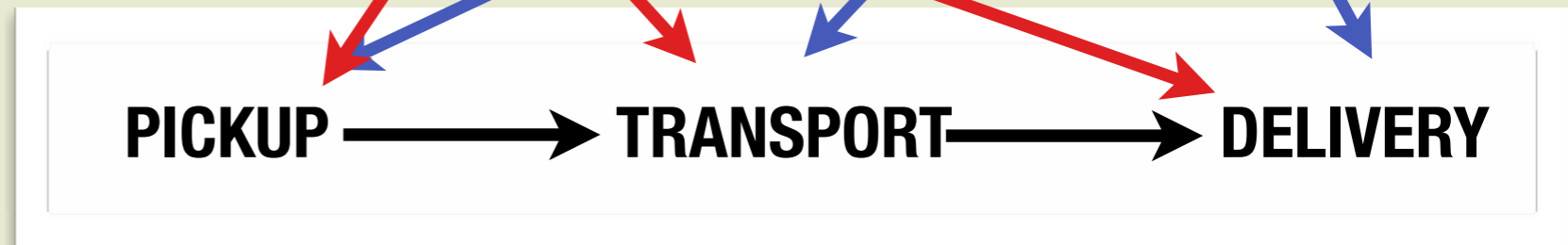
WEIBEL ET AL. PNAS (2005)



EXTERNAL FIELDS

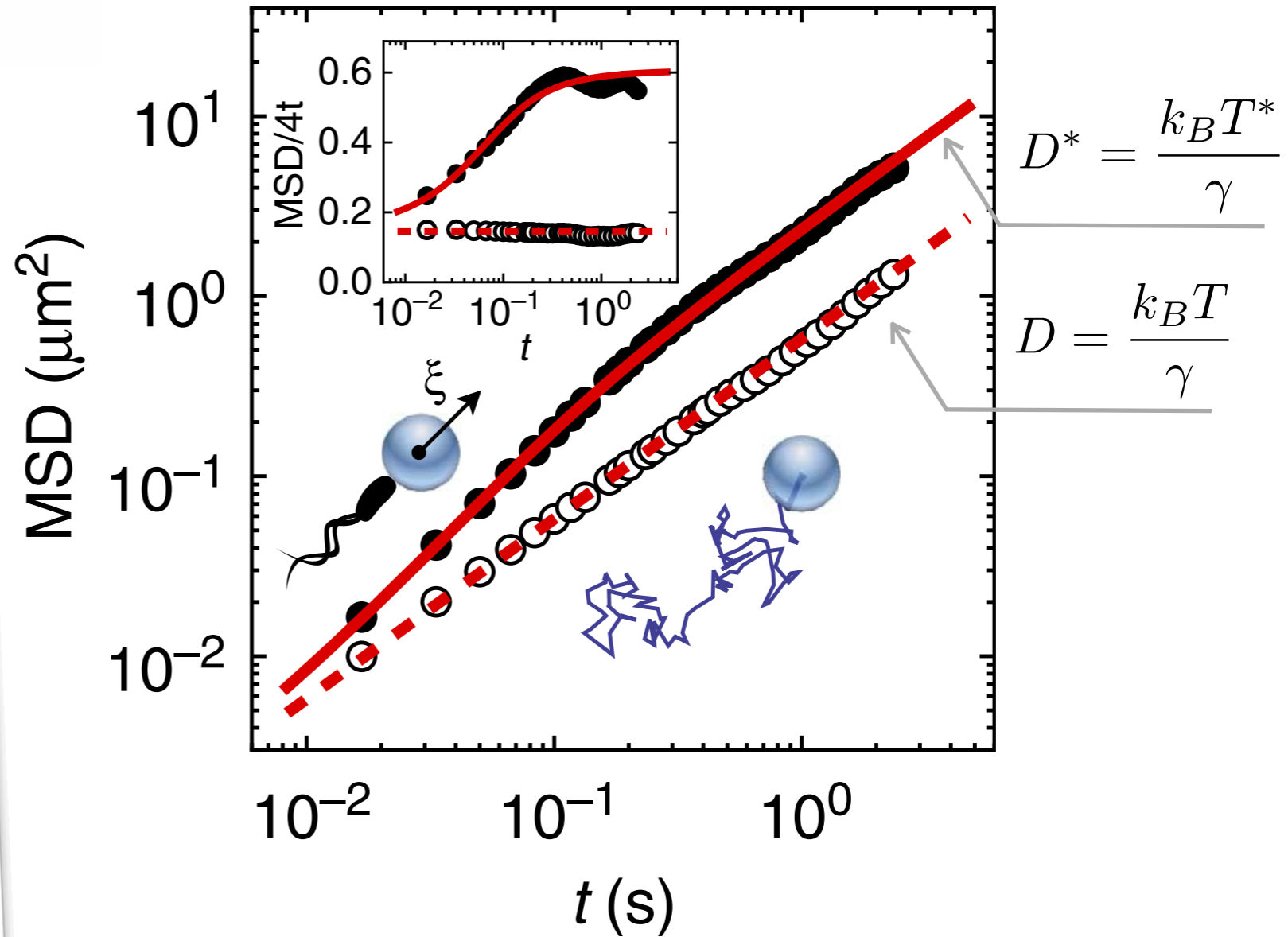
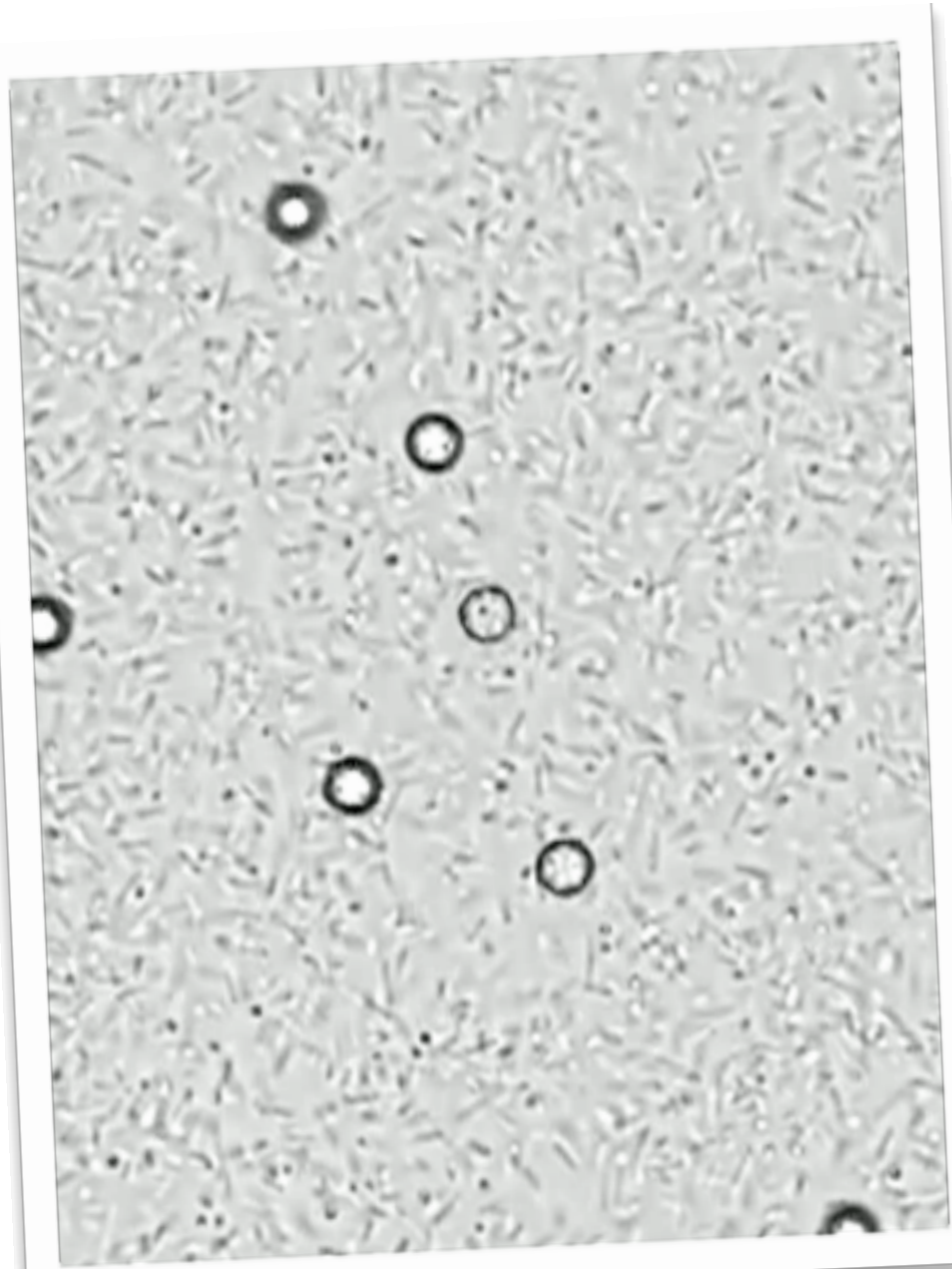
MICROSWIMMERS

PICKUP → TRANSPORT → DELIVERY



# Colloids in active baths

5  $\mu\text{m}$  LATEX BEADS IN E.coli



ACTIVE NOISE

$$0 = f(x) - \gamma \dot{x}(t) + \eta(t) + \xi(t)$$

$$\langle \xi(t) \rangle = 0$$

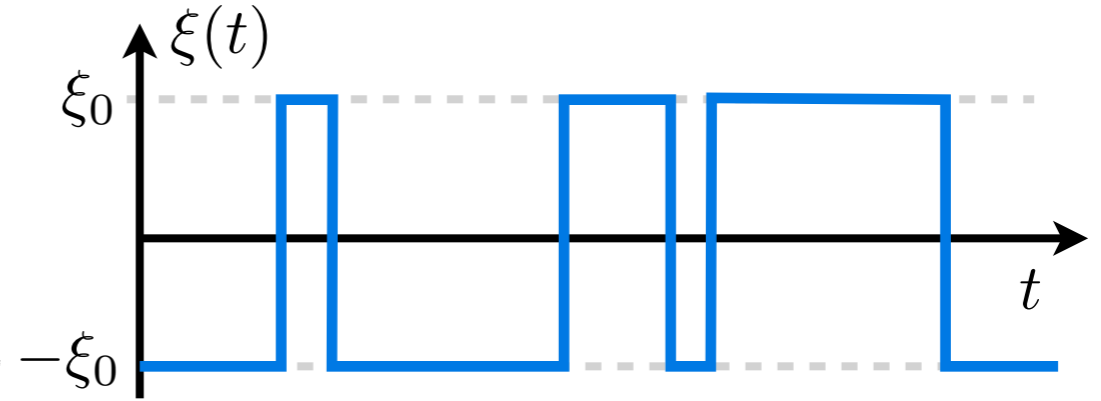
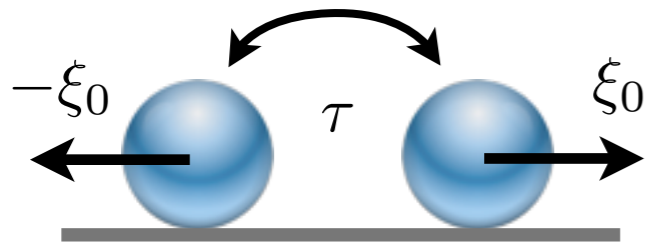
$$\langle \xi(0) \xi(t) \rangle = \langle \xi^2 \rangle e^{-t/\tau}$$

COLORED NOISE

# Non-equilibrium random walks

## 1D RUN AND TUMBLE

SCHNITZER, PRE (1993)  
 TAILLEUR & GATES, PRL (2008)  
 ANGELANI, COSTANZO, RDL, EPL (2011)



### COLORED DICOTOMOUS(1D) NOISE

$$\langle \xi(t) \rangle = 0$$

$$\langle \xi(0)\xi(t) \rangle = \xi_0^2 e^{-t/\tau}$$

RUN LENGTH

### FREE PARTICLE

MOBILITY

$$\dot{x}(t) = \xi(t)/\gamma$$

$$v_0 = \xi_0/\gamma$$

$$\langle \Delta r(t)^2 \rangle = \frac{2v_0^2}{\lambda^2} (\lambda t - 1 + e^{-\lambda t})$$

$$t \ll \tau \rightarrow v_0^2 t^2 \text{ BALLISTIC}$$

$$t \gg \tau \rightarrow 2D^* t \text{ DIFFUSIVE}$$

$$D^* = \frac{v_0^2}{\lambda} = \frac{K_B T^*}{\gamma}$$

$f_0 v_0 \lambda^{-1}$

### RUN & TUMBLE IN EXTERNAL FIELD (J=0)

$$\frac{\rho(x)}{\rho(0)} = \frac{T^*(0)}{T^*(x)} \exp \left[ \int_0^x \frac{f(x)}{k_B T^*(x)} dx \right]$$

$$T^*(x) = T^* - f(x)^2 \tau / \gamma$$

SPACE DEPENDENT TEMPERATURE

### WHITE NOISE LIMIT

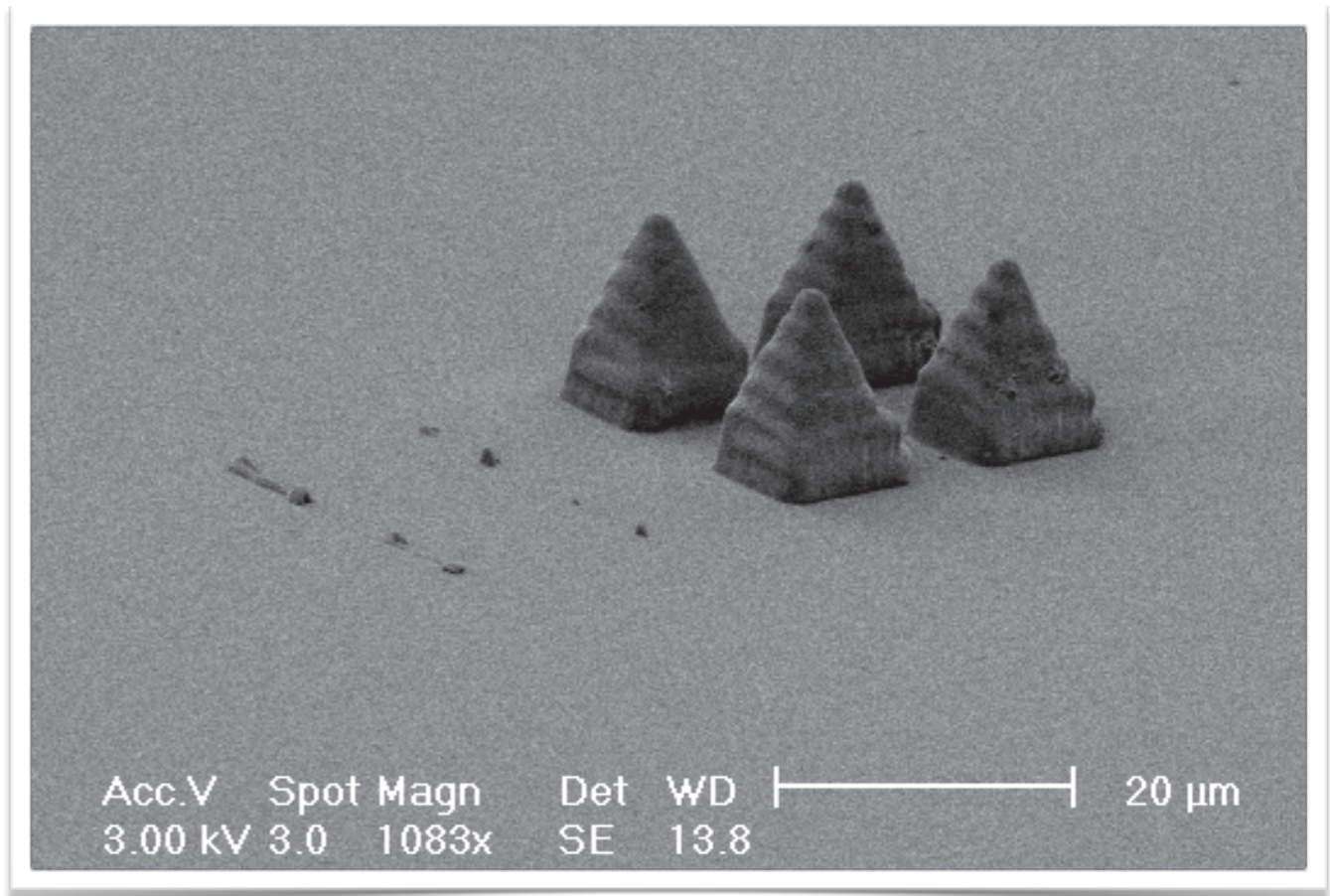
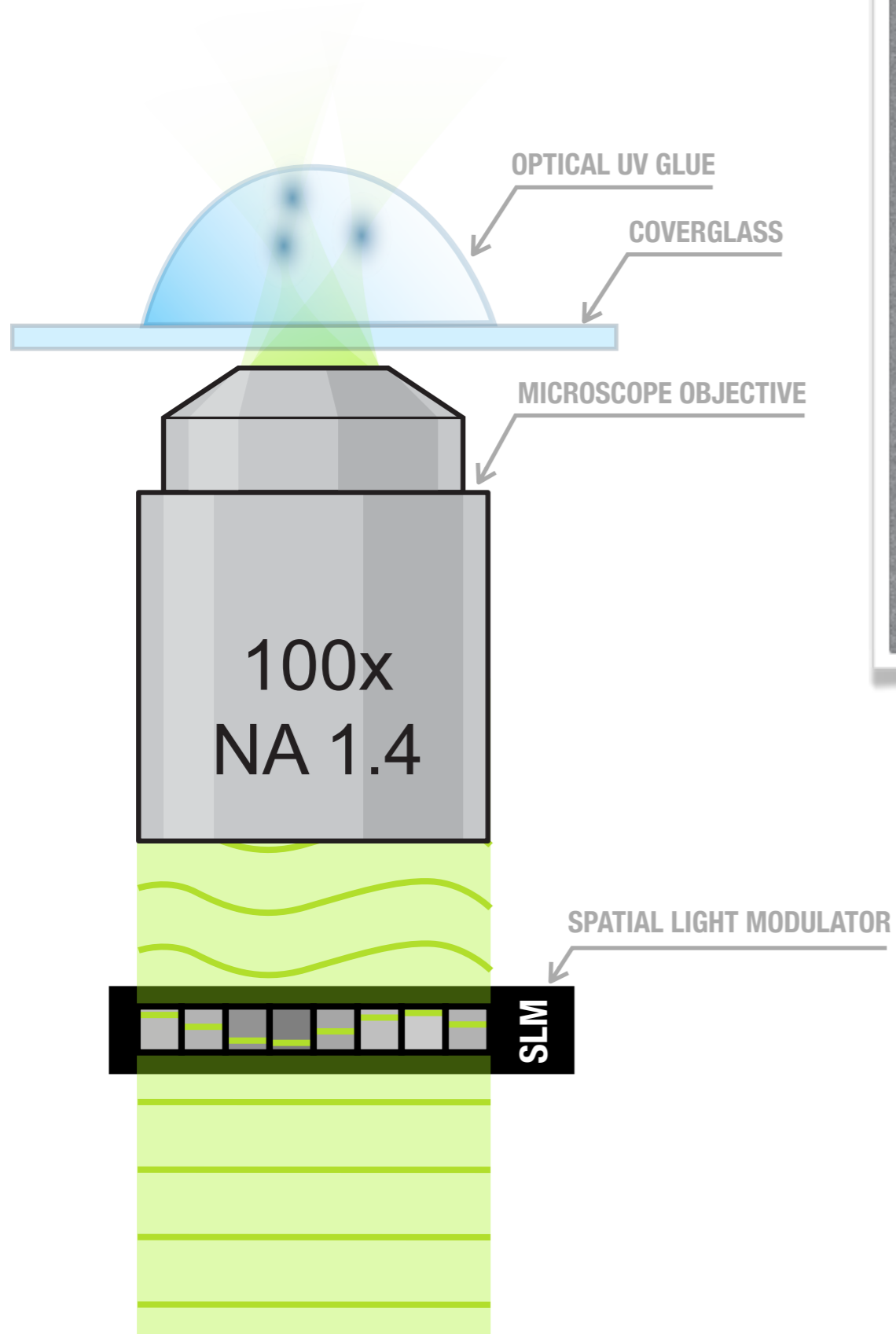
$$\tau \rightarrow 0$$

$$T(x) \rightarrow T^*$$

$$\rho(x) \propto \exp \left[ -\frac{U(x)}{K_B T^*} \right]$$

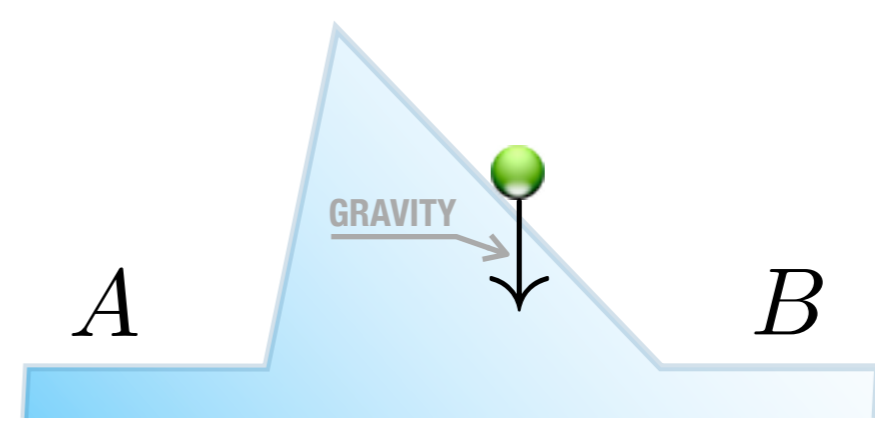
BOLTZMANN-LIKE STATISTICS

# Holographic microfabrication



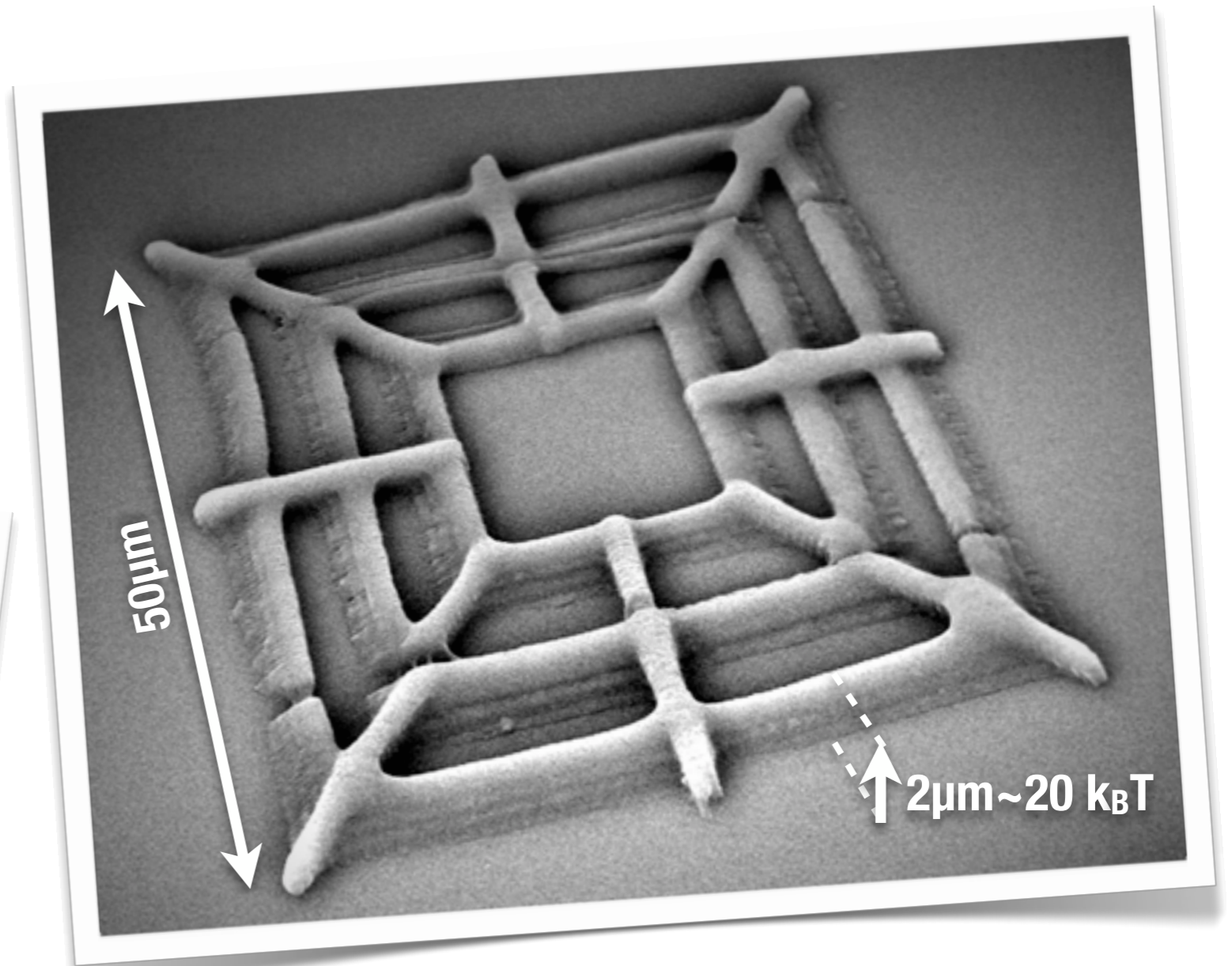
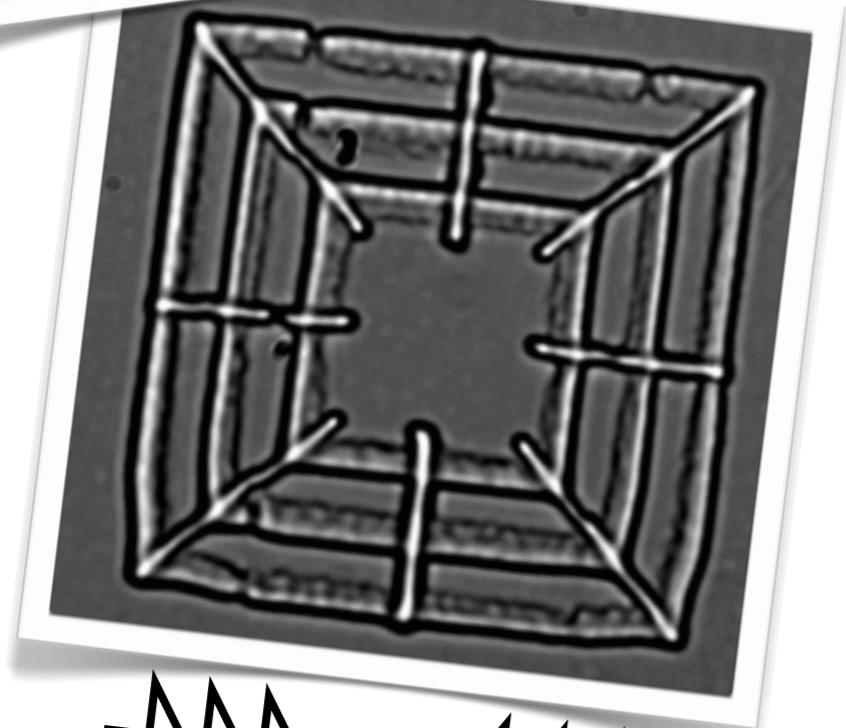
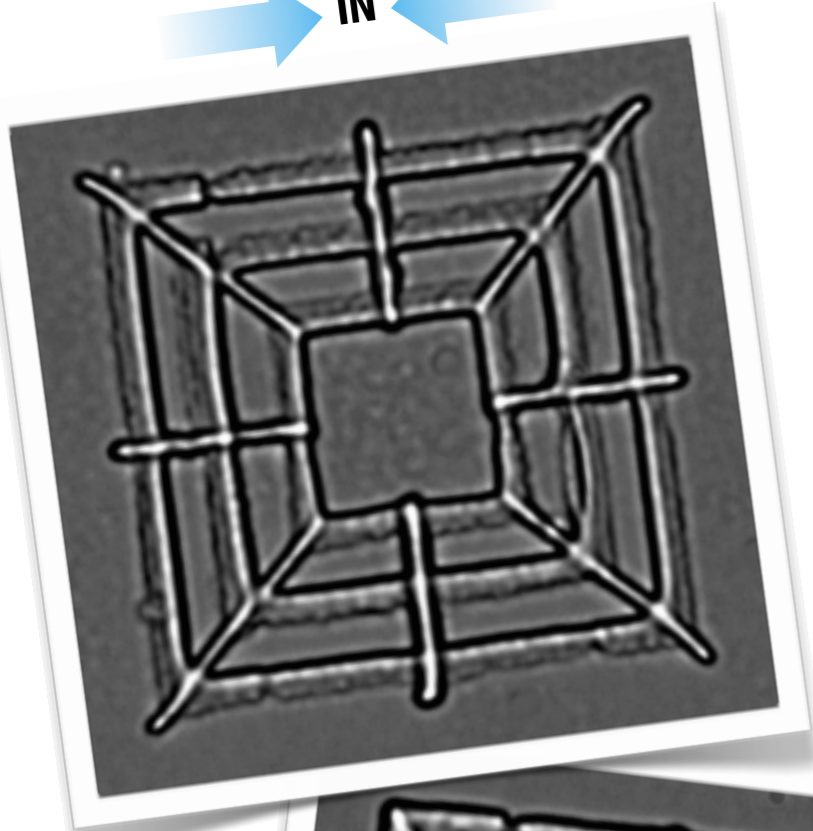
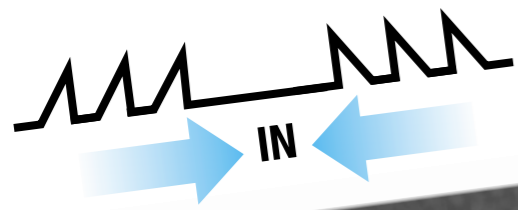
N. J. JENNESS, ET AL. OPT. EXPRESS 16, 15942 (2008).

**A MICROPATTERNED SURFACE WITH A 3D TOPOGRAPHY ACTS AS A STATIC (GRAVITATIONAL) ENERGY LANDSCAPE**



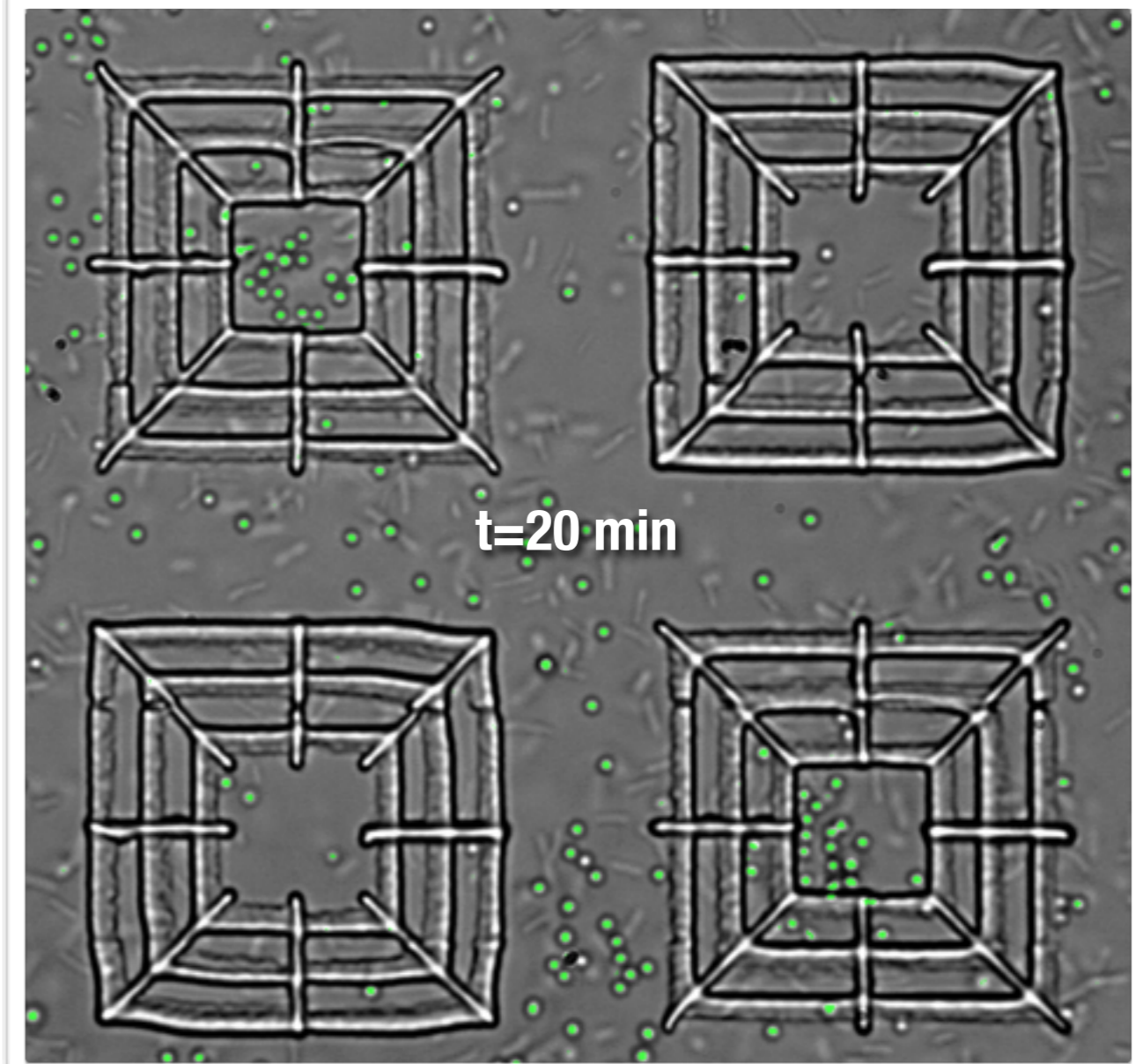
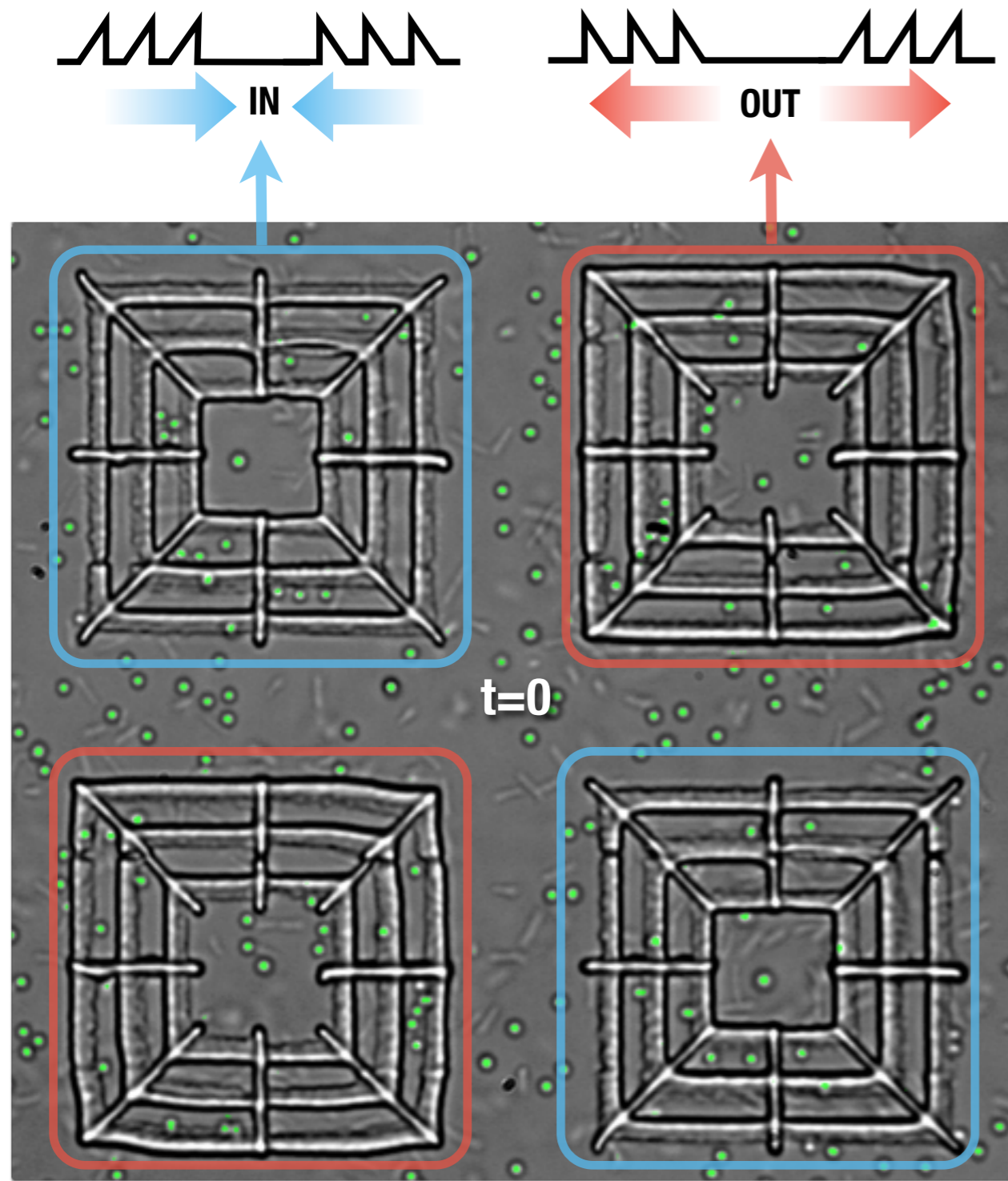
# Collecting and ejecting structures

KOUMAKIS, LEPORE, MAGGI, RDL, Nature Comm. (2013)



# Targeted delivery of colloids

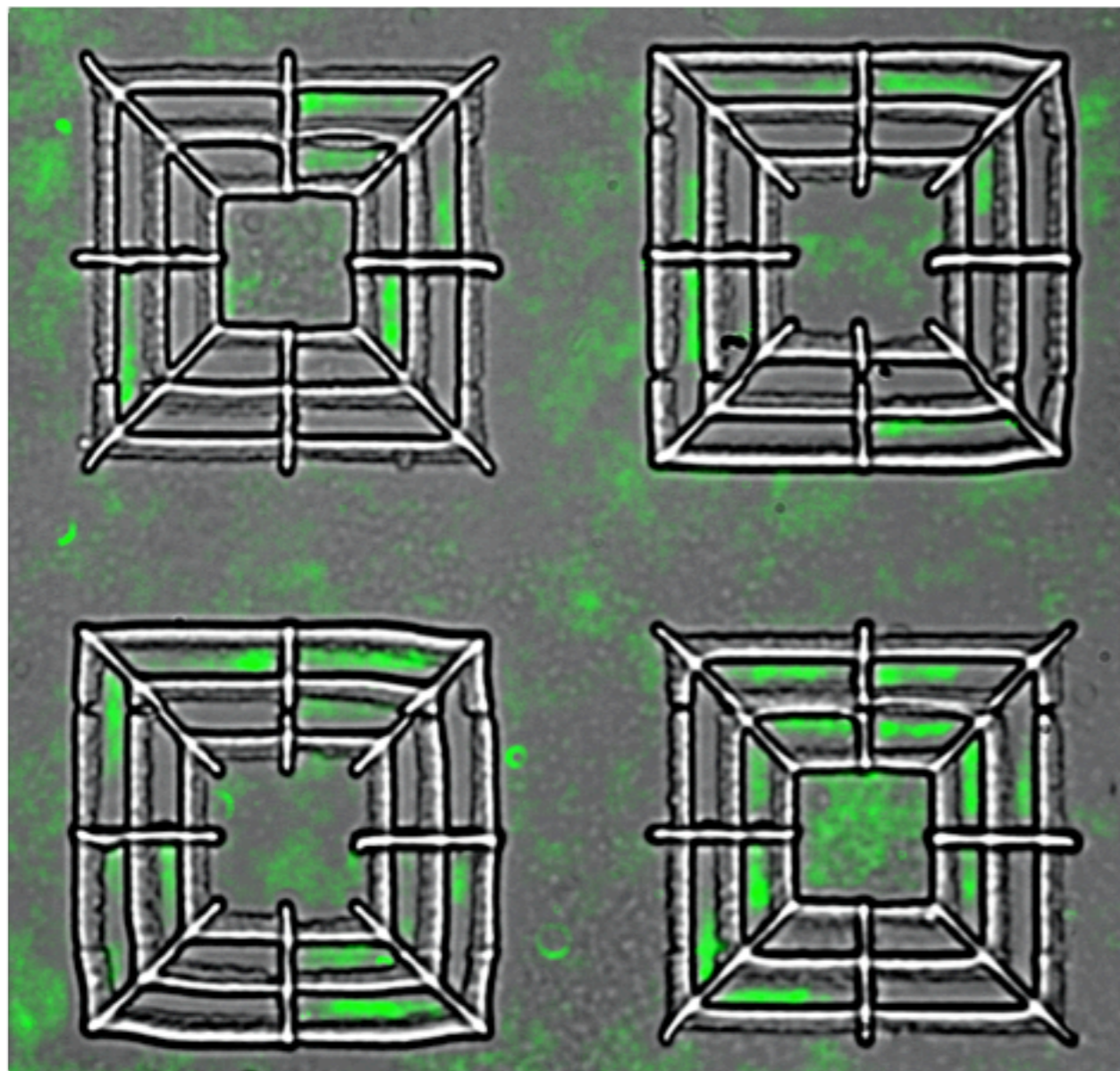
KOUMAKIS, LEPORE, MAGGI, RDL, Nature Comm. (2013)



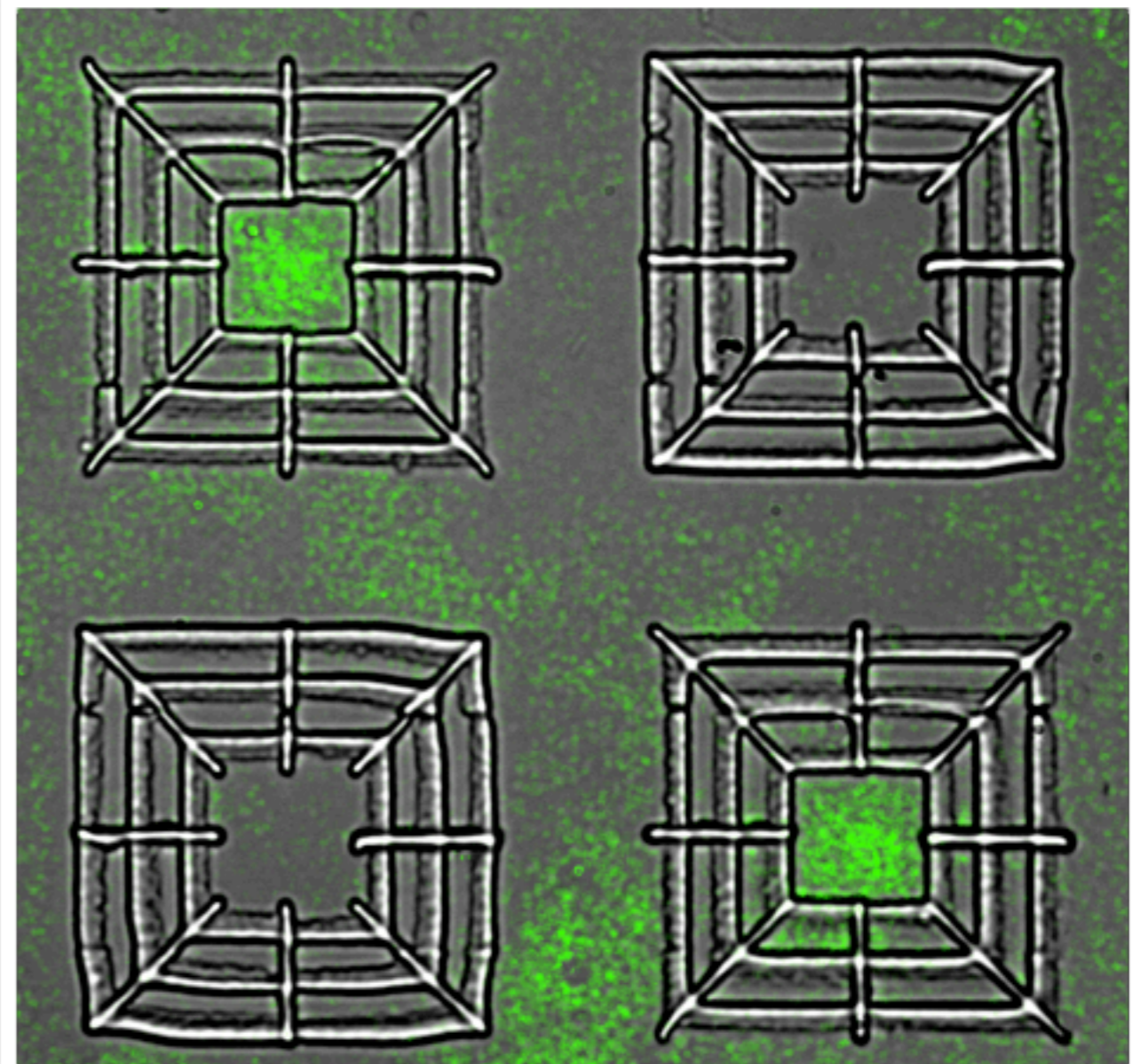
# Average particle densities

KOUMAKIS, LEPORE, MAGGI, RDL, Nature Comm. (2013)

## THERMAL BATH

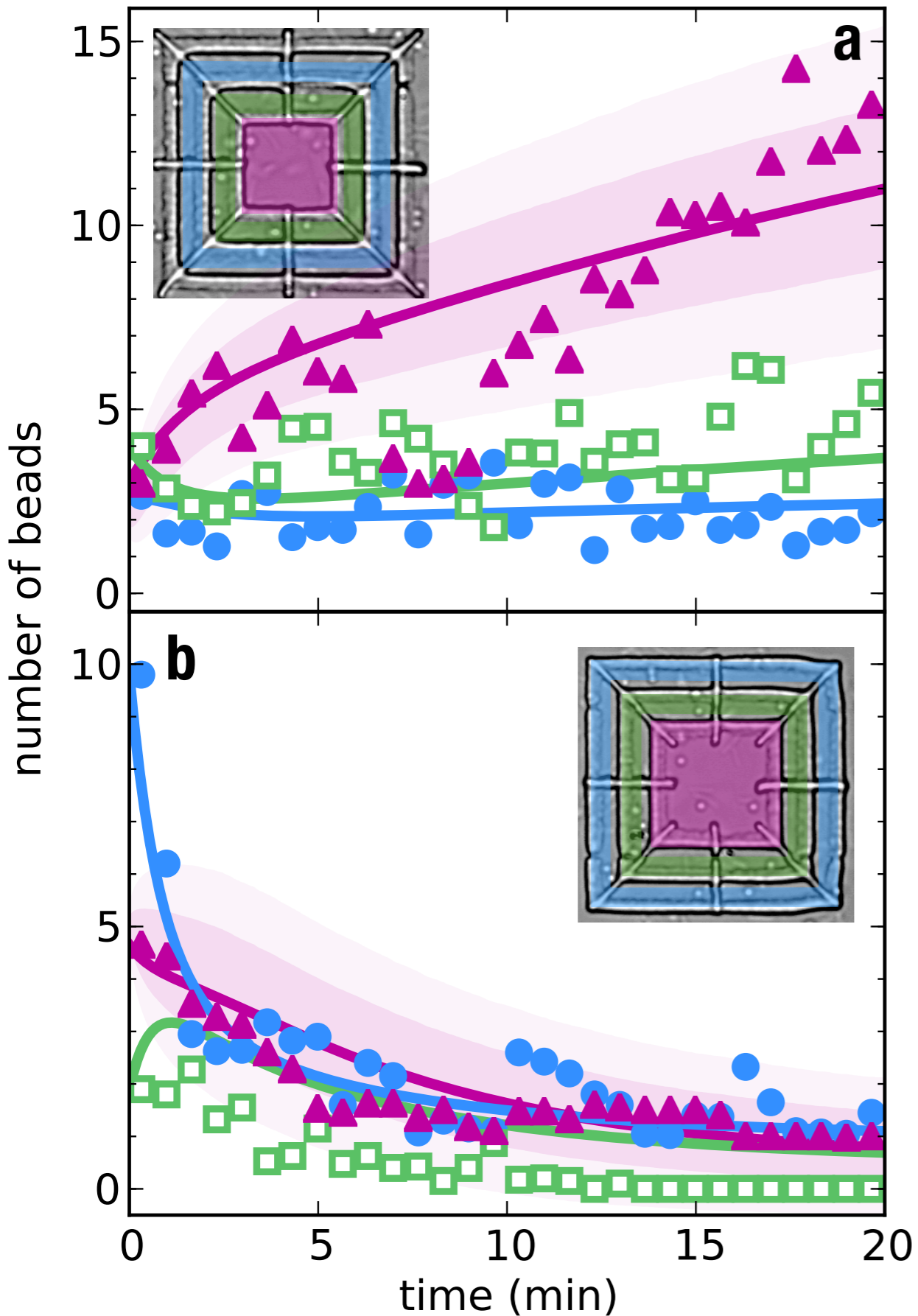


## ACTIVE BATH



# Fitting transition rates

KOUMAKIS, LEPORE, MAGGI, RDL, Nature Comm. (2013)

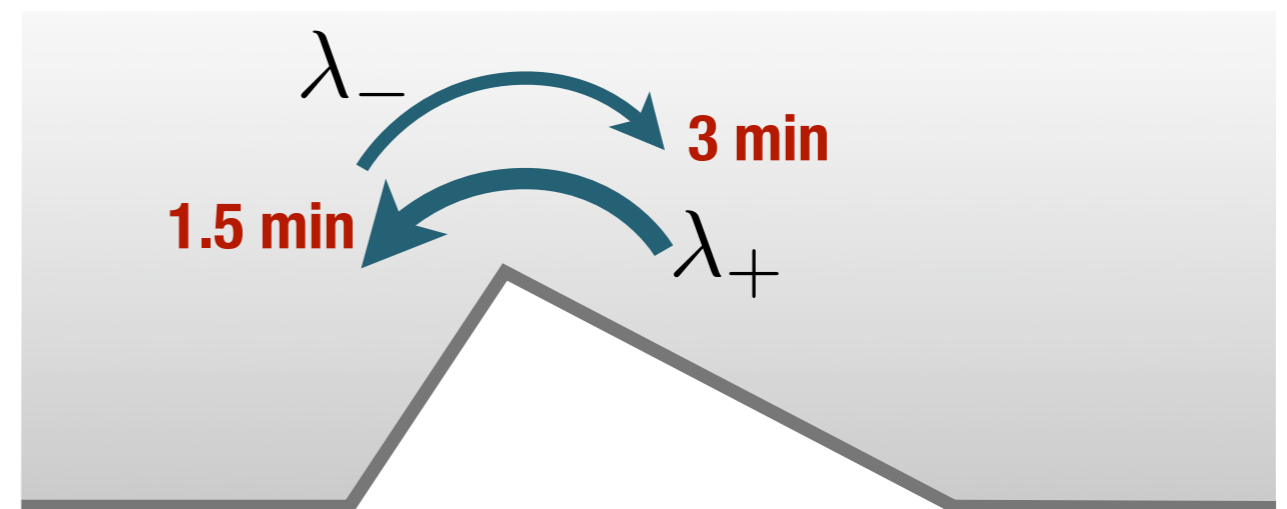


$$\dot{\mathbf{N}}(t) = -\mathbf{\Lambda} \cdot \mathbf{N}(t) + \mathbf{S}$$

$$\mathbf{N} = (n_0, n_1, n_2) \quad \mathbf{S} = (0, 0, s)$$

$$\lambda_+ = 0.66 \text{ min}^{-1}$$

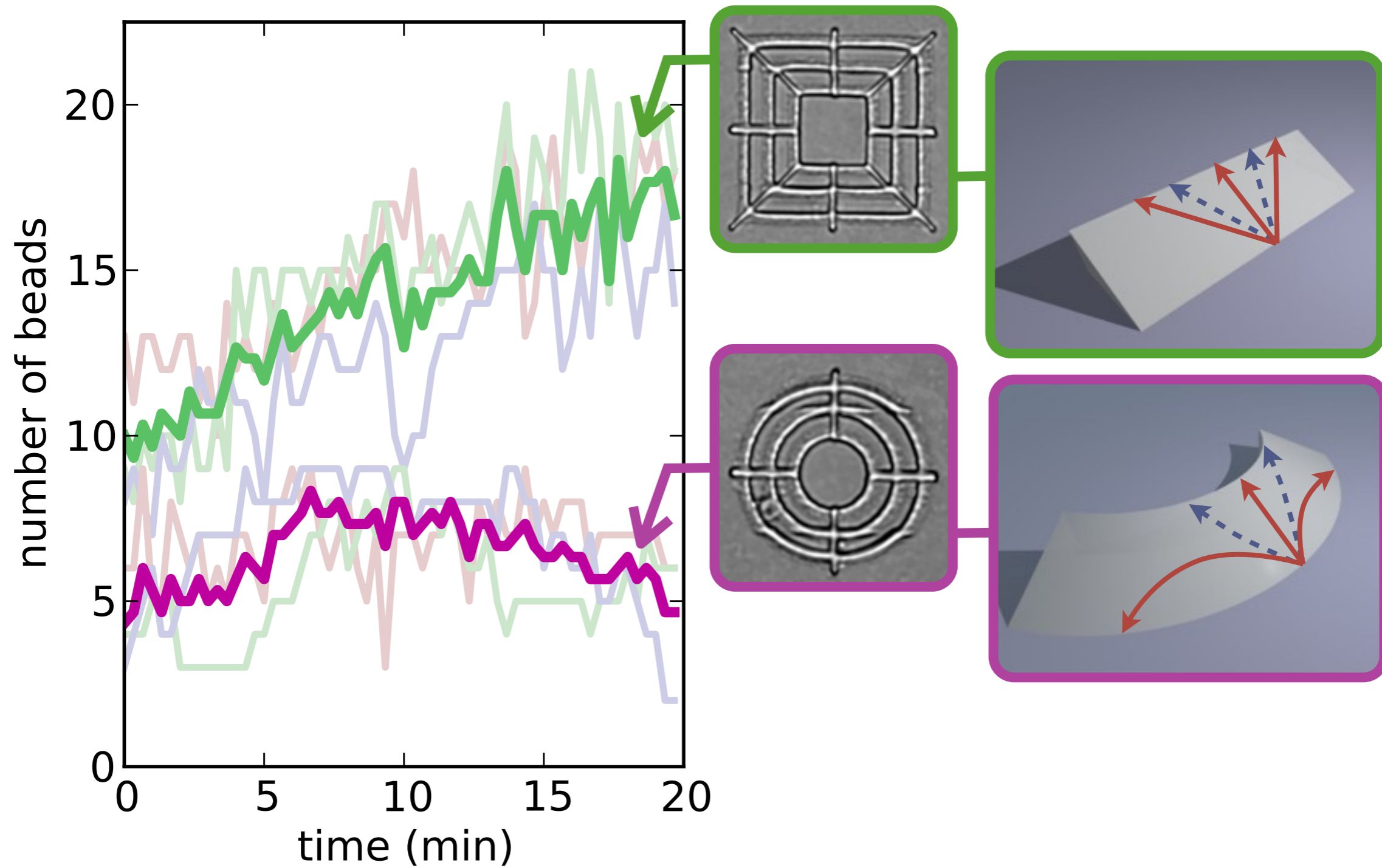
$$\lambda_- = 0.36 \text{ min}^{-1}$$





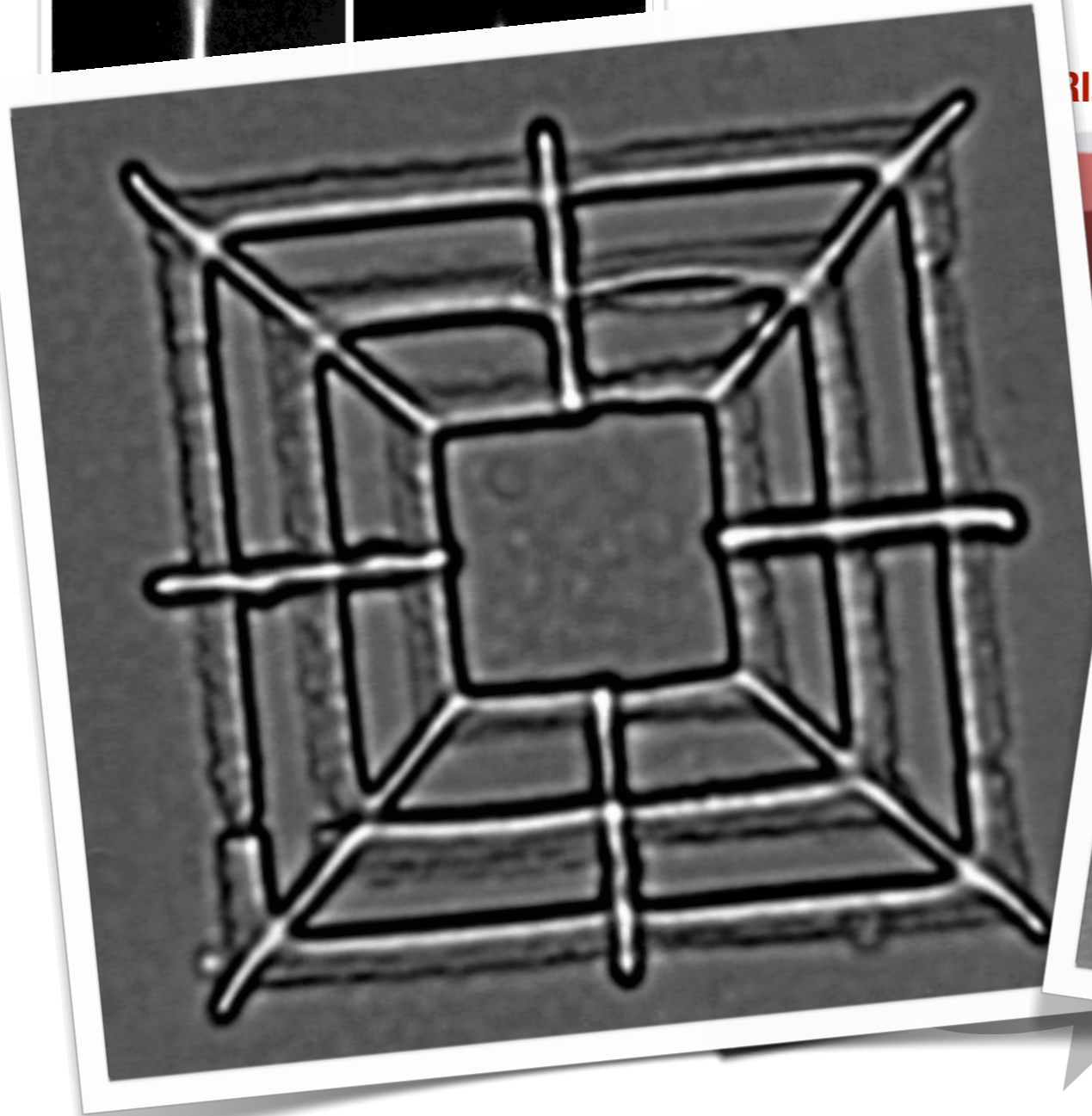
# Curvature effect

KOUMAKIS, LEPORE, MAGGI, RDL, Nature Comm. (2013)

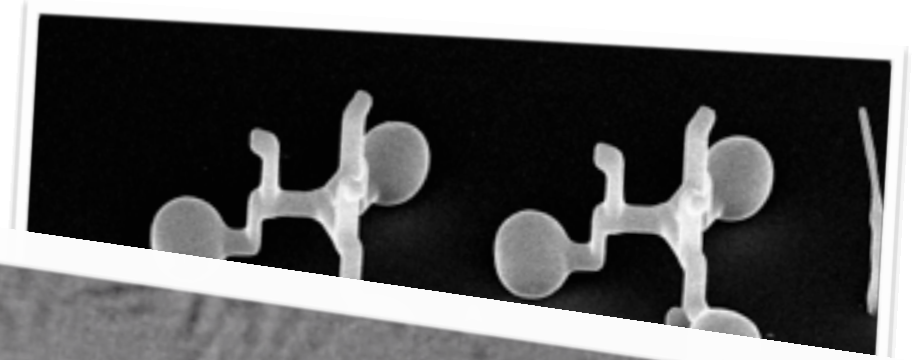
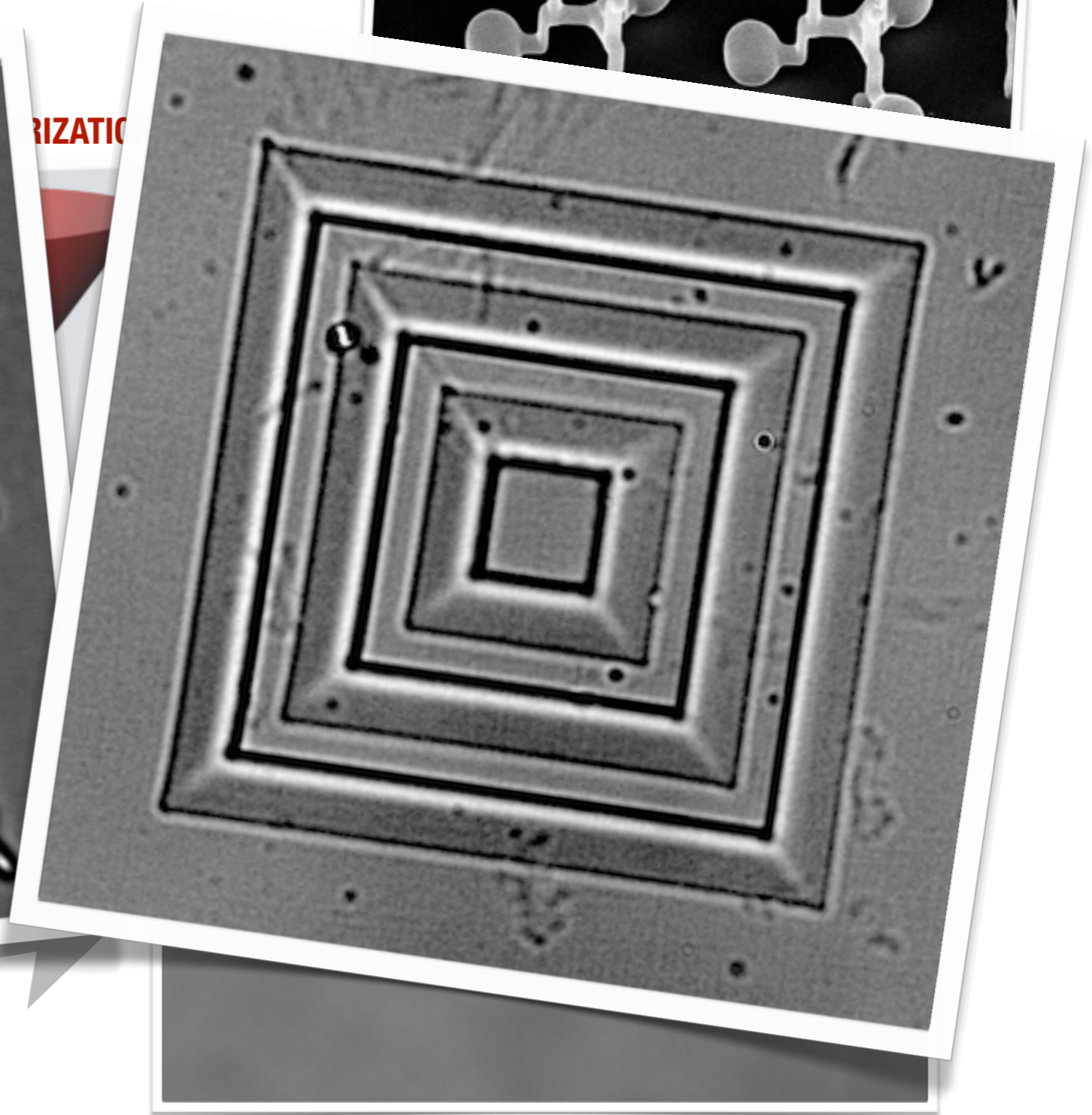


# Two-photon lithography

## TWO PHOTON ABSORPTION

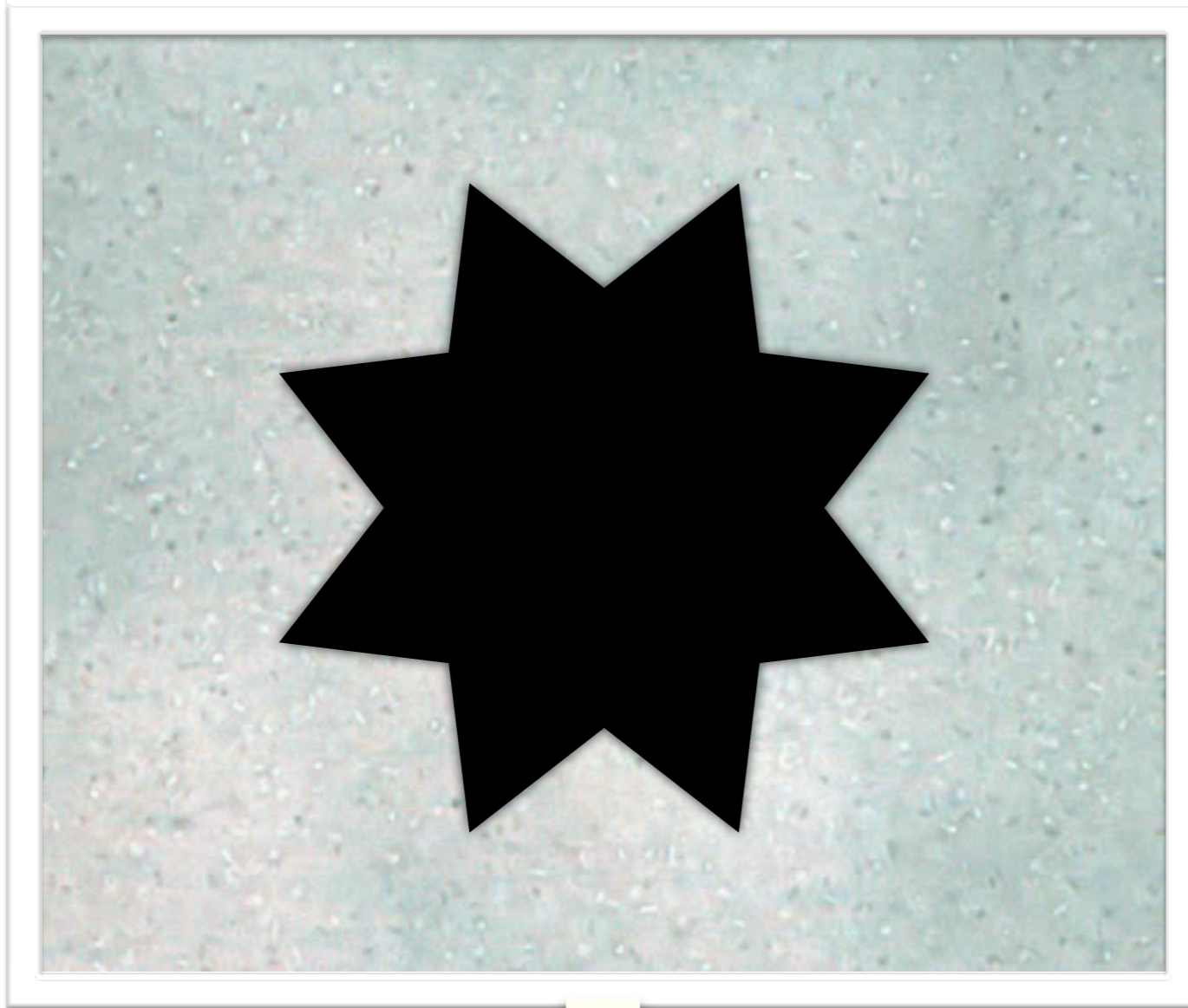


RIZATIO



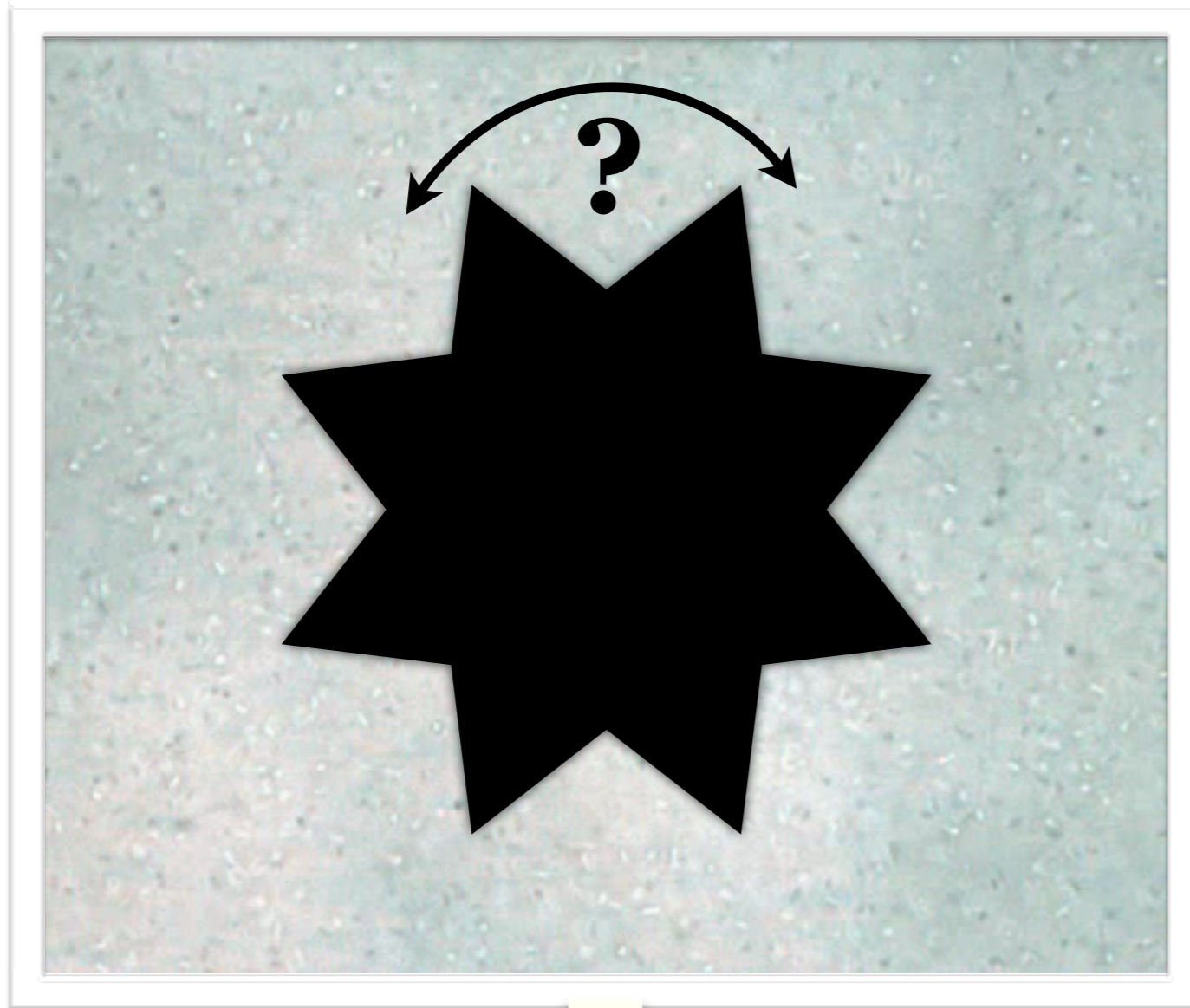
STOCHASTIC DYNAMICS IN ACTIVE BATHS II  
a bacterial ratchet motor

## UNBIASED RANDOM FLUCTUATIONS



**WORK?**

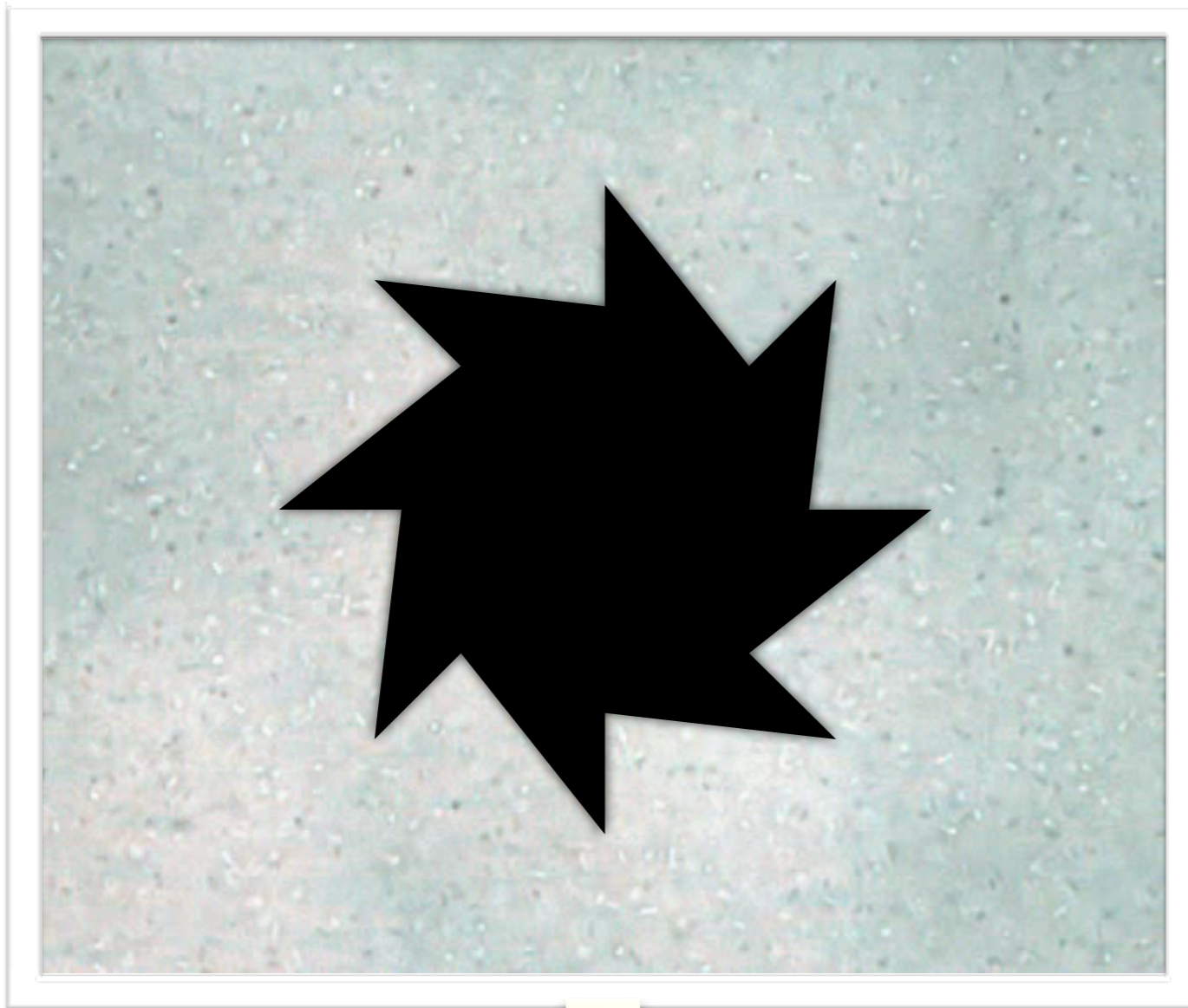
## UNBIASED RANDOM FLUCTUATIONS



**WORK?**

# Work from fluctuations

## UNBIASED RANDOM FLUCTUATIONS



**WORK?**

*“C’est la dissymétrie qui crée le phénomène”* P. CURIE, J. PHYS 3, 393, (1894)



# Brownian ratchets

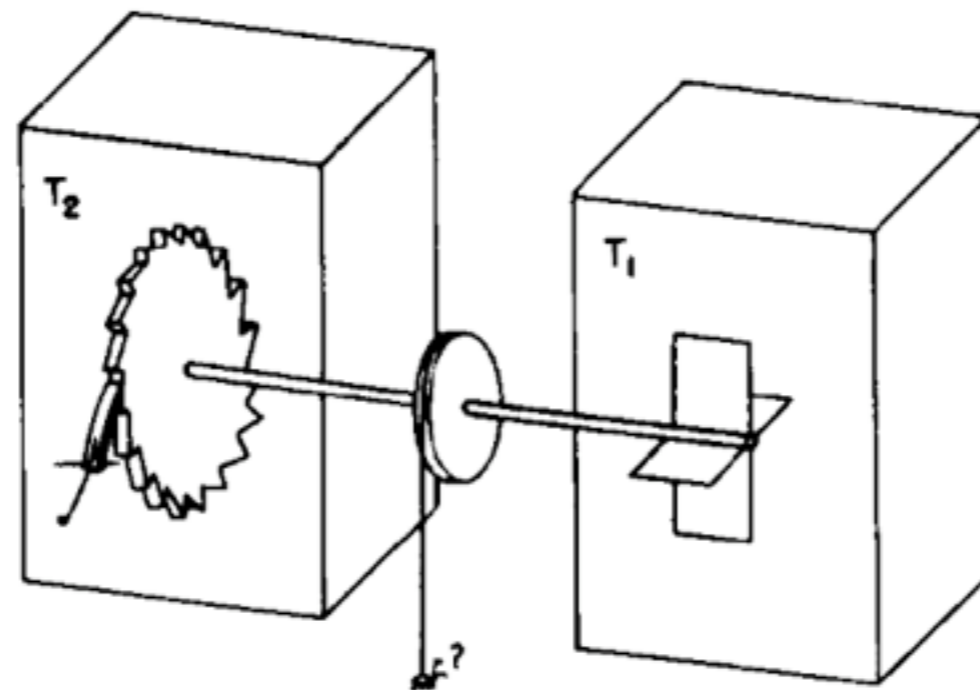
## XXII. EXPERIMENTELL NACHWEISBARE, DER ÜBLICHEN THERMODYNAMIK WIDERSPRECHENDE MOLEKULARPHÄNOMENE.

Physikalische Zeitschrift, XIII. Jahrgang, pp. 1069–1080. 1912. Vortrag vor der 84. Naturforscherversammlung zu Münster (Westfalen).



M. SMOLUCHOWSKI

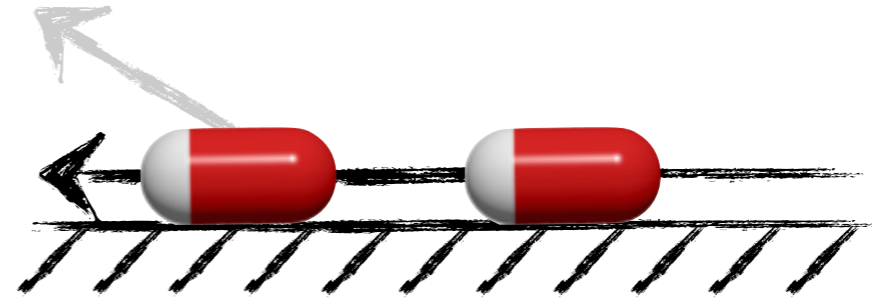
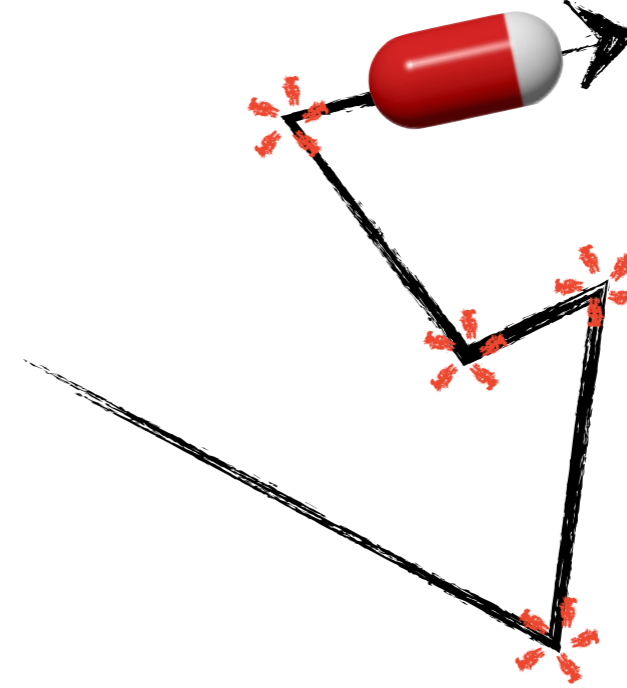
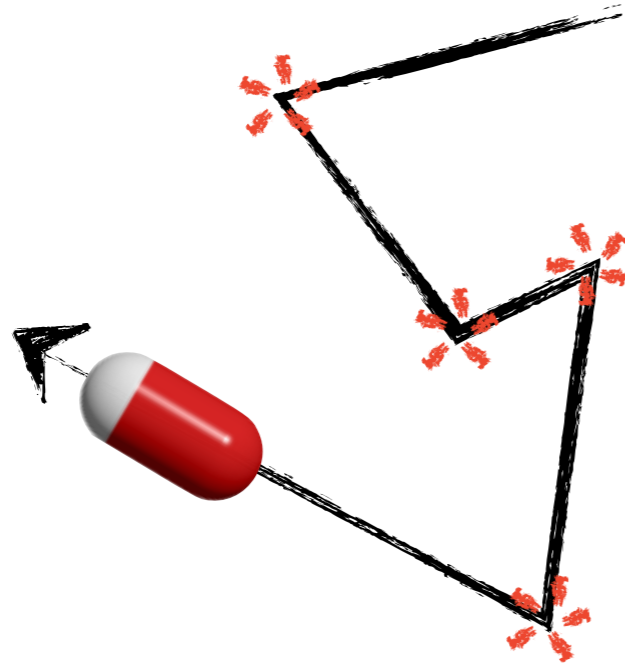
*The Feynman*  
LECTURES ON  
PHYSICS  
MAINLY MECHANICS, RADIATION, AND HEAT



“So it is impossible to design a machine which, in the long run, is more likely to be going one way than the other, if the machine is sufficiently complicated”

“It is based on the fact that the laws of mechanics are reversible”

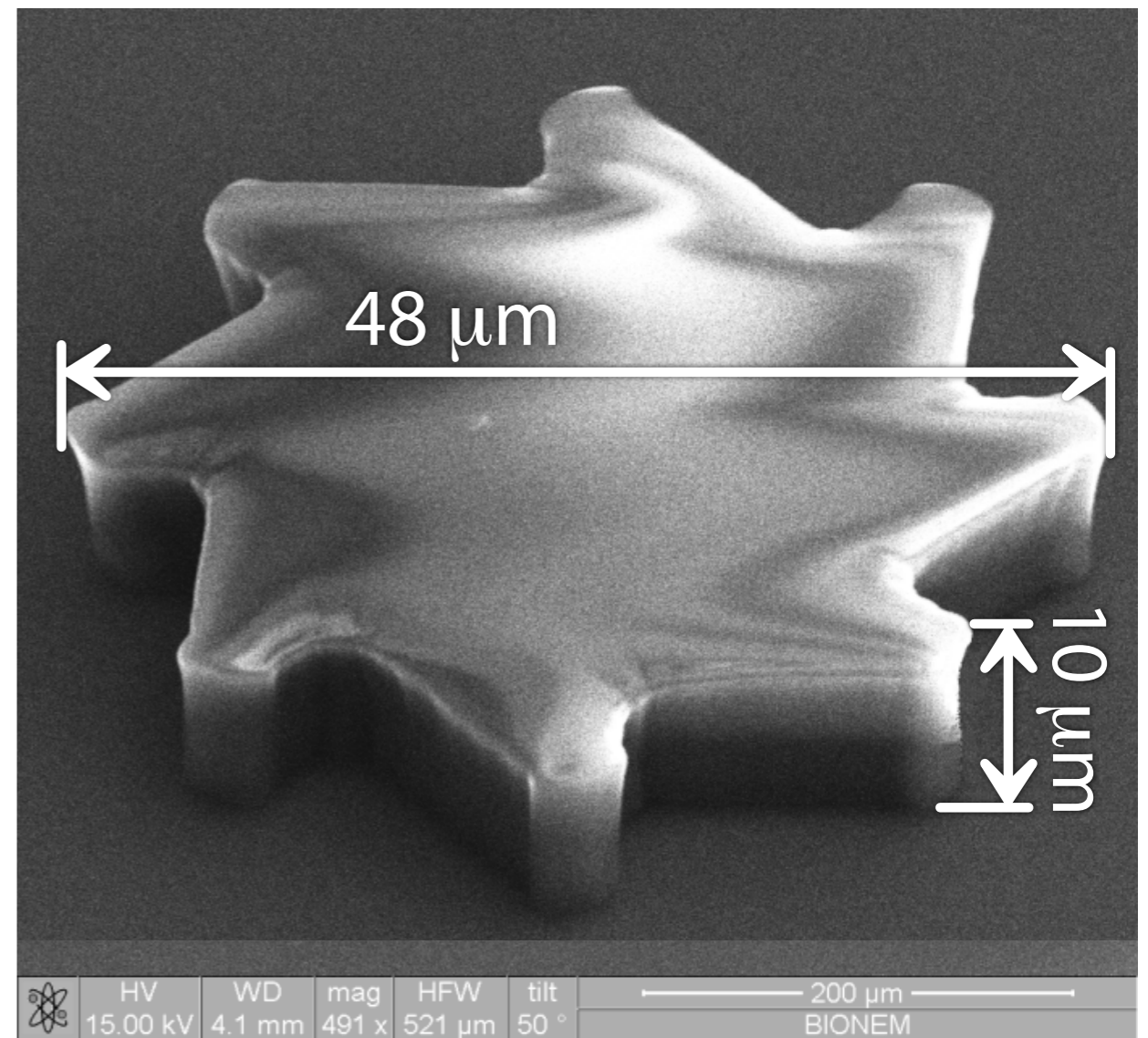
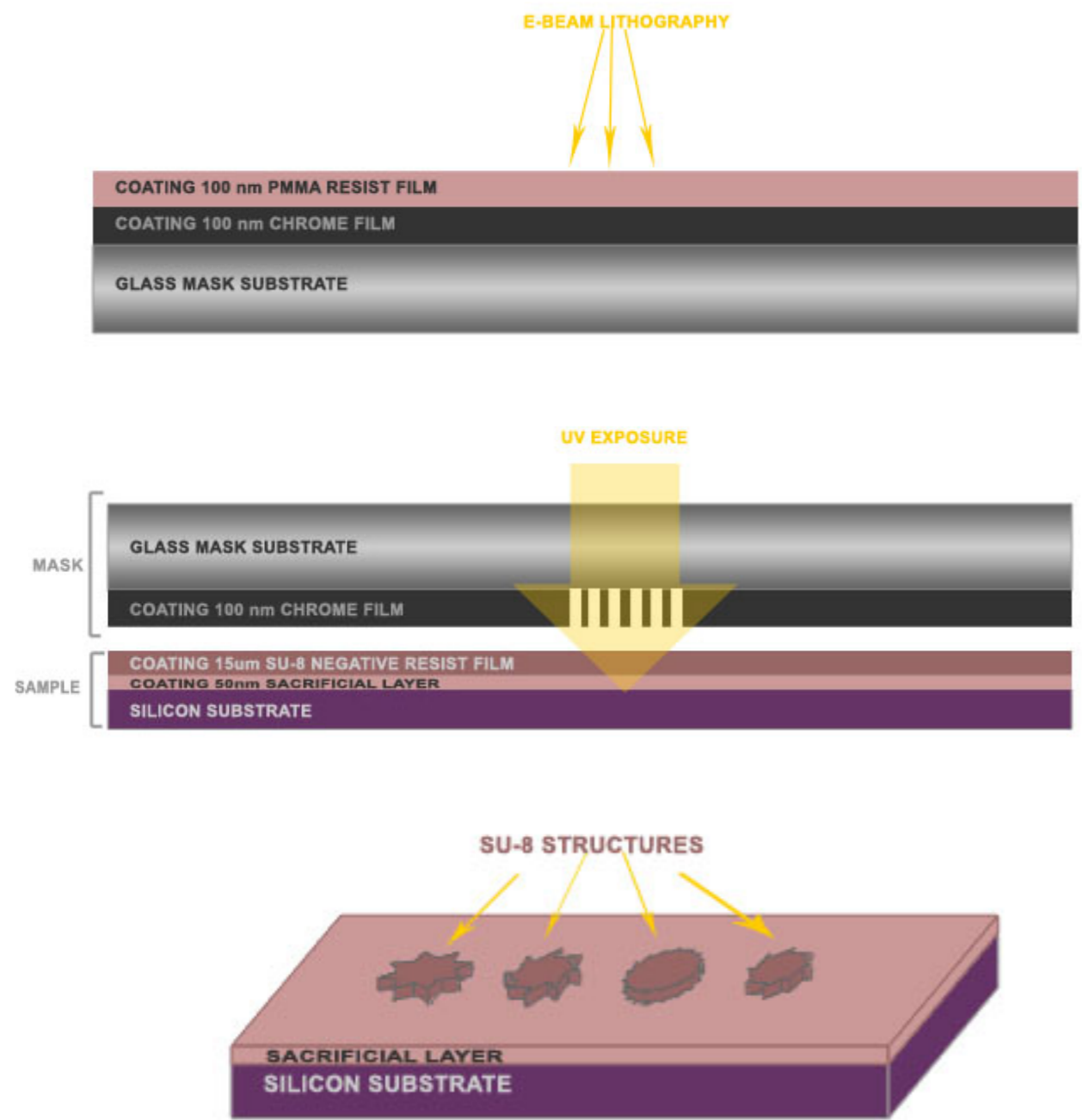
# Bacterial dynamics violates detailed balance



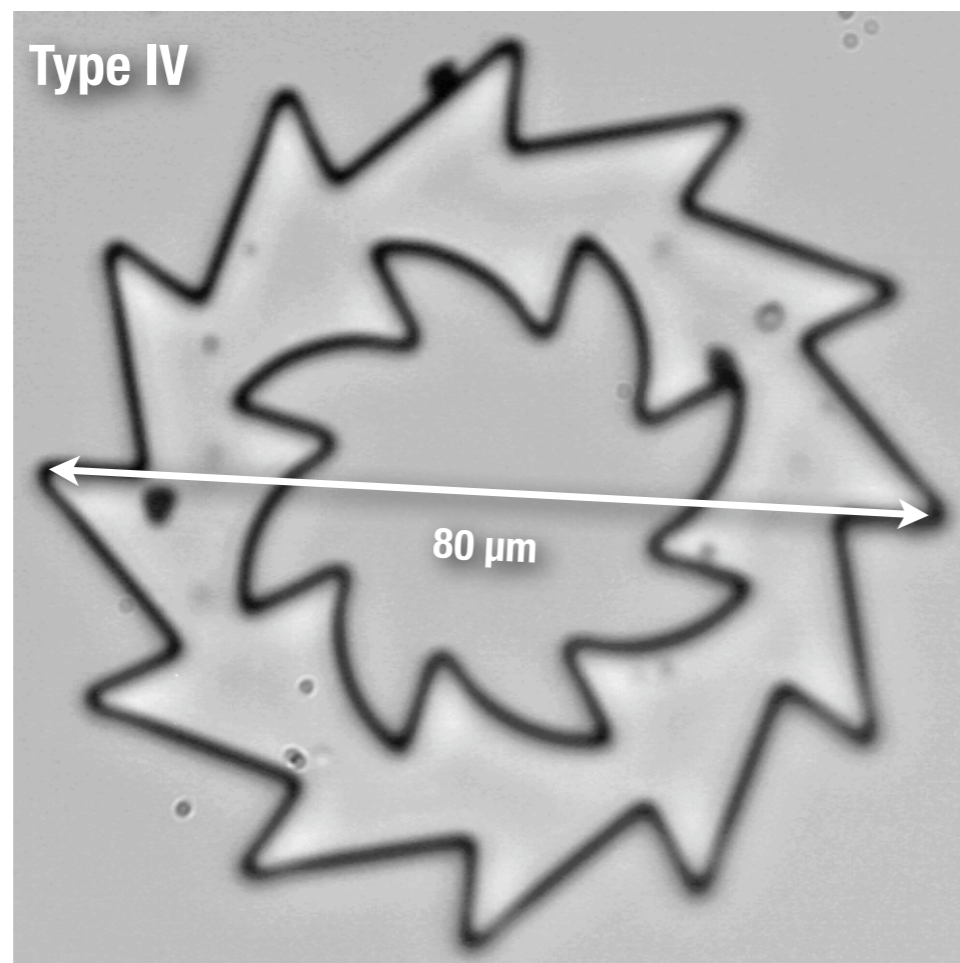
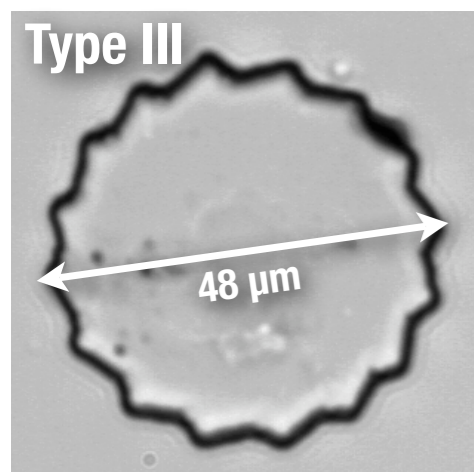
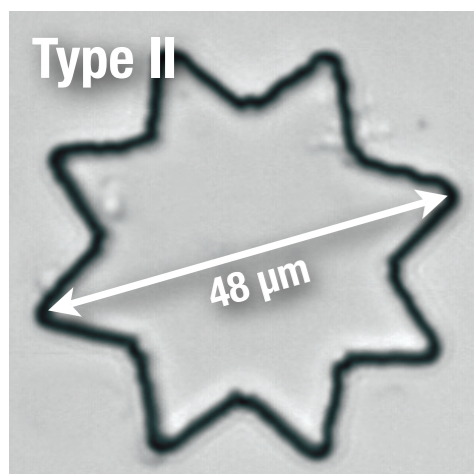
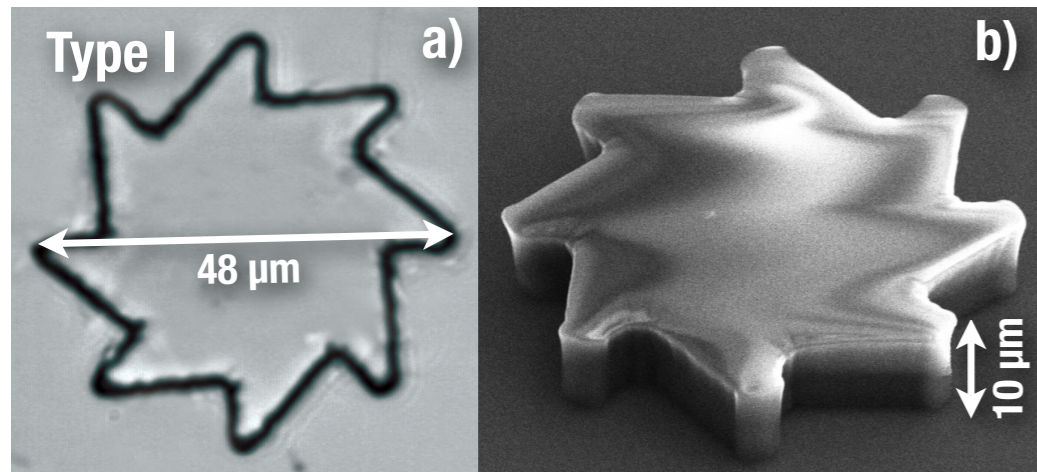


# Micro-fabrication

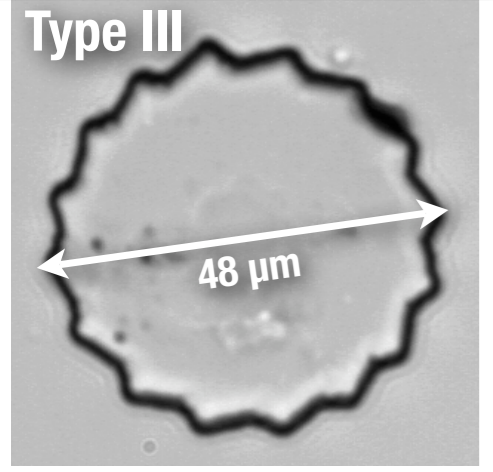
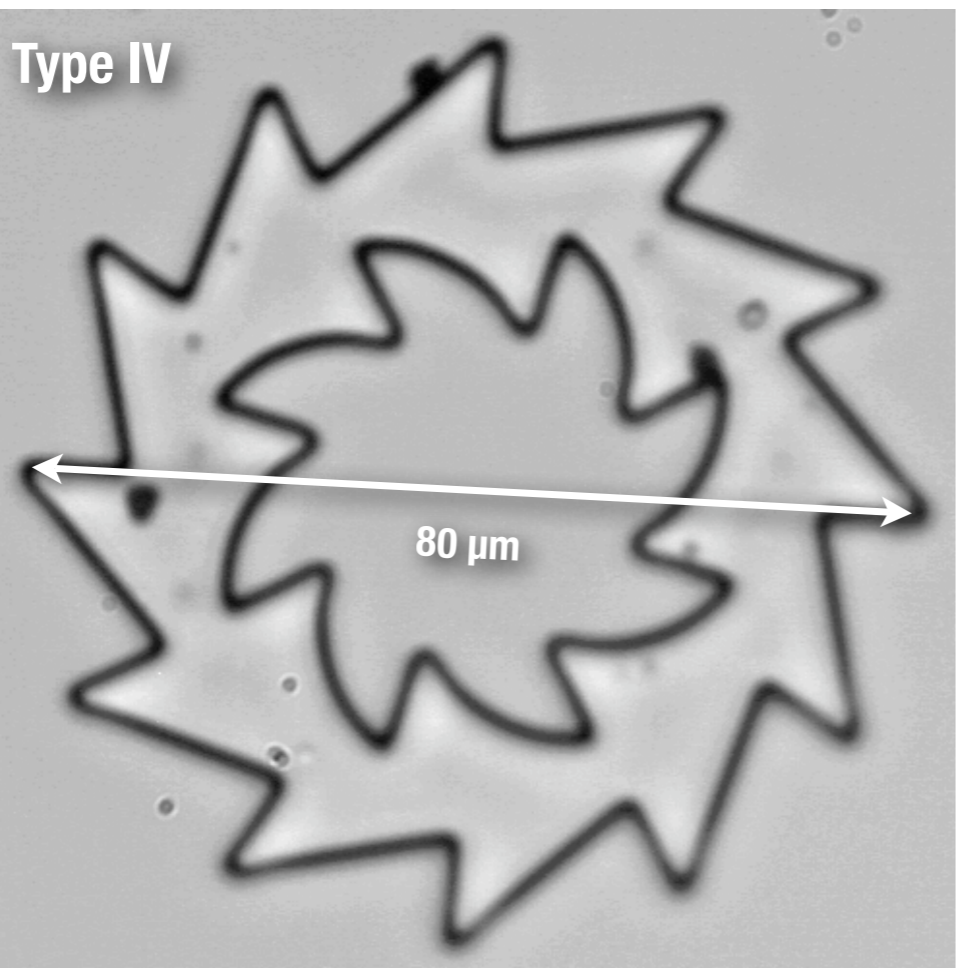
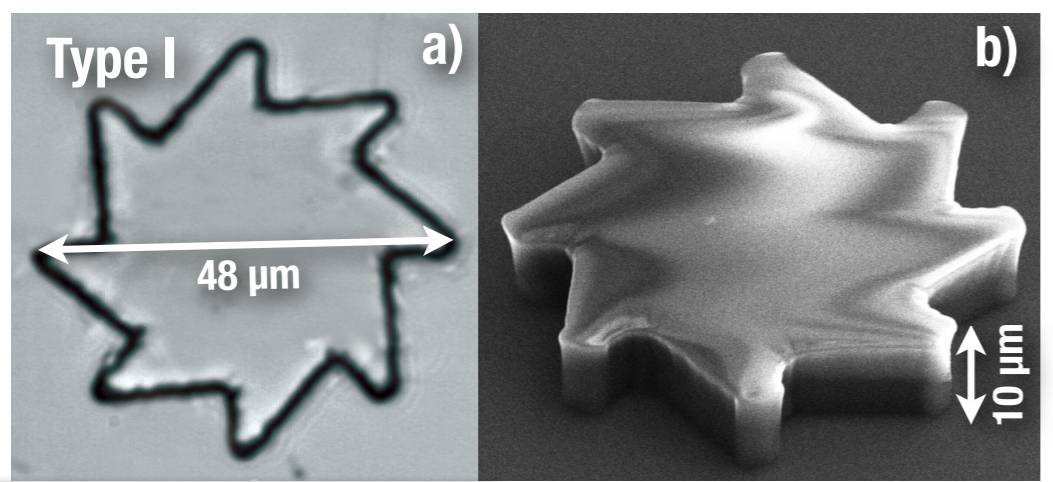
E. Di FABRIZIO BIONEM LAB, CATANZARO



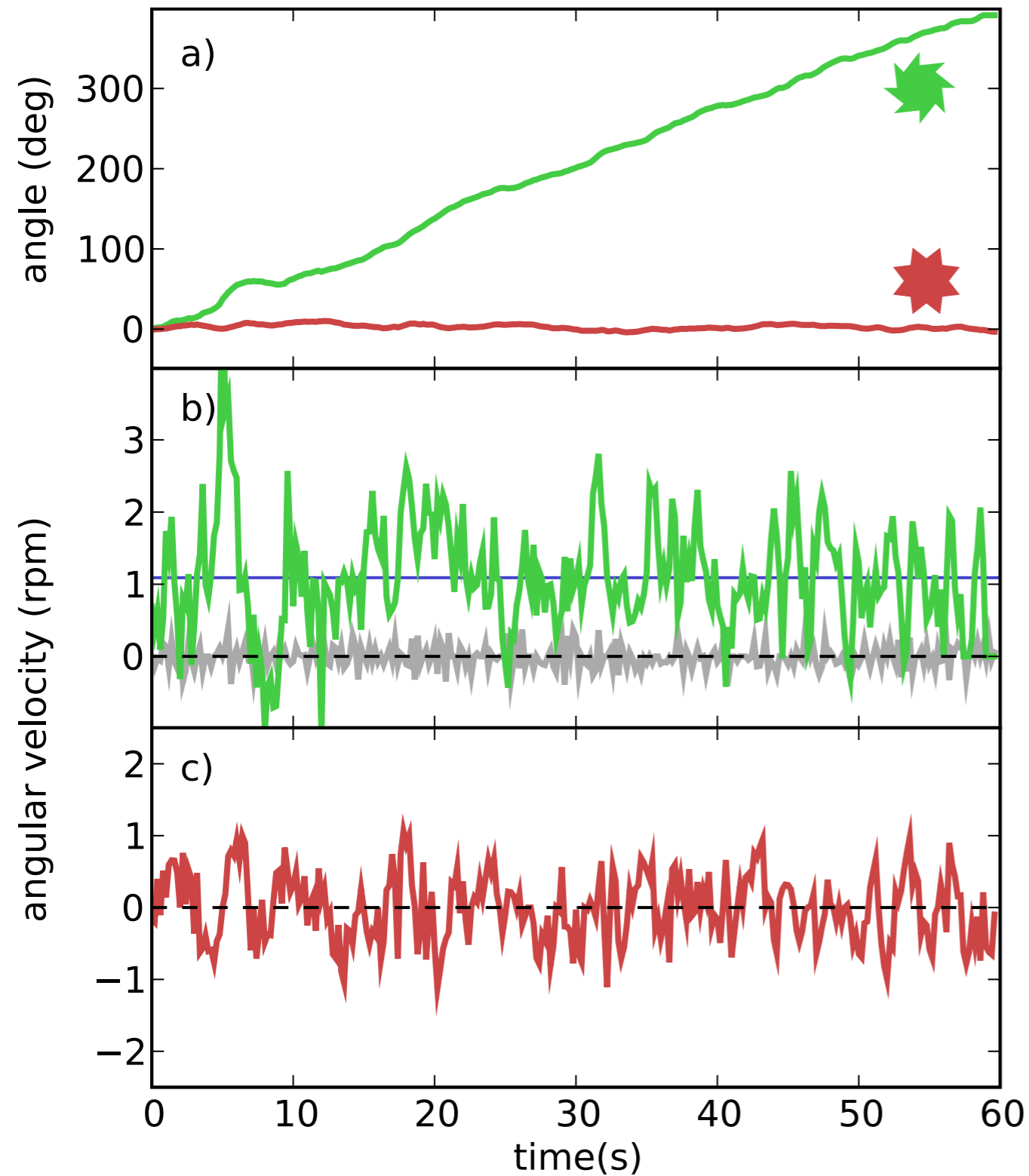
# 2D geometries



# 2D geometries



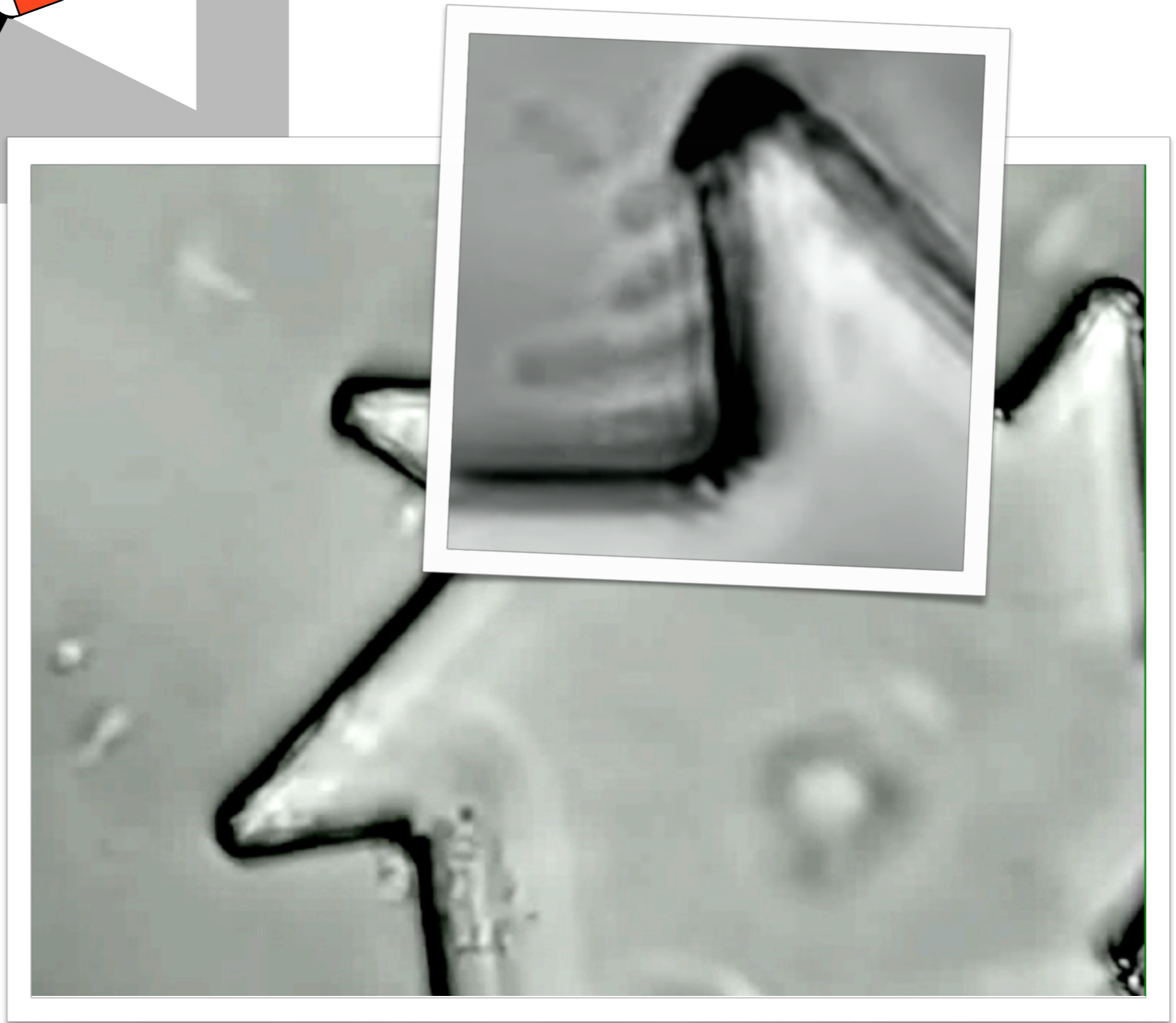
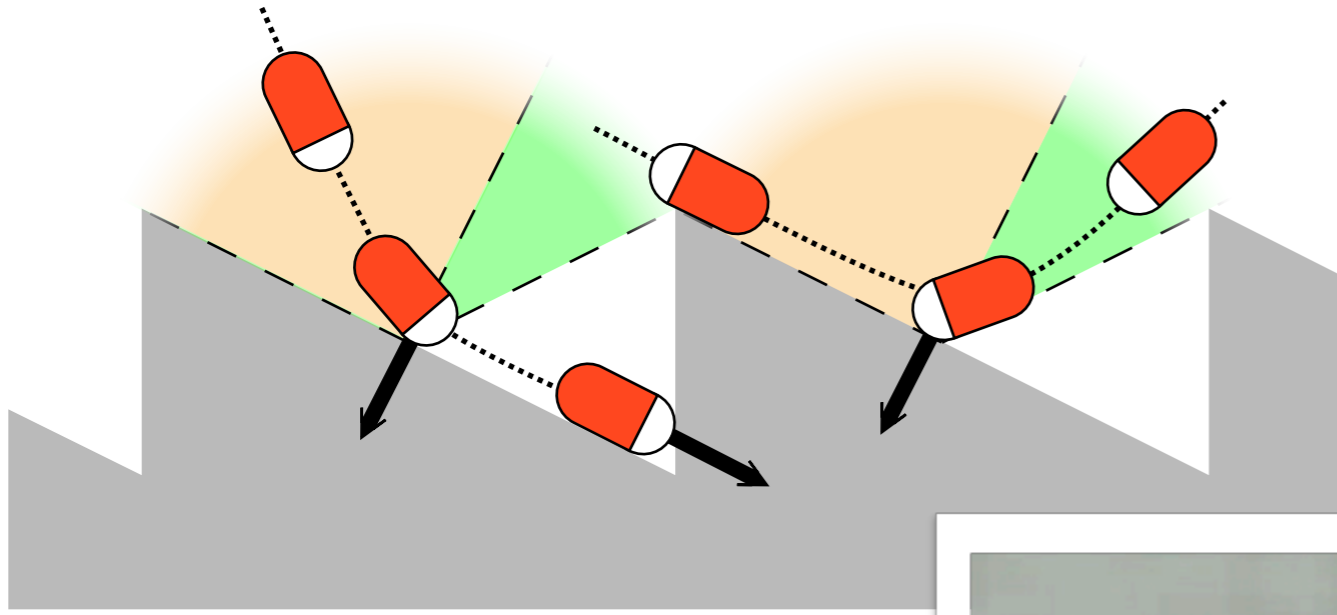
# 2D geometries



R. DI LEONARDO, et al. PNAS (2010)

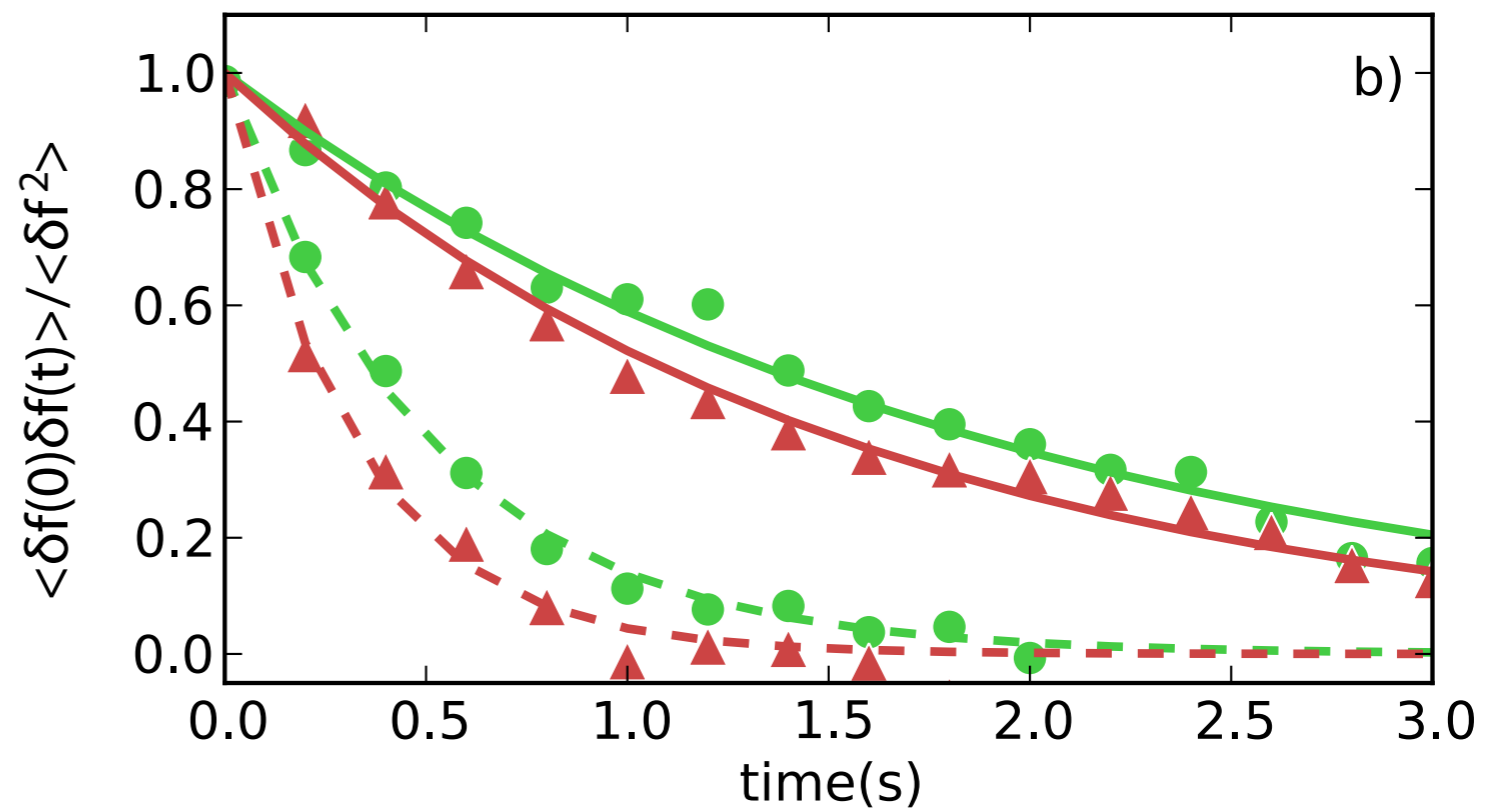
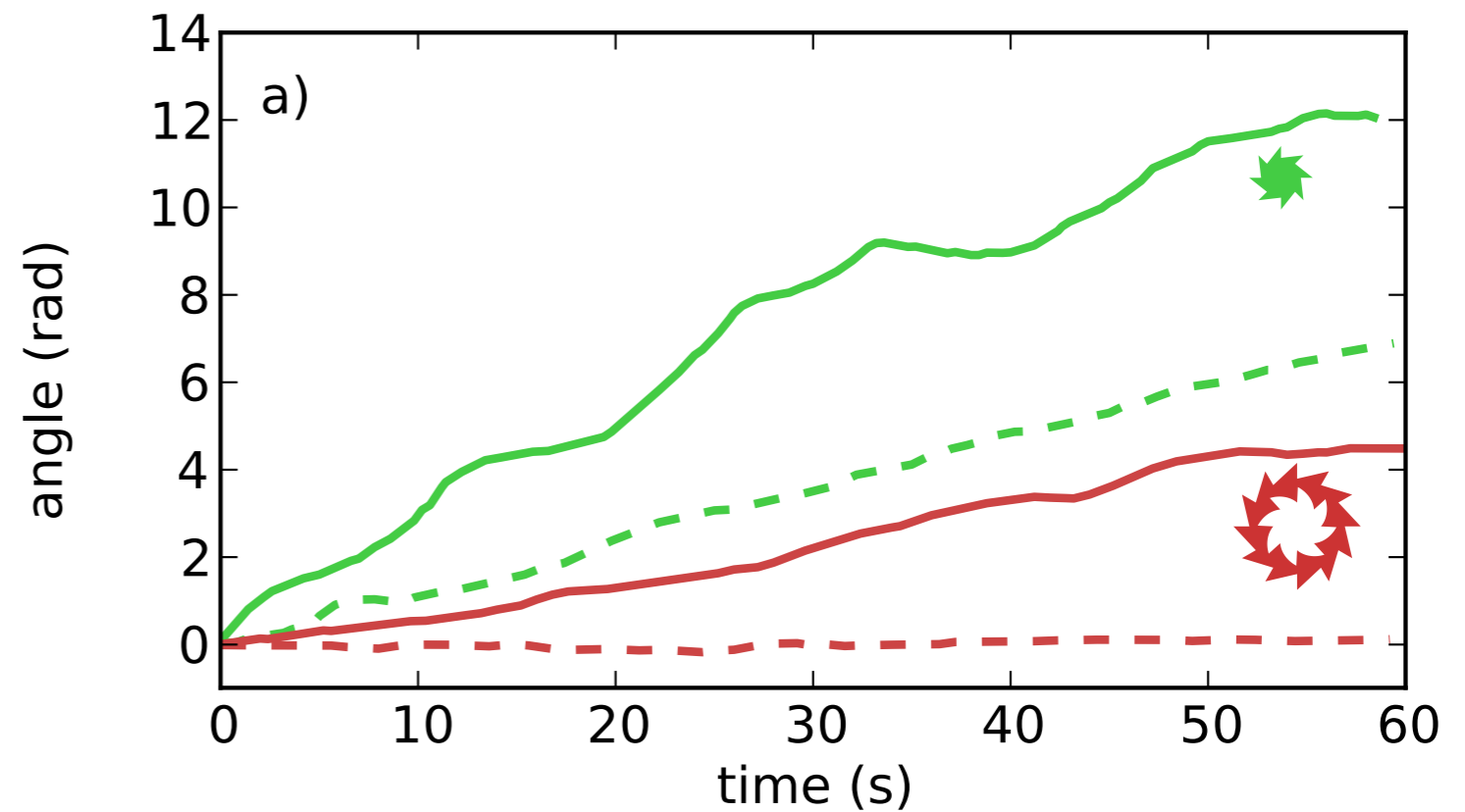
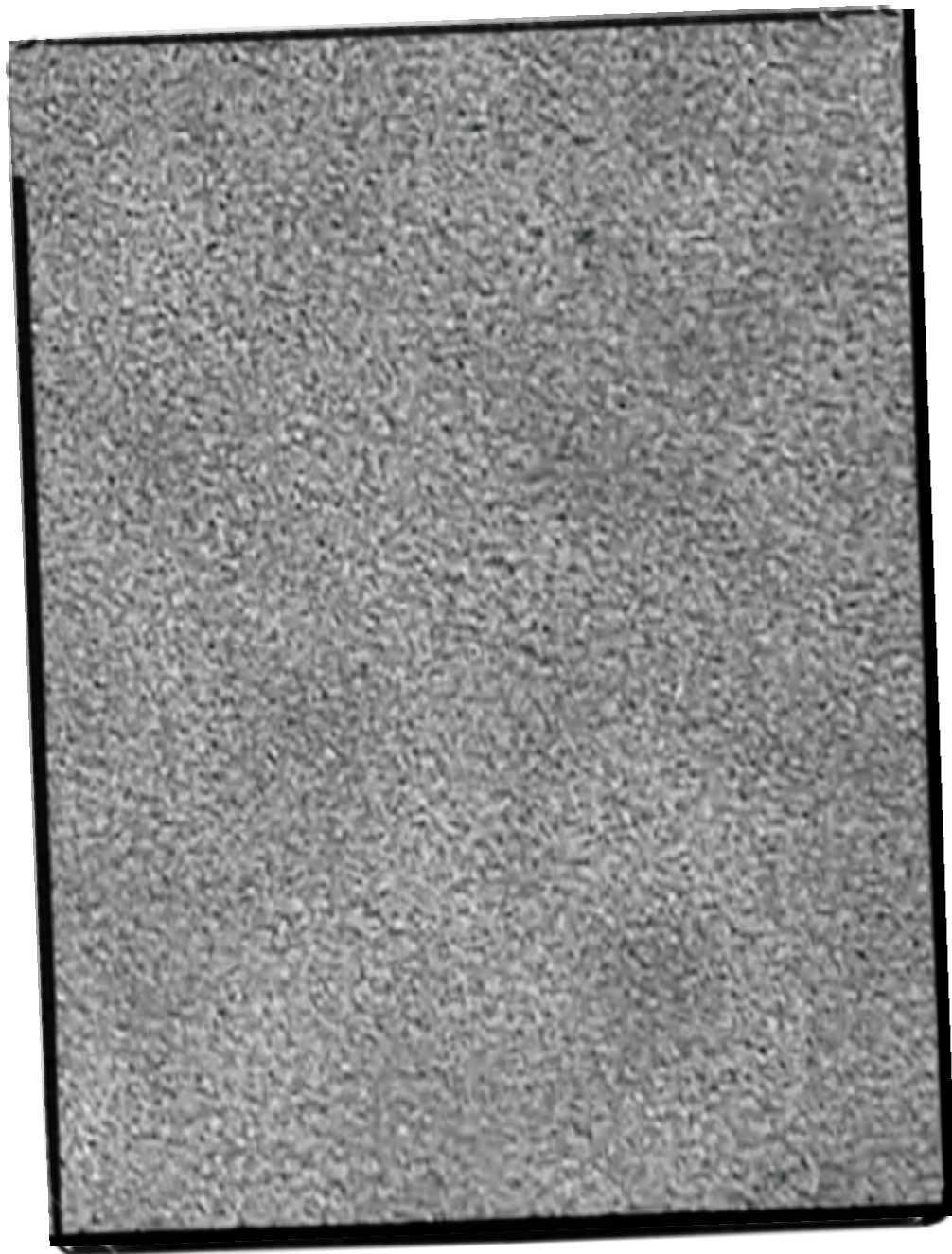
**nature**  
RESEARCH HIGHLIGHTS

# Bacteria-boundary interaction



# High concentration regime

$\sim 10^{11}$   
BACTERIA/ML



## STOCHASTIC DYNAMICS IN ACTIVE BATHS

- persistent (non FDT) forces due to bacteria generate stationary states characterized by probability distributions that strongly deviate from Boltzmann
- these stationary states are also microscopically not invariant under time reversal
- these peculiar properties of active matter allow to exploit bacteria as a workforce in miniaturized environments

## PHYSICS AT THE MICRON SCALE

### PEOPLE



R. DI LEONARDO



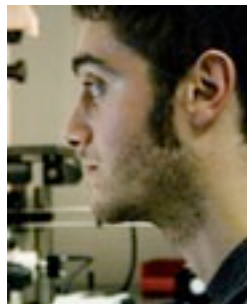
C. MAGGI



N. KOUMAKIS



M. PAOLUZZI



S. BIANCHI



A. LEPORE



F. SAGLIMBENI



G. VIZSNYICZAI

### COLLABORATIONS

L. ANGELANI, CNR-IPCF SAPIENZA

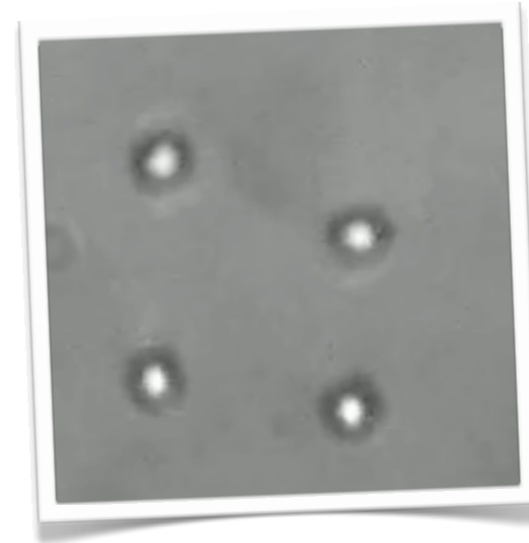
E DI FABRIZIO, C. LIBERALE, KAUST, SAUDI ARABIA

### FUNDING



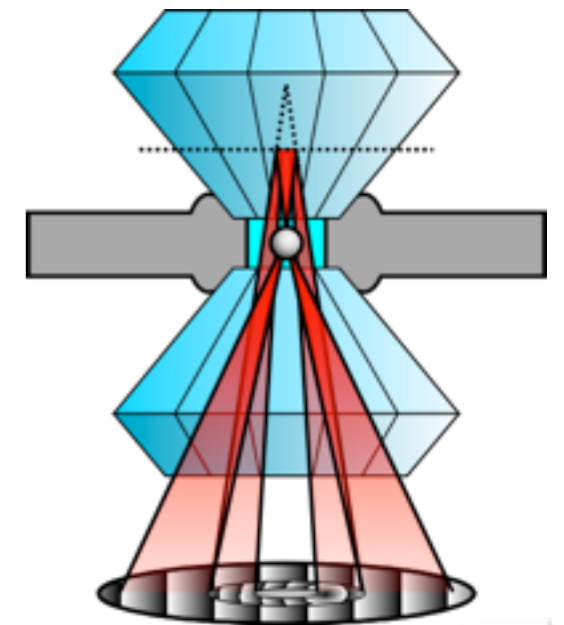
### HYDRO SYNC IN ROTATING LANDSCAPES

KOUMAKIS & RDL, PRL (2013)



### TRAPPING AT GPa

BOWMAN, GIBSON, PADGETT,  
SAGLIMBENI, RDL PRL (2013).



### IMAGING THROUGH OPTICAL FIBERS

BIANCHI & RDL LAB CHIP (2011)

